

Second Edition

Quantum Mechanícs

G. Aruldhas



QUANTUM MECHANICS

SECOND EDITION

G. ARULDHAS

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To

My Parents

Gnanasigamoni & Rajammal

who taught me the merits of discipline and the rewards of education

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