

Exercise 9A

1. **Sol:**

Mean of given observations = $\frac{\text{sum of given observations}}{\text{total number of observations}}$

$$\therefore 11 = \frac{x + (x+2) + (x+4) + (x+6) + (x+8)}{5}$$

$$\Rightarrow 55 = 5x + 20$$

$$\Rightarrow 5x = 55 - 20$$

$$\Rightarrow 5x = 35$$

$$\Rightarrow x = \frac{35}{5}$$

$$\Rightarrow x = 7$$

Hence, the value of x is 7.

2.

Sol:

Mean of given observations = $\frac{\text{sum of given observations}}{\text{total number of observations}}$

Mean of 25 observations = 27

$$\therefore \text{Sum of 25 observations} = 27 \times 25 = 675$$

$$\begin{aligned} \text{If 7 is subtracted from every number, then the sum} &= 675 - (25 \times 7) \\ &= 675 - 175 \\ &= 500 \end{aligned}$$

$$\text{Then, new mean} = \frac{500}{25} = 20$$

Thus, the new mean will be 20.

3.

Sol:

The given data is shown as follows:

Class	Frequency (f_i)	Class mark (x_i)	$f_i x_i$
1 - 3	12	2	24
3 - 5	22	4	88
5 - 7	27	6	162
7 - 9	19	8	152
Total	$\Sigma f_i = 80$		$\Sigma f_i x_i = 426$

The mean of given data is given by

$$\begin{aligned}\bar{x} &= \frac{\sum_i f_i x_i}{\sum_i f_i} \\ &= \frac{426}{80} \\ &= 5.325\end{aligned}$$

Thus, the mean of the following data is 5.325.

4.

Sol:

Class	Frequency (f _i)	Mid values (x _i)	f _i × x _i
0 – 10	7	5	35
10 – 20	5	15	75
20 – 30	6	25	150
30 – 40	12	35	420
40 – 50	8	45	360
50 – 60	2	55	110
	Σ f _i = 40		Σ (f _i × x _i) = 1150

$$\begin{aligned}\therefore \text{Mean, } \bar{x} &= \frac{\sum (f_i \times x_i)}{\sum f_i} \\ &= \frac{1150}{40} \\ &= 28.75 \\ \therefore \bar{x} &= 28.75\end{aligned}$$

5.

Sol:

Class	Frequency (f _i)	Mid values (x _i)	(f _i × x _i)
25 – 35	6	30	180
35 – 45	10	40	400
45 – 55	8	50	400
55 – 65	12	60	720
65 – 75	4	70	280
	Σ f _i = 40		Σ (f _i × x _i) = 1980

$$\therefore \text{Mean, } \bar{x} = \frac{\sum(f_i \times x_i)}{\sum f_i}$$

$$= \frac{1980}{40}$$

$$= 49.5$$

$$\therefore \bar{x} = 49.5$$

6.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	($f_i \times x_i$)
0 - 100	6	50	300
100 - 200	9	150	1350
200 - 300	15	250	3750
300 - 400	12	350	4200
400 - 500	8	450	3600
	$\Sigma f_i = 50$		$\Sigma(f_i \times x_i) = 13200$

$$\therefore \text{Mean, } \bar{x} = \frac{\sum(f_i \times x_i)}{\sum f_i}$$

$$= \frac{13200}{50}$$

$$= 264$$

$$\therefore \bar{x} = 264$$

7.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	($f_i \times x_i$)
84 - 90	8	87	696
90 - 96	10	93	930
96 - 102	16	99	1584
102 - 108	23	105	2415
108 - 114	12	111	1332
114 - 120	11	117	1287
Total	$\Sigma f_i = 80$		$\Sigma f_i x_i = 8244$

The mean of the data is given by,

$$\begin{aligned}\bar{x} &= \frac{\sum_i f_i x_i}{\sum_i f_i} \\ &= \frac{8244}{80} \\ &= 103.05\end{aligned}$$

Thus, the mean of the following data is 103.05.

8.

Sol:

The given data is shown as follows:

Class	Frequency (f_i)	Mid values (x_i)	($f_i x_i$)
0 – 10	3	5	15
10 – 20	4	15	60
20 – 30	p	25	25p
30 – 40	3	35	105
40 – 50	2	45	90
Total	$\sum f_i = 12 + p$		$\sum f_i x_i = 270 + 25p$

The mean of the given data is given by,

$$\bar{x} = \frac{\sum_i f_i x_i}{\sum_i f_i}$$

$$\Rightarrow 24 = \frac{270+25p}{12+p}$$

$$\Rightarrow 24(12 + p) = 270 + 25p$$

$$\Rightarrow 288 + 24p = 270 + 25p$$

$$\Rightarrow 25p - 24p = 288 - 270$$

$$\Rightarrow p = 18$$

Hence, the value of p is 18.

9.

Sol:

The given data is shown as follows:

Daily pocket allowance (in ₹)	Number of children (f_i)	Class mark (x_i)	$f_i x_i$
11 – 13	7	12	84
13 – 15	6	14	84
15 – 17	9	16	144
17 – 19	13	18	234
19 – 21	f	20	$20f$
21 – 23	5	22	110
23 – 25	4	24	96
Total	$\Sigma f_i = 44 + f$		$\Sigma f_i x_i = 752 + 20f$

The mean of the given data is given by,

$$\bar{x} = \frac{\sum f_i x_i}{\sum f_i}$$

$$\Rightarrow 18 = \frac{750+20f}{44+f}$$

$$\Rightarrow 18(44 + f) = 752 + 20f$$

$$\Rightarrow 792 + 18f = 752 + 20f$$

$$\Rightarrow 20f - 18f = 792 - 752$$

$$\Rightarrow 2f = 40$$

$$\Rightarrow f = 20$$

Hence, the value of f is 20.

10.

Sol:

The given data is shown as follows:

Class	Frequency (f_i)	Class mark (x_i)	$f_i x_i$
0 – 20	7	10	70
20 – 40	p	30	$30p$
40 – 60	10	50	500
60 – 80	9	70	630
80 – 100	13	90	1170
Total	$\Sigma f_i = 39 + p$		$\Sigma f_i x_i = 2370 + 30p$

The mean of the given data is given by,

$$\bar{x} = \frac{\sum_i f_i x_i}{\sum_i f_i}$$

$$\Rightarrow 54 = \frac{2370+30p}{39+p}$$

$$\Rightarrow 54 (39 + p) = 2370 + 30p$$

$$\Rightarrow 2106 + 54p = 2370 - 2106$$

$$\Rightarrow 24p = 264$$

$$\Rightarrow p = 11$$

Hence, the value of p is 11.

11.

Sol:

The given data is shown as follows:

Class interval	Frequency (f_i)	Class mark (x_i)	$f_i x_i$
0 – 10	7	5	35
10 – 20	10	15	150
20 – 30	x	25	25x
30 – 40	13	35	455
40 – 50	y	45	45y
50 – 60	10	55	550
60 – 70	14	65	910
70 – 80	9	75	675
Total	$\sum f_i = 63 + x + y$		$\sum f_i x_i = 2775 + 25x + 45y$

Sum of the frequencies = 100

$$\Rightarrow \sum_i f_i = 100$$

$$\Rightarrow 63 + x + y = 100$$

$$\Rightarrow x + y = 100 - 63$$

$$\Rightarrow x + y = 37$$

$$\Rightarrow y = 37 - x \quad \dots\dots(1)$$

Now, the mean of the given data is given by,

$$\bar{x} = \frac{\sum_i f_i x_i}{\sum_i f_i}$$

$$\Rightarrow 42 = \frac{2775 + 25x + 45y}{100}$$

$$\Rightarrow 4200 = 2775 + 25x + 45y$$

$$\Rightarrow 4200 - 2775 = 25x + 45y$$

$$\Rightarrow 1425 = 25x + 45(37 - x) \quad [\text{from (1)}]$$

$$\Rightarrow 1425 = 25x + 1665 - 45x$$

$$\Rightarrow 20x = 1665 - 1425$$

$$\Rightarrow 20x = 240$$

$$\Rightarrow x = 12$$

If $x = 12$, then $y = 37 - 12 = 25$

Thus, the value of x is 12 and y is 25.

12.

Sol:

The given data is shown as follows:

Expenditure (in ₹)	Number of families (f_i)	Class mark (x_i)	$f_i x_i$
140 – 160	5	150	750
160 – 180	25	170	4250
180 – 200	f_1	190	$190f_1$
200 – 220	f_2	210	$210f_2$
220 – 240	5	230	1150
Total	$\Sigma f_i = 35 + f_1 + f_2$		$\Sigma f_i x_i = 6150 + 190f_1 + 210f_2$

Sum of the frequencies = 100

$$\Rightarrow \Sigma_i f_i = 100$$

$$\Rightarrow 35 + f_1 + f_2 = 100$$

$$\Rightarrow f_1 + f_2 = 100 - 35$$

$$\Rightarrow f_1 + f_2 = 65$$

$$\Rightarrow f_2 = 65 - f_1 \quad \dots\dots(1)$$

Now, the mean of the given data is given by,

$$\bar{x} = \frac{\sum_i f_i x_i}{\sum_i f_i}$$

$$\Rightarrow 188 = \frac{6150 + 190f_1 + 210f_2}{100}$$

$$\Rightarrow 18800 = 6150 + 190f_1 + 210f_2$$

$$\Rightarrow 18800 - 6150 = 190f_1 + 210f_2$$

$$\Rightarrow 12650 = 190f_1 + 210(65 - f_1) \quad \text{[from (1)]}$$

$$\Rightarrow 12650 = 190f_1 - 210f_1 + 13650$$

$$\Rightarrow 20f_1 = 13650 - 12650$$

$$\Rightarrow 20f_1 = 1000$$

$$\Rightarrow f_1 = 50$$

If $f_1 = 50$, then $f_2 = 65 - 50 = 15$

Thus, the value of f_1 is 50 and f_2 is 15.

13.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	($f_i \times x_i$)
0 - 20	7	10	70
20 - 40	f_1	30	$30f_1$
40 - 60	12	50	600
60 - 80	$18 - f_1$	70	$1260 - 70f_1$
80 - 100	8	90	720
100 - 120	5	110	550
Total	$\Sigma f_i = 50$		$\Sigma (f_i \times x_i) = 3200 - 40f_1$

We have:

$$7 + f_1 + 12 + f_2 + 8 + 5 = 50$$

$$\Rightarrow f_1 + f_2 = 18$$

$$\Rightarrow f_2 = 18 - f_1$$

$$\therefore \text{Mean, } \bar{x} = \frac{\Sigma_i (f_i \times x_i)}{\Sigma_i f_i}$$

$$\Rightarrow 57.6 = \frac{3200 - 40f_1}{50}$$

$$\Rightarrow 40f_1 = 320$$

$$\therefore f_1 = 8$$

$$\text{And } f_2 = 18 - 8$$

$$\Rightarrow f_2 = 10$$

\therefore The missing frequencies are $f_1 = 8$ and $f_2 = 10$.

14.

Sol:

Using Direct method, the given data is shown as follows:

Number of heartbeats per minute	Number of patients (f_i)	Class mark (x_i)	$f_i x_i$
65 – 68	2	66.5	133
68 – 71	4	69.5	278
71 – 74	3	72.5	217.5
74 – 77	8	75.5	604
77 – 80	7	78.5	549.5
80 – 83	4	81.5	326
83 – 86	2	84.5	169
Total	$\Sigma f_i = 30$		$\Sigma f_i x_i = 2277$

The mean of the data is given by,

$$\begin{aligned}\bar{x} &= \frac{\sum_i f_i x_i}{\sum_i f_i} \\ &= \frac{2277}{30} \\ &= 75.9\end{aligned}$$

Thus, the mean heartbeats per minute for these patients is 75.9.

15.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	Deviation (d_i) $d_i = (x_i - 25)$	$(f_i \times d_i)$
0 – 10	12	5	-20	-240
10 – 20	18	15	-10	-180
20 – 30	27	25 = A	0	0
30 – 40	20	35	10	200
40 – 50	17	45	20	340
50 – 60	6	55	30	180
Total	$\Sigma f_i = 100$			$\Sigma (f_i \times d_i) = 300$

Let A = 25 be the assumed mean. Then we have:

$$\begin{aligned} \text{Mean, } \bar{x} &= A + \frac{\Sigma(f_i \times d_i)}{\Sigma f_i} \\ &= 25 + \frac{300}{100} \\ &= 28 \\ \therefore \bar{x} &= 28 \end{aligned}$$

16.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	Deviation (d_i) $d_i = (x_i - 150)$	$(f_i \times d_i)$
100 – 120	10	110	-40	-400
120 – 140	20	130	-20	-400
140 – 160	30	150 = A	0	0
160 – 180	15	170	20	300
180 – 200	5	190	40	200
	$\Sigma f_i = 80$			$\Sigma (f_i \times d_i) = -300$

Let A = 150 be the assumed mean. Then we have:

$$\begin{aligned} \text{Mean, } \bar{x} &= A + \frac{\Sigma(f_i \times d_i)}{\Sigma f_i} \\ &= 150 - \frac{300}{80} \\ &= 150 - 3.75 \\ \therefore \bar{x} &= 146.25 \end{aligned}$$

17.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	Deviation (d_i) $d_i = (x_i - 50)$	$(f_i \times d_i)$
0 – 20	20	10	-40	-800
20 – 40	35	30	-20	-700
40 – 60	52	50 = A	0	0
60 – 80	44	70	20	880
80 – 100	38	90	40	1520
100 – 120	31	110	60	1860
	$\Sigma f_i = 220$			$\Sigma (f_i \times d_i) = 2760$

Let A = 50 be the assumed mean. Then we have:

$$\begin{aligned} \text{Mean, } \bar{x} &= A + \frac{\Sigma (f_i \times d_i)}{\Sigma f_i} \\ &= 50 + \frac{2760}{220} \\ &= 50 + 12.55 \\ \therefore \bar{x} &= 62.55 \end{aligned}$$

18.

Sol:

Using Direct method, the given data is shown as follows:

Literacy rate (%)	Number of cities (f_i)	Class mark (x_i)	$(f_i x_i)$
45 – 55	4	50	200
55 – 65	11	60	660
65 – 75	12	70	840
75 – 85	9	80	720
85 – 95	4	90	360
Total	$\Sigma f_i = 40$		$\Sigma f_i x_i = 2780$

The mean of the data is given by,

$$\bar{x} = \frac{\sum_i f_i x_i}{\sum_i f_i}$$

$$= \frac{2780}{40}$$

$$= 69.5$$

Thus, the mean literacy rate is 69.5%.

19.

Sol:

Let us choose $a = 25$, $h = 10$, then $d_i = x_i - 25$ and $u_i = \frac{x_i - 25}{10}$

Using step-deviation method, the given data is shown as follows:

Class	Frequency (f_i)	Class mark (x_i)	$d_i = x_i - 25$	$u_i = \frac{x_i - 25}{10}$	$(f_i u_i)$
0 – 10	7	5	-20	-2	-14
10 – 20	10	15	-10	-1	-10
20 – 30	15	25	0	0	0
30 – 40	8	35	10	1	8
40 – 50	10	45	20	2	20
Total	$\Sigma f_i = 50$				$\Sigma f_i u_i = 4$

The mean of the data is given by,

$$\bar{x} = a + \left(\frac{\Sigma f_i u_i}{\Sigma f_i} \right) \times h$$

$$= 25 + \frac{4}{50} \times 10$$

$$= 25 + \frac{4}{5}$$

$$= \frac{125 + 4}{5}$$

$$= \frac{129}{5}$$

$$= 25.8$$

Thus, the mean is 25.8.

20.

Sol:

Let us choose $a = 40$, $h = 10$, then $d_i = x_i - 40$ and $u_i = \frac{x_i - 40}{10}$

Using step-deviation method, the given data is shown as follows:

Class	Frequency (f_i)	Class mark (x_i)	$d_i = x_i - 40$	$u_i = \frac{x_i - 40}{10}$	$(f_i u_i)$
5 – 15	6	10	-30	-3	-18
15 – 25	10	20	-20	-2	-20
25 – 35	16	30	-10	-1	-16

35 – 45	15	40	0	0	0
45 – 55	24	50	10	1	24
55 – 65	8	60	20	2	16
65 – 75	7	70	30	3	21
Total	$\Sigma f_i = 86$				$\Sigma f_i u_i = 7$

The mean of the data is given by,

$$\begin{aligned}\bar{x} &= a + \left(\frac{\sum_i f_i u_i}{\sum_i f_i} \right) \times h \\ &= 40 + \frac{7}{86} \times 10 \\ &= 40 + \frac{70}{86} \\ &= 40 + 0.81 \\ &= 40.81\end{aligned}$$

21.

Sol:

Let us choose $a = 202.5$, $h = 1$, then $d_i = x_i - 202.5$ and $u_i = \frac{x_i - 202.5}{1}$

Using step-deviation method, the given data is shown as follows:

Weight	Number of packets (f_i)	Class mark (x_i)	$d_i = x_i - 202.5$	$u_i = \frac{x_i - 202.5}{1}$	$(f_i u_i)$
200 - 201	13	200.5	-2	-2	-26
201 – 202	27	201.5	-1	-1	-27
202 – 203	18	202.5	0	0	0
203 – 204	10	203.5	1	1	10
204 – 205	1	204.5	2	2	2
205 – 206	1	205.5	3	3	3
Total	$\Sigma f_i = 70$				$\Sigma f_i u_i = -38$

The mean of the given data is given by,

$$\begin{aligned}\bar{x} &= a + \left(\frac{\sum_i f_i u_i}{\sum_i f_i} \right) \times h \\ &= 202.5 + \left(\frac{-38}{70} \right) \times 1 \\ &= 202.5 - 0.542 \\ &= 201.96\end{aligned}$$

Hence, the mean is 201.96 g.

22.

Sol:

Let us choose $a = 45$, $h = 10$, then $d_i = x_i - 45$ and $u_i = \frac{x_i - 45}{10}$

Using step-deviation method, the given data is shown as follows:

Weight	Number of packets (f_i)	Class mark (x_i)	$d_i = x_i - 45$	$u_i = \frac{x_i - 45}{10}$	$(f_i u_i)$
20 – 30	25	35	-20	-2	-50
30 – 40	40	35	-10	-1	-40
40 – 50	42	45	0	0	0
50 – 60	33	55	10	1	33
60 – 70	10	65	20	2	20
Total	$\Sigma f_i = 150$				$\Sigma f_i u_i = -37$

The mean of the given data is given by,

$$\begin{aligned} \bar{x} &= a + \left(\frac{\sum f_i u_i}{\sum f_i} \right) \times h \\ &= 45 - \left(\frac{37}{150} \right) \times 10 \\ &= 45 - \frac{37}{15} \\ &= 45 - 2.466 \\ &= 42.534 \end{aligned}$$

Hence, the mean is 42.534.

23.

Find the mean marks.

Sol:

Let us choose $a = 52.5$, $h = 15$, then $d_i = x_i - 52.5$ and $u_i = \frac{x_i - 52.5}{15}$

Using step-deviation method, the given data is shown as follows:

Weight	Number of students (f_i)	Class mark (x_i)	$d_i = x_i - 37.5$	$u_i = \frac{x_i - 52.5}{15}$	$(f_i u_i)$
0 – 15	2	7.5	-45	-3	-6
15 – 30	4	22.5	-30	-2	-8
30 – 45	5	37.5	-15	-1	-5

45 – 60	20	52.5	0	0	0
60 – 75	9	67.5	15	1	9
75 – 90	10	82.5	30	2	20
Total	$\Sigma f_i = 50$				$\Sigma f_i u_i = 10$

The mean of the given data is given by,

$$\begin{aligned}\bar{x} &= a + \left(\frac{\sum_i f_i u_i}{\sum_i f_i} \right) \times h \\ &= 52.5 + \left(\frac{10}{50} \right) \times 15 \\ &= 52.5 + 3 \\ &= 55.5\end{aligned}$$

Thus, the mean is 55.5.

24.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	$u_i = \frac{(x_i - A)}{h}$ $= \frac{(x_i - 33)}{6}$	$(f_i \times u_i)$
18 – 24	6	21	-2	-12
24 – 30	8	27	-1	-8
30 – 36	12	33 = A	0	0
36 – 42	8	39	1	8
42 – 48	4	45	2	8
48 – 54	2	51	3	6
Total	$\Sigma f_i = 40$			$\Sigma (f_i \times u_i) = 2$

Now, $A = 33$, $h = 6$, $\Sigma f_i = 40$ and $\Sigma (f_i \times u_i) = 2$

$$\begin{aligned}\therefore \text{Mean, } \bar{x} &= A + \left\{ h \times \frac{\sum (f_i \times u_i)}{\sum f_i} \right\} \\ &= 33 + \left\{ 6 \times \frac{2}{40} \right\} \\ &= 33 + 0.3 \\ &= 33.3\end{aligned}$$

$\therefore \bar{x} = 33.3$ years

25.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	$u_i = \frac{(x_i - A)}{h}$ $= \frac{(x_i - 550)}{20}$	($f_i \times u_i$)
500 – 520	14	510	-2	-28
520 – 540	9	530	-1	-9
540 – 560	5	550 = A	0	0
560 – 580	4	570	1	4
580 – 600	3	590	2	6
600 – 620	5	610	3	15
	$\Sigma f_i = 40$			$\Sigma (f_i \times u_i) = -12$

Now, $A = 550$, $h = 20$, $\Sigma f_i = 40$ and $\Sigma (f_i \times u_i) = -12$

$$\therefore \text{Mean, } \bar{x} = A + \left\{ h \times \frac{\Sigma (f_i \times u_i)}{\Sigma f_i} \right\}$$

$$= 550 + \left\{ 20 \times \frac{(-12)}{40} \right\}$$

$$= 550 - 6$$

$$= 544$$

$$\therefore \bar{x} = 544$$

26.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	$u_i = \frac{(x_i - A)}{h}$ $= \frac{(x_i - 42)}{5}$	($f_i \times u_i$)
24.5 – 29.5	4	27	-3	-12
29.5 – 34.5	14	32	-2	-28
34.5 – 39.5	22	37	-1	-22
39.5 – 44.5	16	42 = A	0	0
44.5 – 49.5	6	47	1	6
49.5 – 54.5	5	52	2	10
54.5 – 59.5	3	57	3	9
	$\Sigma f_i = 70$			$\Sigma (f_i \times u_i) = -37$

Now, $A = 42$, $h = 5$, $\Sigma f_i = 70$ and $\Sigma (f_i \times u_i) = -37$

$$\begin{aligned} \therefore \text{Mean, } \bar{x} &= A + \left\{ h \times \frac{\sum (f_i \times u_i)}{\sum f_i} \right\} \\ &= 42 + \left\{ 5 \times \frac{(-37)}{70} \right\} \\ &= 42 - 2.64 \\ &= 39.36 \\ \therefore \bar{x} &= 39.36 \\ \therefore \text{Mean age} &= 39.36 \text{ years.} \end{aligned}$$

27.

Sol:

Class	Frequency (f_i)	Mid values (x_i)	$u_i = \frac{(x_i - A)}{h}$ $= \frac{(x_i - 29.5)}{10}$	($f_i \times u_i$)
4.5 – 14.5	6	9.5	-2	-12
14.5 – 24.5	11	19.5	-1	-11
24.5 – 34.5	21	29.5 = A	0	0
34.5 – 44.5	23	39.5	1	23
44.5 – 54.5	14	49.5	2	28
54.5 – 64.5	5	59.5	3	15
	$\sum f_i = 80$			$\sum (f_i \times u_i) = 43$

Now, $A = 29.5$, $h = 10$, $\sum f_i = 80$ and $\sum (f_i \times u_i) = 43$

$$\begin{aligned} \therefore \text{Mean, } \bar{x} &= A + \left\{ h \times \frac{\sum (f_i \times u_i)}{\sum f_i} \right\} \\ &= 29.5 + \left\{ 10 \times \frac{43}{80} \right\} \\ &= 29.5 + 5.375 \\ &= 34.875 \\ \therefore \bar{x} &= 34.875 \end{aligned}$$

\therefore The average age of the patients is 34.87 years.

28.

Sol:

Let us choose $a = 92$, $h = 5$, then $d_i = x_i - 92$ and $u_i = \frac{x_i - 92}{5}$

Using step-deviation method, the given data is shown as follows:

Weight (in grams)	Number of eggs (f_i)	Class mark (x_i)	$d_i = x_i - 92$	$u_i = \frac{x_i - 92}{5}$	$(f_i u_i)$
74.5 – 79.5	4	77	-15	-3	-12
79.5 – 84.5	9	82	-10	-2	-18
84.5 – 89.5	13	87	-5	-1	-13
89.5 – 94.5	17	92	0	0	0
94.5 – 99.5	12	97	5	1	12
99.5 – 104.5	3	102	10	2	6
104.5 – 109.5	2	107	15	3	6
Total	$\Sigma f_i = 60$				$\Sigma f_i u_i = -19$

The mean of the given data is given by,

$$\begin{aligned}\bar{x} &= a + \left(\frac{\sum f_i u_i}{\sum f_i} \right) \times h \\ &= 92 + \left(\frac{-19}{60} \right) \times 5 \\ &= 92 - 1.58 \\ &= 90.42 \\ &\approx 90\end{aligned}$$

Thus, the mean weight to the nearest gram is 90 g.

29.

Sol:

Let us choose $a = 17.5$, $h = 5$, then $d_i = x_i - 17.5$ and $u_i = \frac{x_i - 17.5}{5}$

Using step-deviation method, the given data is shown as follows:

Marks	Number of students (cf)	Frequency (f_i)	Class mark (x_i)	$d_i = x_i - 17.5$	$u_i = \frac{x_i - 17.5}{5}$	$(f_i u_i)$
0 – 5	3	3	2.5	-15	-3	-9
5 – 10	10	7	7.5	-10	-2	-14
10 – 15	25	15	12.5	-5	-1	-15
15 – 20	49	24	17.5	0	0	0
20 – 25	65	16	22.5	5	1	16
25 – 30	73	8	27.5	10	2	16
30 – 35	78	5	32.5	15	3	15
35 – 40	80	2	37.5	20	4	8

Total		$\Sigma f_i = 80$				$\Sigma f_i u_i = 17$
-------	--	-------------------	--	--	--	-----------------------

The mean of the given data is given by,

$$\begin{aligned}\bar{x} &= a + \left(\frac{\sum_i f_i u_i}{\sum_i f_i} \right) \times h \\ &= 17.5 + \left(\frac{17}{80} \right) \times 5 \\ &= 17.5 + 1.06 \\ &= 18.56\end{aligned}$$

Thus, the mean marks correct to 2 decimal places is 18.56.

