
AREAS OF TRIANGLES AND QUADRILATERALS

CHAPTER 14

EXERCISE 14

Answer1 : Given: Base = 24 cm
Height = 14.5 cm

$$\text{Area of triangle} = \frac{1}{2} \times \text{Base} \times \text{Height} = \frac{1}{2} \times 24 \times 14.5 = 174 \text{ cm}^2$$

Answer2 : Let the height of the triangle be h m.

$$\therefore \text{Base} = 3h \text{ m}$$

$$\text{Area of the triangle} = \text{Total Cost/Rate} = 783/58 = 13.5 \text{ ha} = 135000 \text{ m}^2$$

$$\text{Area of triangle} = 135000 \text{ m}^2 \Rightarrow \frac{1}{2} \times \text{Base} \times \text{Height} = 135000 \Rightarrow \frac{1}{2} \times 3h \times h = 135000$$

$$\Rightarrow h^2 = 90000$$

$$\Rightarrow h = \sqrt{90000}$$

$$\Rightarrow h = 300 \text{ m}$$

Thus, we have:

$$\text{Height} = h = 300 \text{ m}$$

$$\text{Base} = 3h = 900 \text{ m}$$

Answer3 : Let, $a = 42$ cm, $b = 34$ cm and $c = 20$ cm

$$\therefore s = (a+b+c)/2 = (42+34+20)/2 = 48 \text{ cm}$$

By Heron's formula,

$$\text{Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{48(48-42)(48-34)(48-20)}$$

$$= \sqrt{48 \times 6 \times 14 \times 28}$$

$$= 4 \times 2 \times 6 \times 7$$

$$= 336 \text{ cm}^2$$

We know that the longest side is 42 cm.

Thus, we can find out the height of the triangle corresponding to 42 cm.

Area of triangle =

$$\Rightarrow 336 \text{ cm}^2 = \frac{1}{2} \times \text{Base} \times \text{Height}$$

$$\Rightarrow \text{Height} = \frac{336 \times 2}{42} = 16 \text{ cm}$$

Answer4: Let: $a=18$ cm, $b = 24$ cm and $c=30$ cm

$$\therefore s = (a+b+c)/2 = (24+18+30)/2 = 36 \text{ cm}$$

By Heron's formula,

$$\text{Area of triangle} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[36(36-18)(36-24)(36-30)]}$$

$$= \sqrt{(36 \times 18 \times 12 \times 6)}$$

$$= 12 \times 3 \times 6$$

$$= 216 \text{ cm}^2$$

We know that the smallest side is 18 cm.

Thus, we can find out the height of the triangle corresponding to 18 cm.

Area of triangle

$$\Rightarrow 216 \text{ cm}^2 = \frac{1}{2} \times \text{Base} \times \text{Height}$$

$$\Rightarrow \text{Height} = \frac{2 \times 216}{18} = 24 \text{ cm}$$

Answer5: Let: $a=91$ m, $b = 98$ m and $c=105$ m

$$\therefore s = (a+b+c)/2 = (91+98+105)/2 = 147 \text{ m}$$

By Heron's formula,

$$\text{Area of triangle} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[147(147-91)(147-98)(147-105)]}$$

$$= \sqrt{(147 \times 56 \times 49 \times 42)}$$

$$= 7 \times 7 \times 7 \times 2 \times 3 \times 2$$

$$= 4116 \text{ m}^2$$

We know that the longest side is 105 m.

Thus, we can find out the height of the triangle corresponding to 42 cm.

$$\text{Area of triangle} = 4116 \text{ m}^2 \Rightarrow \frac{1}{2} \times \text{Base} \times \text{Height} = 4116 \Rightarrow \text{Height} = 78.4 \text{ m}$$

Answer6: Let the sides of the triangle be $5x$ m, $12x$ m and $13x$ m.

Perimeter = Sum of all sides

$$\text{or, } 150 = 5x + 12x + 13x$$

$$\text{or, } 30x = 150$$

$$\text{or, } x = 5$$

Thus, we obtain the sides of the triangle.

$$5 \times 5 = 25 \text{ m}$$

$$12 \times 5 = 60 \text{ m}$$

$$13 \times 5 = 65 \text{ m}$$

Now ATQ,

$$\text{Let: } a=25 \text{ m, } b = 60 \text{ m and } c=65 \text{ m}$$

$$\therefore s = 150/2 = 75 \text{ m}$$

By Heron's formula,

$$\text{Area of triangle} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[75(75-25)(75-60)(75-65)]} = \sqrt{(75 \times 50 \times 15 \times 10)}$$

$$= 15 \times 5 \times 10$$

$$= 750 \text{ m}^2$$

Answer7 : Let the sides of the triangle be $25x$ m, $17x$ m and $12x$ m.

Perimeter = Sum of all sides

$$\text{or, } 540 = 25x + 17x + 12x$$

$$\text{or, } 54x = 540$$

$$\text{or, } x = 10$$

Thus, we obtain the sides of the triangle.

$$25 \times 10 = 250 \text{ m}$$

$$17 \times 10 = 170 \text{ m}$$

$$12 \times 10 = 120 \text{ m}$$

Let, $a=250 \text{ m}$, $b=170 \text{ m}$ and $c=120 \text{ m}$

$$\therefore s = 540/2 = 270 \text{ m}$$

By Heron's formula,

$$\text{Area of triangle} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[270(270-250)(270-170)(270-120)]}$$

$$= \sqrt{(270 \times 20 \times 100 \times 150)}$$

$$= 30 \times 3 \times 20 \times 5$$

$$= 9000 \text{ m}^2$$

Cost of ploughing 10 m^2 field = Rs 18.80

Cost of ploughing 1 m^2 field = Rs 18.8/10

Cost of ploughing 9000 m^2 field = $18.8/10 \times 9000 = \text{Rs } 16920$

Answer 8: (i) Let, $a=85 \text{ m}$ and $b=154 \text{ m}$

Given: Perimeter = 324 m

$$\text{or, } a+b+c=324$$

$$\Rightarrow c = 324 - a - b$$

$$\Rightarrow c = 324 - 85 - 154 = 85 \text{ m}$$

$$\therefore s = \frac{324}{2} = 162 \text{ m}$$

By Heron's formula,

$$\text{Area of triangle} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[162(162-85)(162-154)(162-85)]}$$

$$= \sqrt{(162 \times 77 \times 8 \times 77)}$$

$$= \sqrt{(1296 \times 77 \times 77)}$$

$$= \sqrt{(36 \times 77 \times 77 \times 36)}$$

$$=36 \times 77$$

$$=2772 \text{ m}^2$$

(ii) We can find out the height of the triangle corresponding to 154 m in the following manner:

Area of triangle

$$\Rightarrow 2772 \text{ m}^2 = \frac{1}{2} \times \text{Base} \times \text{Height}$$

$$\Rightarrow \text{Height} = (2772 \times 2) / 154 = 36 \text{ m}$$

Answer9: Given : $a=13 \text{ cm}$ and $b=20 \text{ cm}$

$$\therefore \text{Area of isosceles triangle} = \frac{b}{4} \times \sqrt{(4a^2 - b^2)} = \frac{20}{4} \times \sqrt{[4(13)^2 - 20^2]}$$

$$\Rightarrow 5 \times \sqrt{[(4 \times 13 \times 13) - (20 \times 20)]}$$

$$\Rightarrow 5 \times \sqrt{(676 - 400)} = 5 \times \sqrt{276} = 5 \times 16.6$$

$$=83.06 \text{ cm}^2$$

Answer10: Let $\triangle PQR$ be an isosceles triangle and $PX \perp QR$.

$$\text{Area of triangle} = 360 \text{ cm}^2 \Rightarrow \frac{1}{2} \times QR \times PX = 360 \Rightarrow h = 9 \text{ cm}$$

$$\text{Now, } QX = \frac{1}{2} \times 80 = 40 \text{ cm and } PX = 9 \text{ cm}$$

Also,

$$PQ = \sqrt{(QX^2 + PX^2)} = \sqrt{(40^2 + 9^2)}$$

$$\Rightarrow \sqrt{[(40 \times 40) + (9 \times 9)]}$$

$$\Rightarrow \sqrt{(1600 + 81)} = \sqrt{1681} = 41 \text{ cm}$$

$$\therefore \text{Perimeter} = 80 + 41 + 41 = 162 \text{ cm}$$

Answer11: The ratio of the equal side to its base is 3 : 2.

$$\Rightarrow \text{Ratio of sides} = 3 : 3 : 2.$$

Let the three sides of triangle be $3y, 3y, 2y$.

The perimeter of isosceles triangle = 32 cm.

$$\Rightarrow 3y + 3y + 2y = 32 \text{ cm}$$

$$\Rightarrow 8y = 32$$

$$\Rightarrow y = \frac{32}{8}$$

$$\Rightarrow y = 4 \text{ cm}$$

Therefore, the three side of triangle are $3y$, $3y$, $2y = 12 \text{ cm}$, 12 cm , 8 cm .

Let S be the semi-perimeter of the triangle. Then,

$$S = \frac{1}{2}(12+12+8)$$

$$\Rightarrow s = \frac{1}{2} \times 32$$

$$\Rightarrow s = 16$$

Area of the triangle will be

$$= \sqrt{[S(S-a)(S-b)(S-c)]}$$

$$= \sqrt{[16(16-12)(16-12)(16-8)]}$$

$$= \sqrt{(16 \times 4 \times 4 \times 8)}$$

$$\Rightarrow 4 \times 4 \times 2\sqrt{2} = 32\sqrt{2} \text{ cm}^2$$

Answer12: Let ABC be any triangle with perimeter 50 cm .

Let the smallest side of the triangle be z .

Then the other sides be $z + 4$ and $2z - 6$.

Now,

$$z + z + 4 + 2z - 6 = 50$$

$$\Rightarrow 4z - 2 = 50$$

$$\Rightarrow 4z = 50 + 2$$

$$\Rightarrow 4z = 52$$

$$\Rightarrow z = 13$$

\therefore The sides of the triangle are of length 13 cm , 17 cm and 20 cm .

\therefore Semi-perimeter of the triangle is

$$s = (13+17+20)/2 = 25 \text{ cm}$$

\therefore By Heron's formula,

$$\text{Area of } \triangle ABC = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[25(25-13)(25-17)(25-20)]}$$

$$=\sqrt{[25(12)(8)(5)]}$$

$$=\sqrt{5 \times 5 \times 3 \times 4 \times 4 \times 2 \times 5}$$

$$=20\sqrt{30} \text{ cm}^2$$

Hence, the area of the triangle is $20\sqrt{30} \text{ cm}^2$

Answer13: The sides of the triangle are of length 13 m, 14 m and 15 m.

\therefore Semi-perimeter of the triangle is

$$s=(13+14+15)/2=21 \text{ m}$$

\therefore By Heron's formula,

$$\text{Area of } \Delta=\sqrt{[s(s-a)(s-b)(s-c)]}$$

$$=\sqrt{[21(21-13)(21-14)(21-15)]}$$

$$=\sqrt{[21(8)(7)(6)]}$$

$$=\sqrt{7 \times 3 \times 4 \times 2 \times 7 \times 3 \times 2}$$

$$=84 \text{ m}^2$$

Now,

The rent of advertisements per m^2 per year = Rs 2000

The rent of the wall with area 84 m^2 per year = Rs 2000×84
 $= \text{Rs } 168000$

The rent of the wall with area 84 m^2 for 6 months = Rs $\frac{168000}{2}$
 $= \text{Rs } 84000$

Hence, the rent paid by the company is Rs 84000.

Answer14: Let the equal sides of the isosceles triangle be a cm each.

\therefore Base of the triangle, $b = 32a$ cm

(i) Perimeter = 42 cm

$$\text{or, } a + a + 32a = 42$$

$$a=12$$

So, equal sides of the triangle are 12 cm each.

$$\text{Base} = \frac{3}{2}a = \frac{3}{2} \times 12 = 18 \text{ cm}$$

$$\text{(ii) Area of isosceles triangle} = \frac{b}{4} \sqrt{(4a^2 - b^2)} = \frac{18}{4} \times \sqrt{[4(12)^2 - 18^2]}$$

$$= 4.5 \sqrt{(4 \times 144 - 324)}$$

$$= 4.5 \sqrt{(576 - 324)}$$

$$= 4.5 \times \sqrt{252}$$

$$= 4.5 \times 15.87$$

$$= 71.42 \text{ cm}^2$$

$$\text{(iii) Area of triangle} = 71.42 \text{ cm}^2$$

$$\Rightarrow \frac{1}{2} \times \text{Base} \times \text{Height} = 71.42$$

$$\Rightarrow \text{Height} = 7.94 \text{ cm}$$

Answer 15:

Area of equilateral triangle is $36\sqrt{3}$ is given.

$$\text{Area of equilateral triangle} = \frac{\sqrt{3}}{4} \times (\text{Side})^2$$

$$\Rightarrow \frac{\sqrt{3}}{4} \times (\text{Side})^2 = 36\sqrt{3}$$

$$\Rightarrow (\text{Side})^2 = 36\sqrt{3} \times \frac{4}{\sqrt{3}} = 36 \times 4 = 72$$

$$\Rightarrow \text{Side} = 12 \text{ cm}$$

Thus, we have:

$$\text{Perimeter} = 3 \times \text{Side}$$

$$\Rightarrow 3 \times 12 = 36 \text{ cm}$$

Answer16: Area of equilateral triangle $= \frac{\sqrt{3}}{4} \times (\text{Side})^2$

$$\Rightarrow \frac{\sqrt{3}}{4} \times (\text{Side})^2 = 81\sqrt{3}$$

$$\Rightarrow (\text{side}^2) = 81\sqrt{3} \times \frac{4}{\sqrt{3}}$$

$$\Rightarrow (\text{Side})^2 = 324$$

$$\Rightarrow \text{Side} = 18 \text{ cm}$$

Now, we have:

$$\text{Height} = \frac{\sqrt{3}}{2} \times \text{side} = \frac{\sqrt{3}}{2} \times 18 = 9\sqrt{3} \text{ cm.}$$

Answer17: Side of the equilateral triangle = 8 cm

$$(i) \text{Area of equilateral triangle} = \frac{\sqrt{3}}{4} \times (\text{Side})^2 = \frac{\sqrt{3}}{4} \times (8)^2 = \frac{\sqrt{3}}{4} \times 64 = 27.71 \text{ cm}^2$$

$$(ii) \text{Height} = \frac{\sqrt{3}}{2} \times \text{Side} = \frac{\sqrt{3}}{2} \times 8 = 6.93 \text{ cm}$$

Answer18: Height of the equilateral triangle = 9 cm

Thus, we have:

$$\text{Height} = \frac{\sqrt{3}}{2} \times \text{Side}$$

$$\Rightarrow 9 = \frac{\sqrt{3}}{2} \times \text{Side}$$

$$\Rightarrow \text{Side} = \frac{9 \times 2}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 18 \times \frac{\sqrt{3}}{3} = 6\sqrt{3} \text{ cm}$$

Also,

$$\text{Area of equilateral triangle} = \frac{\sqrt{3}}{4} \times (\text{Side})^2 = \frac{\sqrt{3}}{4} \times (6\sqrt{3})^2$$

$$\Rightarrow \frac{\sqrt{3}}{4} \times 36 \times 3$$

$$\Rightarrow 27\sqrt{3} = 46.76 \text{ cm}^2$$

Answer19: Let $\triangle PQR$ be a right-angled triangle and $PQ \perp QR$.

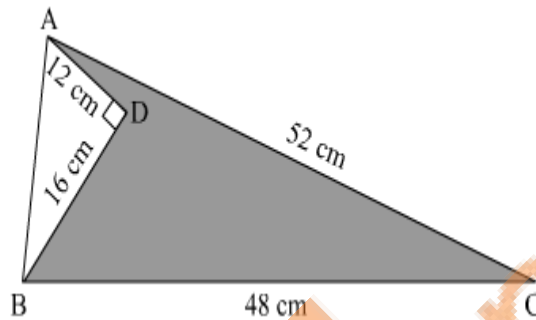
Now,

$$PQ = \sqrt{(PR^2 - QR^2)} = \sqrt{(50^2 - 48^2)} = \sqrt{(2500 - 2304)}$$

$$\Rightarrow \sqrt{196} = \sqrt{14} \times 14 = 14 \text{ cm}$$

$$\text{Area of triangle} = \frac{1}{2} \times QR \times PQ = \frac{1}{2} \times 48 \times 14 = 336 \text{ cm}^2$$

Answer 20:



In right angled $\triangle ABD$,

$$AB^2 = AD^2 + DB^2$$

$$\Rightarrow AB^2 = 12^2 + 16^2$$

$$\Rightarrow AB^2 = 144 + 256$$

$$\Rightarrow AB^2 = 400$$

$$\Rightarrow AB = \sqrt{400}$$

$$\Rightarrow AB = 20 \text{ cm}$$

$$\begin{aligned} \text{Area of } \triangle ADB &= \frac{1}{2} \times DB \times AD \\ &= \frac{1}{2} \times 16 \times 12 = 16 \times 6 \\ &= 96 \text{ cm}^2 \quad \dots(1) \end{aligned}$$

In $\triangle ACB$,

The sides of the triangle are of length 20 cm, 52 cm and 48 cm.

\therefore Semi-perimeter of the triangle is

$$s = \frac{(20+52+48)}{2} = \frac{120}{2} = 60 \text{ cm}$$

∴ By Heron's formula,

$$\text{Area of } \triangle ACB = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[60(60-20)(60-52)(60-48)]}$$

$$= \sqrt{[60(40)(8)(12)]}$$

$$= \sqrt{6 \times 10 \times 4 \times 10 \times 4 \times 2 \times 6 \times 2}$$

$$= 480 \text{ cm}^2 \quad \dots(2)$$

Now,

$$\text{Area of the shaded region} = \text{Area of } \triangle ACB - \text{Area of } \triangle ADB$$

$$= 480 - 96$$

$$= 384 \text{ cm}^2$$

Hence, the area of the shaded region in the given figure is 384 cm^2 .

Answer 21 : In right angled $\triangle ABC$, by Pythagoras theorem

$$AC^2 = AB^2 + BC^2$$

$$\Rightarrow AC^2 = 6^2 + 8^2$$

$$\Rightarrow AC^2 = 36 + 64$$

$$\Rightarrow AC^2 = 100$$

$$\Rightarrow AC = \sqrt{100}$$

$$\Rightarrow AC = 10 \text{ cm}$$

$$\text{Area of } \triangle ABC = \frac{1}{2} \times AB \times BC$$

$$= \frac{1}{2} \times 6 \times 8$$

$$= 24 \text{ cm}^2 \quad \dots(1)$$

In $\triangle ACD$,

The sides of the triangle are of length 10 cm, 12 cm and 14 cm.

∴ Semi-perimeter of the triangle is

$$s = \frac{(10+12+14)}{2} = 18 \text{ cm}$$

∴ By Heron's formula,

$$\text{Area of } \triangle ACD = \sqrt{[s(s-a)(s-b)(s-c)]} = \sqrt{[18(18-10)(18-12)(18-14)]}$$

$$= \sqrt{[18(8)(6)(4)]}$$

$$= \sqrt{9 \times 2 \times 4 \times 2 \times 6 \times 4}$$

$$= 24\sqrt{6} \text{ cm}^2$$

$$= 24(2.45) \text{ cm}^2$$

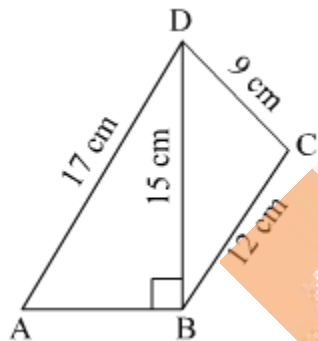
$$= 58.8 \text{ cm}^2 \quad \dots(2)$$

Thus,

$$\begin{aligned} \text{Area of quadrilateral } ABCD &= \text{Area of } \triangle ABC + \text{Area of } \triangle ACD \\ &= (24 + 58.8) \text{ cm}^2 \\ &= 82.8 \text{ cm}^2 \end{aligned}$$

Hence, the area of quadrilateral $ABCD$ is 82.8 cm^2 .

Answer 22



We know that $\triangle ABD$ is a right-angled triangle.

By Pythagoras theorem

$$\therefore AB^2 = \sqrt{(AD^2 - DB^2)} = \sqrt{(17^2 - 15^2)} = \sqrt{(289 - 225)} = \sqrt{64} = 8 \text{ cm}$$

$$\text{Now, Area of triangle } ABD = \frac{1}{2} \times \text{Base} \times \text{Height}$$

$$\Rightarrow \frac{1}{2} \times AB \times BD = \frac{1}{2} \times 8 \times 15 = 60 \text{ cm}^2$$

Let, $a = 9 \text{ cm}$, $b = 15 \text{ cm}$ and $c = 12 \text{ cm}$

$$S = 18 \text{ cm}$$

By Heron's formula,

$$\text{Area of triangle } DBC = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[18(18-9)(18-15)(18-12)]}$$

$$= \sqrt{[(8 \times 9 \times 3 \times 6)]}$$

$$= \sqrt{(6 \times 3 \times 3 \times 3 \times 6)}$$

$$= 6 \times 3 \times 3$$

$$= 54 \text{ cm}^2$$

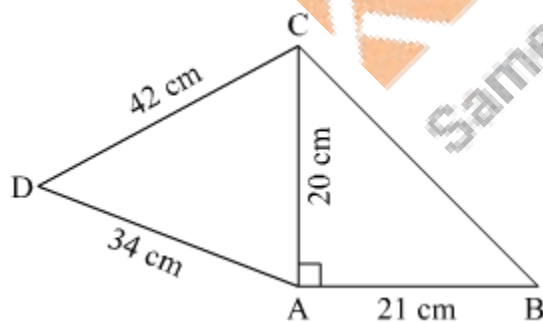
Now,

$$\begin{aligned} \text{Area of quadrilateral } ABCD &= \text{Area of } \triangle ABD + \text{Area of } \triangle BCD \\ &= (60 + 54) \text{ cm}^2 = 114 \text{ cm}^2 \end{aligned}$$

And,

$$\text{Perimeter of quadrilateral } ABCD = AB + BC + CD + AD = 17 + 8 + 12 + 9 = 46 \text{ cm}$$

Answer 23



In right angled $\triangle ABC$,
 $BC^2 = AB^2 + AC^2$

$$\begin{aligned}\Rightarrow BC^2 &= 21^2 + 20^2 \\ \Rightarrow BC^2 &= 441 + 400 \\ \Rightarrow BC^2 &= 841\end{aligned}$$

$$\begin{aligned}\Rightarrow BC &= \sqrt{841} \\ \Rightarrow BC &= 29 \text{ cm}\end{aligned}$$

$$\begin{aligned}\text{Area of } \triangle ABC &= \frac{1}{2} \times AB \times AC \\ &= \frac{1}{2} \times 21 \times 20 \\ &= 210 \text{ cm}^2 \quad \dots(1)\end{aligned}$$

In $\triangle ACD$, The sides of the triangle are of length 20 cm, 34 cm and 42 cm.

\therefore Semi-perimeter of the triangle is

$$s = \frac{20+34+42}{2} = 48 \text{ cm}$$

\therefore By Heron's formula,

Area of $\triangle ACD$

$$\begin{aligned}&= \sqrt{[s(s-a)(s-b)(s-c)]} \\ &= \sqrt{[48(48-20)(48-34)(48-42)]} \\ &= \sqrt{[48(28)(14)(6)]} \\ &= \sqrt{6} \times 4 \times 2 \times 7 \times 4 \times 7 \times 2 \times 6 \\ &= 336 \text{ cm}^2 \quad \dots(2)\end{aligned}$$

Thus,

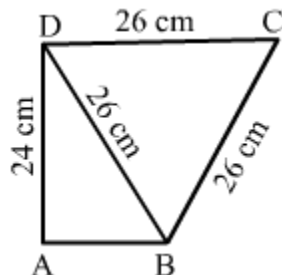
$$\begin{aligned}\text{Area of quadrilateral } ABCD &= \text{Area of } \triangle ABC + \text{Area of } \triangle ACD \\ &= (210 + 336) \text{ cm}^2 \\ &= 546 \text{ cm}^2\end{aligned}$$

Also,

$$\begin{aligned}\text{Perimeter of quadrilateral } ABCD &= (34 + 42 + 29 + 21) \text{ cm} \\ &= 126 \text{ cm}\end{aligned}$$

Hence, the perimeter and area of quadrilateral $ABCD$ is 126 cm and 546 cm², respectively.

Answer 24:



We know that $\triangle BAD$ is a right-angled triangle.

$$\therefore AB = \sqrt{(BD^2 - AD^2)} = \sqrt{(26^2 - 24^2)}$$

$$\Rightarrow \sqrt{(676 - 576)} = \sqrt{100} = 10 \text{ cm}$$

$$\text{Now, Area of triangle } BAD = \frac{1}{2} \times \text{Base} \times \text{Height} = \frac{1}{2} \times AB \times AD = \frac{1}{2} \times 10 \times 24 = 120 \text{ cm}^2$$

Also, we know that $\triangle BDC$ is an equilateral triangle.

$$\therefore \text{Area of equilateral triangle} = \frac{\sqrt{3}}{4} \times (\text{Side})^2 = \frac{\sqrt{3}}{4} \times (26)^2 = \frac{\sqrt{3}}{4} \times 676$$

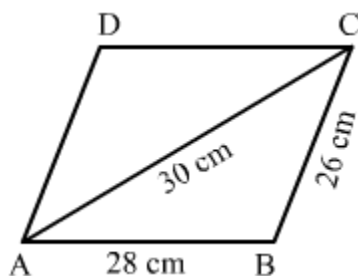
$$\Rightarrow 169\sqrt{3} = 292.37 \text{ cm}^2$$

Now,

$$\begin{aligned} \text{Area of quadrilateral } ABCD &= \text{Area of } \triangle ABD + \text{Area of } \triangle BDC \\ &= (120 + 292.37) \text{ cm}^2 = 412.37 \text{ cm}^2 \end{aligned}$$

$$\text{Perimeter of } ABCD = AB + BC + CD + DA = 10 + 26 + 26 + 24 = 86 \text{ cm}$$

Answer 25:



Let, $a=26$ cm, $b=30$ cm and $c=28$ cm

$$\Rightarrow s = \frac{(a+b+c)}{2} = \frac{(30+26+28)}{2} = 42\text{cm}$$

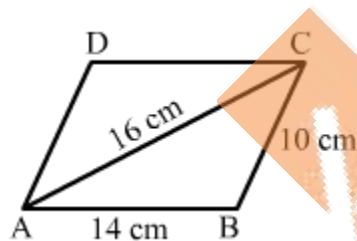
By Heron's formula,

$$\begin{aligned}\text{Area of triangle } ABC &= \sqrt{[s(s-a)(s-b)(s-c)]} \\ &= \sqrt{[42(42-26)(42-30)(42-28)]} \\ &= \sqrt{(42 \times 16 \times 12 \times 14)} \\ &= \sqrt{(14 \times 3 \times 4 \times 4 \times 2 \times 2 \times 3 \times 14)} \\ &= \sqrt{(14 \times 4 \times 2 \times 3)} = 336 \text{ cm}^2\end{aligned}$$

We know that a diagonal divides a parallelogram into two triangles of equal areas.

$$\therefore \text{Area of parallelogram } ABCD = 2(\text{Area of triangle } ABC) = 2 \times 336 = 672 \text{ cm}^2$$

Answer 26



Let, $a=10$ cm, $b=16$ cm and $c=14$ cm

$$s = \frac{(a+b+c)}{2} = \frac{(10+16+14)}{2} = \frac{40}{2} = 20\text{cm}$$

By Heron's formula,

$$\begin{aligned}\text{Area of triangle } ABC &= \sqrt{[s(s-a)(s-b)(s-c)]} \\ &= \sqrt{20(20-10)(20-16)(20-14)} \\ &= \sqrt{20 \times 10 \times 4 \times 6}\end{aligned}$$

$$=\sqrt{(10 \times 2 \times 10 \times 2 \times 2 \times 3 \times 2)}$$

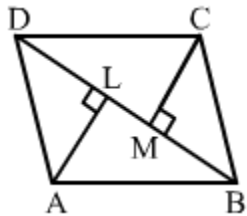
$$= 10 \times 2 \times 2 \times \sqrt{3}$$

$$=69.2 \text{ cm}^2$$

We know that a diagonal divides a parallelogram into two triangles of equal areas.

$$\therefore \text{Area of parallelogram } ABCD = 2(\text{Area of triangle } ABC) = 2 \times 69.2 \text{ cm}^2 = 138.4 \text{ cm}^2$$

Answer 27:



Area of $ABCD = \text{Area of } \triangle ABD + \text{Area of } \triangle BDC$

$$= \frac{1}{2} \times BD \times AL + \frac{1}{2} \times BD \times CM$$

$$= \frac{1}{2} \times BD (AL + CM)$$

$$= \frac{1}{2} \times 64 (16.8 + 13.2)$$

$$= 32 \times 30$$

$$= 960 \text{ cm}^2$$

Answer 28: Let the length of CD be y .

Then, the length of AB be $y + 4$.

Area of trapezium $= \frac{1}{2} \times \text{sum of parallel sides} \times \text{height}$

$$\Rightarrow 475 = \frac{1}{2} \times (y + y + 4) \times 19$$

$$\Rightarrow 475 \times 2 = 19(2y + 4)$$

$$\Rightarrow 950 = 38y + 76$$

$$\Rightarrow 38y = 950 - 76$$

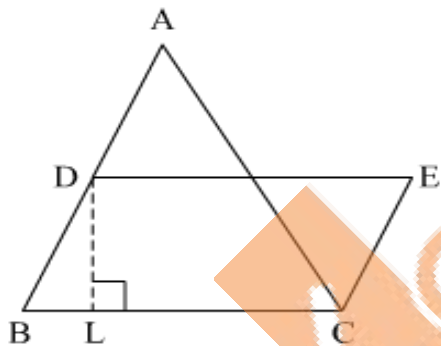
$$\Rightarrow 38x = 874$$

$$\Rightarrow y = \frac{874}{38}$$

$$\Rightarrow x = 23$$

\therefore The length of CD is 23 cm and the length of AB is 27 cm.
Hence, the lengths of two parallel sides is 23 cm and 27

Answer 29:



In $\triangle ABC$,

The sides of the triangle are of length 7.5 cm, 6.5 cm and 7 cm.

\therefore Semi-perimeter of the triangle is

$$s = (7.5 + 6.5 + 7)/2 = 10.5 \text{ cm}$$

\therefore By Heron's formula,

$$\text{Area of } \triangle ABC = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[10.5(10.5 - 7.5)(10.5 - 6.5)(10.5 - 7)]}$$

$$= \sqrt{[10.5(3)(4)(3.5)]}$$

$$= \sqrt{441}$$

$$= 21 \text{ cm}^2 \quad \dots(2)$$

Now,

$$\begin{aligned}\text{Area of parallelogram } DBCE &= \text{Area of } \triangle ABC \\ &= 21 \text{ cm}^2\end{aligned}$$

Also,

$$\begin{aligned}\text{Area of parallelogram } DBCE &= \text{base} \times \text{height} \\ \Rightarrow 21 &= BC \times DL\end{aligned}$$

$$\Rightarrow 21 = 7 \times DL$$

$$\Rightarrow DL = \frac{21}{7} = 3 \text{ cm}$$

Hence, the height DL of the parallelogram is 3 cm.

Answer 30: In right angled $\triangle ADE$,
 $AD^2 = AE^2 + ED^2$

$$\Rightarrow 100^2 = (90 - 30)^2 + ED^2$$

$$\Rightarrow 10000 = 3600 + ED^2$$

$$\Rightarrow ED^2 = 10000 - 3600$$

$$\Rightarrow ED^2 = 6400$$

$$\Rightarrow ED = \sqrt{6400} = 80 \text{ m}$$

Thus, the height of the trapezium = 80 m ... (1)

Now,

$$\begin{aligned}\text{Area of trapezium} &= \frac{1}{2} \times \text{sum of parallel sides} \times \text{height} \\ &= \frac{1}{2} \times (90 + 30) \times 80\end{aligned}$$

$$\begin{aligned}&= \frac{1}{2} \times 120 \times 80 = 60 \times 80 \\ &= 4800 \text{ m}^2\end{aligned}$$

The cost to plough per m^2 = Rs 5

$$\begin{aligned}\text{The cost to plough } 4800 \text{ m}^2 &= \text{Rs } 5 \times 4800 \\ &= \text{Rs } 24000\end{aligned}$$

Hence, the total cost of ploughing the field is Rs 24000.

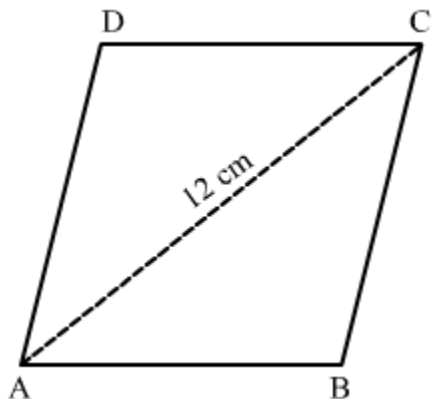
Answer 31 : Let $ABCD$ be a rectangular plot is given for constructing a house, having a measurement of 40 m long and 15 m in the front.

According to the laws, the length of the inner rectangle = $40 - 3 - 3 = 34$ m and the breath of the inner rectangle = $15 - 2 - 2 = 11$ m.

$$\begin{aligned}\therefore \text{Area of the inner rectangle } PQRS &= \text{Length} \times \text{Breath} \\ &= 34 \times 11 \\ &= 374 \text{ m}^2\end{aligned}$$

Hence, the largest area where house can be constructed is 374 m^2 .

Answer 32: Let the sides of rhombus be of length x cm.



Perimeter of rhombus = $4x$

$$\Rightarrow 40 = 4x$$

$$\Rightarrow x = 10 \text{ cm}$$

Now,

In $\triangle ABC$,

The sides of the triangle are of length 10 cm, 10 cm and 12 cm.

\therefore Semi-perimeter of the triangle is

$$s = (10 + 10 + 12) / 2 = 16 \text{ cm}$$

\therefore By Heron's formula,

$$\text{Area of } \triangle ABC = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[16(16-10)(16-10)(16-12)]}$$

$$= \sqrt{[16(6)(6)(4)]}$$

$$= \sqrt{4 \times 4 \times 6 \times 6 \times 2 \times 2}$$

$$= 48 \text{ cm}^2 \quad \dots(1)$$

In $\triangle ADC$, The sides of the triangle are of length 10 cm, 10 cm and 12 cm.

\therefore Semi-perimeter of the triangle is

$$s = (10 + 10 + 12) / 2 = 16 \text{ cm}$$

\therefore By Heron's formula,

$$\text{Area of } \triangle ADC = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[16(16-10)(16-10)(16-12)]}$$

$$= \sqrt{[16(6)(6)(4)]}$$

$$= \sqrt{2304}$$

$$= 48 \text{ cm}^2 \quad \dots(2)$$

\therefore Area of the rhombus = Area of $\triangle ABC$ + Area of $\triangle ADC$

$$= 48 + 48$$

$$= 96 \text{ cm}^2$$

The cost to paint per cm^2 = Rs 5

The cost to paint 96 cm^2 = Rs 5×96

$$= \text{Rs } 480$$

The cost to paint both sides of the sheet = Rs 2×480

$$= \text{Rs } 960$$

Hence, the total cost of painting is Rs 960.

Answer33: Let the semi-perimeter of the triangle be s .

Let the sides of the triangle be a , b and c .

Given: $s - a = 8$, $s - b = 7$ and $s - c = 5 \quad \dots(1)$

Adding all three equations

$$3s - (a + b + c) = 8 + 7 + 5$$

$$\Rightarrow 3s - (a + b + c) = 20$$

$$\Rightarrow 3s - 2s = 20$$

$$\Rightarrow s = 20 \text{ cm} \quad \dots(2)$$

\therefore By Heron's formula,

$$\text{Area of } \triangle = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[20(8)(7)(5)]}$$

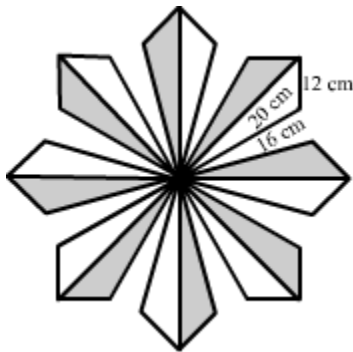
$$= \sqrt{2 \times 5 \times 2 \times 2 \times 2 \times 2 \times 7 \times 5}$$

$$= 20\sqrt{14} \text{ cm}^2$$

Hence, the area of the triangle is $20\sqrt{14} \text{ cm}^2$

.

Answer34



Let, $a=16$ cm, $b=12$ cm and $c=20$ cm

$$s = (a+b+c)/2 = (16+12+20)/2 = 24 \text{ cm}$$

By Heron's formula,

$$\therefore \text{Area of triangle} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[24(24-16)(24-12)(24-20)]}$$

$$= \sqrt{(24 \times 8 \times 12 \times 4)}$$

$$= \sqrt{(6 \times 4 \times 4 \times 4 \times 4 \times 6)}$$

$$= 6 \times 4 \times 4$$

$$= 96 \text{ cm}^2$$

Now,

$$\text{Area of 16 triangular-shaped tiles} = 16 \times 96 = 1536 \text{ cm}^2$$

$$\text{Cost of polishing tiles of area } 1 \text{ cm}^2 = \text{Rs } 1$$

$$\text{Cost of polishing tiles of area } 1536 \text{ cm}^2 = 1 \times 1536 = \text{Rs } 1536$$

Answer 35



We know that the triangle is an isosceles triangle.

Thus, we can find out the area of one triangular piece of cloth.

Area of isosceles triangle $= \frac{b}{4} \sqrt{(4a^2 - b^2)}$

$$= \frac{20}{4} \times \sqrt{[4(50)^2 - 20^2]}$$

$$= 5 \times \sqrt{(10000 - 400)}$$

$$\Rightarrow 5 \times \sqrt{9600} = 5 \times 40\sqrt{6}$$

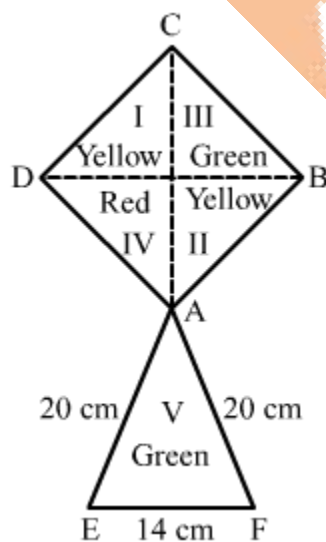
$$\Rightarrow 200\sqrt{6} = 490 \text{ cm}^2$$

Now,

Area of 1 triangular piece of cloth $= 490 \text{ cm}^2$

Area of 12 triangular pieces of cloth $= 12 \times 490 = 5880 \text{ cm}^2$

Answer 36:



In the given figure, $ABCD$ is a square with diagonal 44 cm.

$\therefore AB = BC = CD = DA.$ (1)

In right angled $\triangle ABC$,
 $AC^2 = AB^2 + BC^2$

$$\begin{aligned}\Rightarrow 44^2 &= 2AB^2 \\ \Rightarrow 1936 &= 2AB^2 \\ \Rightarrow AB^2 &= 1936/2 \\ \Rightarrow AB^2 &= 968\end{aligned}$$

$$\begin{aligned}\Rightarrow AB &= \sqrt{968} \\ \Rightarrow AB &= 22\sqrt{2} \text{ cm} \quad \dots(2) \\ \therefore \text{Sides of square } AB &= BC = CD = DA = 22\sqrt{2} \text{ cm} \\ \text{Area of square } ABCD &= (\text{side})^2 \\ &= (22\sqrt{2})^2 \\ &= 968 \text{ cm}^2 \quad \dots(3)\end{aligned}$$

$$\begin{aligned}\text{Area of red portion} &= \frac{968}{4} = 242 \text{ cm}^2 \\ \text{Area of yellow portion} &= \frac{968}{2} = 484 \text{ cm}^2 \\ \text{Area of green portion} &= \frac{968}{4} = 242 \text{ cm}^2\end{aligned}$$

Now, in $\triangle AEF$,

The sides of the triangle are of length 20 cm, 20 cm and 14 cm.

\therefore Semi-perimeter of the triangle is

$$s = (20+20+14)/2 = 27 \text{ cm}$$

\therefore By Heron's formula,

$$\text{Area of } \triangle AEF = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[27(27-20)(27-20)(27-14)]}$$

$$= \sqrt{[27(7)(7)(13)]}$$

$$= \sqrt{2139}$$

$$= 131.04 \text{ cm}^2 \quad \dots(4)$$

$$\text{Total area of the green portion} = 242 + 131.04 = 373.04 \text{ cm}^2$$

Hence, the paper required of each shade to make a kite is red paper 242 cm^2 , yellow paper 484 cm^2 and green paper 373.04 cm^2 .

Answer37 : Area of rectangle $ABCD = \text{Length} \times \text{Breath}$

$$= 75 \times 4$$

$$= 300 \text{ m}^2$$

Area of rectangle $PQRS = \text{Length} \times \text{Breath}$

$$= 60 \times 4$$

$$= 240 \text{ m}^2$$

$$\begin{aligned}\text{Area of square } EFGH &= (\text{side})^2 \\ &= (4)^2 \\ &= 16 \text{ m}^2\end{aligned}$$

\therefore Area of the footpath = Area of rectangle $ABCD$ + Area of rectangle $PQRS$ – Area of square $EFGH$

$$\begin{aligned}&= 300 + 240 - 16 \\ &= 524 \text{ m}^2\end{aligned}$$

The cost of gravelling the road per m^2 = Rs 50

$$\begin{aligned}\text{The cost of gravelling the roads } 524 \text{ m}^2 &= \text{Rs } 50 \times 524 \\ &= \text{Rs } 26200\end{aligned}$$

Hence, the total cost of gravelling the roads at Rs 50 per m^2 is Rs 26200.

Answer38 : Given, 10m wide at the top, and 6m wide at the bottom
Let the height of the trapezium be h .

Area of trapezium $= \frac{1}{2} \times \text{sum of parallel sides} \times \text{height}$

$$\Rightarrow 640 = \frac{1}{2} \times (10 + 6) \times h$$

$$\Rightarrow 640 = \frac{1}{2} \times 16 \times h = 8h$$

$$\Rightarrow h = \frac{640}{8} = 80 \text{ m}$$

Hence, the depth of the canal is 80 m.

Answer39: In $\triangle BCE$, The sides of the triangle are of length 15 m, 13 m and 14 m.

\therefore Semi-perimeter of the triangle is

$$s = (15+13+14)/2 = 21 \text{ m}$$

\therefore By Heron's formula,

$$\text{Area of } \triangle BCE = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[21(21-15)(21-13)(21-14)]}$$

$$= \sqrt{[21(6)(8)(7)]}$$

$$= \sqrt{7} \times 3 \times 3 \times 2 \times 2 \times 2 \times 2 \times 7$$

$$= 84 \text{ m}^2 \quad \dots(1)$$

Also,

$$\text{Area of } \triangle BCE = \frac{1}{2} \times \text{Base} \times \text{Height}$$

$$\Rightarrow 84 = \frac{1}{2} \times 14 \times \text{Height}$$

$$\Rightarrow 84 = 7 \times \text{Height}$$

$$\Rightarrow \text{Height} = \frac{84}{7}$$

$$\Rightarrow \text{Height} = 12 \text{ m}$$

$$\therefore \text{Height of } \triangle BCE = \text{Height of the parallelogram } ABED = 12 \text{ m}$$

Now,

$$\text{Area of the parallelogram } ABED = \text{Base} \times \text{Height}$$

$$= 11 \times 12$$

$$= 132 \text{ m}^2$$

...(2)

$$\therefore \text{Area of the trapezium} = \text{Area of the parallelogram } ABED + \text{Area of the triangle } BCE$$

$$= 132 + 84$$

$$= 216 \text{ m}^2$$

Hence, the area of a trapezium is 216 m^2 .

Answer40 : Let the length of the parallel sides be l and $l - 8$.

The height of the trapezium = 24 cm

Area of trapezium = $\frac{1}{2} \times \text{sum of parallel sides} \times \text{height}$

$$\Rightarrow 312 = \frac{1}{2} \times (l + l - 8) \times 24$$

$$\Rightarrow 312 = 12(2l - 8)$$

$$\Rightarrow 2l - 8 = 312/12$$

$$\Rightarrow 2l - 8 = 26$$

$$\Rightarrow 2l = 26 + 8$$

$$\Rightarrow 2l = 34$$

$$\Rightarrow l = \frac{34}{2}$$

$$\Rightarrow l = 17 \text{ cm}$$

Hence, the lengths of the parallel sides are 17 cm and 9 cm .

Answer41: Diagonals d_1 and d_2 of the rhombus measure 120 m and 44 m , respectively.

Base of the parallelogram = 66 m

Now,

Area of the rhombus = Area of the parallelogram

$$\Rightarrow \frac{1}{2} \times d_1 \times d_2 = \text{Base} \times \text{Height}$$

$$\Rightarrow \frac{1}{2} \times 120 \times 44 = 66 \times \text{Height}$$

$$\Rightarrow 60 \times 44 = 66 \times \text{Height}$$

$$\Rightarrow \text{Height} = \frac{60 \times 44}{66} = \frac{2640}{66}$$

$$\Rightarrow \text{Height} = 40 \text{ m}$$

Hence, the measure of the altitude of the parallelogram is 40 m.

Answer42 : It is given that,

Sides of the square = 40 m

Altitude of the parallelogram = 25 m

Now,

Area of the parallelogram = Area of the square

$$\Rightarrow \text{Base} \times \text{Height} = (\text{side})^2$$

$$\Rightarrow \text{Base} \times 25 = (40)^2$$

$$\Rightarrow \text{Base} \times 25 = 1600$$

$$\Rightarrow \text{Base} = \frac{1600}{25}$$

$$\Rightarrow \text{Base} = 64 \text{ m}$$

Hence, the length of the corresponding base of the parallelogram is 64 m.

Answer43: It is given that,

The sides of rhombus = 20 cm.

One of the diagonal = 24 cm.

In $\triangle ABC$,

The sides of the triangle are of length 20 cm, 20 cm and 24 cm.

\therefore Semi-perimeter of the triangle is

$$s = (20 + 20 + 24) / 2$$

$$\Rightarrow 64 / 2 = 32 \text{ cm}$$

\therefore By Heron's formula,

$$\text{Area of } \triangle ACD = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[32(32-20)(32-20)(32-24)]}$$

$$= \sqrt{[32(12)(12)(8)]}$$

$$= 192 \text{ cm}^2 \quad \dots(1)$$

In $\triangle ACD$,

The sides of the triangle are of length 20 cm, 20 cm and 24 cm.

\therefore Semi-perimeter of the triangle is

$$s = (20+20+24)/2 = 64/2 = 32 \text{ cm}$$

\therefore By Heron's formula,

$$\text{Area of } \triangle ACD = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[32(32-20)(32-20)(32-24)]}$$

$$= \sqrt{[32(12)(12)(8)]}$$

$$= 12 \times 8 \times 2$$

$$= 192 \text{ cm}^2 \quad \dots(2)$$

\therefore Area of the rhombus = Area of $\triangle ABC$ + Area of $\triangle ACD$

$$= 192 + 192$$

$$= 384 \text{ cm}^2$$

Hence, the area of a rhombus is 384 cm^2 .

Answer44 : It is given that,

Area of rhombus = 480 cm^2 .

One of the diagonal = 48 cm.

$$(i) \text{ Area of the rhombus} = \frac{1}{2} \times d_1 \times d_2$$

$$\Rightarrow 480 = \frac{1}{2} \times 48 \times d_2$$

$$\Rightarrow 480 = 24 \times d_2$$

$$\Rightarrow d_2 = \frac{480}{24} = \frac{6 \times 8 \times 10}{6 \times 4}$$

$$\Rightarrow d_2 = 20 \text{ cm}$$

Hence, the length of the other diagonal is 20 cm.

(ii) We know that the diagonals of the rhombus bisect each other at right angles.

In right angled $\triangle ABO$,

$$AB^2 = AO^2 + OB^2$$

$$\Rightarrow AB^2 = 24^2 + 10^2$$

$$\Rightarrow AB^2 = 576 + 100$$

$$\Rightarrow AB^2 = 676$$

$$\Rightarrow AB = \sqrt{676}$$

$$\Rightarrow AB = 26 \text{ cm}$$

Hence, the length of each of the sides of the rhombus is 26 cm.

(iii) Perimeter of the rhombus = $4 \times \text{side}$

$$= 4 \times 26$$

$$= 104 \text{ cm}$$

Hence, the perimeter of the rhombus is 104 cm.

MULTIPLE-CHOICE QUESTIONS

Answer1: (b) 30 cm^2

Area of triangle = $\frac{1}{2} \times \text{Base} \times \text{Height}$

$$\text{Area of } \triangle ABC = \frac{1}{2} \times 12 \times 5 = 30 \text{ cm}^2$$

Answer2: (a) 96 cm^2

Let, $a=20 \text{ cm}$, $b=16 \text{ cm}$ and $c=12 \text{ cm}$

$$s = (a+b+c)/2 = (20+16+12)/2 = 24 \text{ cm}$$

By Heron's formula, we have:

$$\text{Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{24(24-20)(24-16)(24-12)}$$

$$= \sqrt{24 \times 4 \times 8 \times 12}$$

$$= \sqrt{6 \times 4 \times 4 \times 4 \times 6}$$

$$= 6 \times 4 \times 4$$

$$= 96 \text{ cm}^2$$

Answer3: (b) $16\sqrt{3} \text{ cm}^2$

$$\text{Area of equilateral triangle} = \frac{\sqrt{3}}{4} (\text{Side})^2 = \frac{\sqrt{3}}{4} (8)^2 = \frac{\sqrt{3}}{4} (64) = 16\sqrt{3} \text{ cm}^2$$

Answer4: (b) $8\sqrt{5} \text{ cm}^2$

$$\text{Area of isosceles triangle} = \frac{b}{4} \times \sqrt{4a^2 - b^2}$$

$$a = 6 \text{ cm and } b = 8 \text{ cm}$$

Thus

$$= 8/4 \times \sqrt{[4(6)^2 - 8^2]}$$

$$= 8/4 \times \sqrt{(144 - 64)}$$

$$= 8/4 \times \sqrt{80}$$

$$= 8/4 \times 4\sqrt{5}$$

$$= 8\sqrt{5} \text{ cm}^2$$

Answer5: (c) 4 cm

$$\text{Height of isosceles triangle} = \frac{1}{2} \times \sqrt{(4a^2 - b^2)}$$

$$= \frac{1}{2} \times \sqrt{[4(5)^2 - 6^2]}$$

$$= \frac{1}{2} \times \sqrt{(100 - 36)}$$

$$= \frac{1}{2} \times \sqrt{64}$$

$$= \frac{1}{2} \times 8$$

$$= 4 \text{ cm}$$

Answer6: (b) 50 cm²

Here, the base and height of the triangle are 10 cm and 10 cm, respectively.

Thus,

$$\text{Area of triangle} = \frac{1}{2} \times \text{Base} \times \text{Height} = \frac{1}{2} \times 10 \times 10 = 50 \text{ cm}^2$$

Answer7: (b) $5\sqrt{3}$ cm

$$\text{Height of equilateral triangle} = \sqrt{3}/2 \times (\text{Side}) = \sqrt{3}/2 \times 10 = 5\sqrt{3} \text{ cm}$$

Answer8: (a) $12\sqrt{3}$ cm²

$$\text{Height of equilateral triangle} = \sqrt{3}/2 \times (\text{Side})$$

$$\Rightarrow 6 = \sqrt{3}/2 \times (\text{Side})$$

$$\Rightarrow \text{Side} = (12/\sqrt{3}) \times (\sqrt{3}/\sqrt{3}) = (12/3) \times \sqrt{3} = 4\sqrt{3} \text{ cm}$$

Now,

$$\text{Area of equilateral triangle} = \frac{\sqrt{3}}{4} \times (\text{Side})^2 = \frac{\sqrt{3}}{4} \times (4\sqrt{3})^2 = \frac{\sqrt{3}}{4} \times 48 = 12\sqrt{3} \text{ cm}^2$$

Answer9: (c) 384 m^2

Let, $a=40 \text{ m}$, $b = 24 \text{ m}$ and $c=32 \text{ m}$

$$s = (a+b+c)/2 = (40+24+32)/2 = 48 \text{ m}$$

By Heron's formula,

$$\text{Area of triangle} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[48(48-40)(48-24)(48-32)]}$$

$$= \sqrt{(48 \times 8 \times 24 \times 16)}$$

$$= \sqrt{(24 \times 2 \times 8 \times 24 \times 8 \times 2)}$$

$$= 24 \times 8 \times 2$$

$$= 384 \text{ m}^2$$

Answer10: (b) 750 cm^2

Let the sides of the triangle be $5x \text{ cm}$, $12x \text{ cm}$ and $13x \text{ cm}$.

Perimeter = Sum of all sides

$$\text{or, } 150 = 5x + 12x + 13x$$

$$\text{or, } 30x = 150$$

$$\text{or, } x = 5$$

Thus, the sides of the triangle are $5 \times 5 \text{ cm}$, $12 \times 5 \text{ cm}$ and $13 \times 5 \text{ cm}$, i.e., 25 cm , 60 cm and 65 cm .

Now,

Let: $a=25 \text{ cm}$, $b = 60 \text{ cm}$ and $c=65 \text{ cm}$

$$s = 150/2 = 75 \text{ cm}$$

By Heron's formula,

$$\text{Area of triangle} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$= \sqrt{[75(75-25)(75-60)(75-65)]}$$

$$= \sqrt{(75 \times 50 \times 15 \times 10)}$$

$$=\sqrt{(15 \times 5 \times 5 \times 10 \times 15 \times 10)}$$

$$=15 \times 5 \times 10$$

$$=750 \text{ cm}^2$$

Answer11:(a) 24 cm

Let, $a=30$ cm, $b = 24$ cm and $c=18$ cm

$$s = (a+b+c)/2 = (30+24+18)/2 = 36 \text{ cm}$$

On applying Heron's formula, we get

$$\text{Area of triangle} = \sqrt{[s(s-a)(s-b)(s-c)]}$$

$$=\sqrt{[36(36-30)(36-24)(36-18)]}$$

$$=\sqrt{(36 \times 6 \times 12 \times 18)}$$

$$=\sqrt{(12 \times 3 \times 12 \times 6 \times 3)}$$

$$=12 \times 3 \times 6$$

$$=216 \text{ cm}^2$$

The smallest side is 18 cm.

Hence, the altitude of the triangle corresponding to 18 cm is given by:

$$\text{Area of triangle} = 216 \text{ cm}^2$$

$$\Rightarrow \frac{1}{2} \times \text{Base} \times \text{Height} = 216$$

$$\Rightarrow \text{Height} = (216 \times 2)/18 = 24 \text{ cm}$$

Answer12:(b) 36 cm

Let $\triangle PQR$ be an isosceles triangle and $PX \perp QR$.

Now,

$$\text{Area of triangle} = 48 \text{ cm}^2$$

$$\Rightarrow \frac{1}{2} \times QR \times PX = 48$$

$$\Rightarrow h = 96/16 = 6 \text{ cm}$$

Also,

$$QX = 1/2 \times 24 = 12 \text{ cm and } PX = 12 \text{ cm}$$

$$PQ = \sqrt{(QX^2 + PX^2)}$$

$$a = \sqrt{(8^2 + 6^2)} = \sqrt{(64 + 36)} = \sqrt{100} = 10 \text{ cm}$$

$$\therefore \text{Perimeter} = (10 + 10 + 16) \text{ cm} = 36 \text{ cm}$$

Answer13: (a) 36 cm

$$\text{Area of equilateral triangle} = \frac{\sqrt{3}}{4} \times (\text{Side})^2 \Rightarrow \frac{\sqrt{3}}{4} \times (\text{Side})^2 = 36\sqrt{3}$$

$$(\text{Side})^2 = 144$$

$$\text{Side} = 12 \text{ cm}$$

Now,

$$\text{Perimeter} = 3 \times \text{Side} = 3 \times 12 = 36 \text{ cm}$$

Answer14: (c) 60 cm²

$$\text{Area of isosceles triangle} = \frac{b}{4} \times \sqrt{4(a)^2 - (b)^2} \text{ Here,}$$

$$a = 13 \text{ cm and } b = 24 \text{ cm}$$

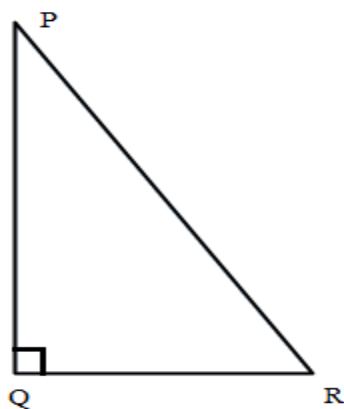
$$\text{Thus, } \frac{24}{4} \times \sqrt{4(13)^2 - 24^2}$$

$$= 6 \times \sqrt{(676 - 576)}$$

$$= 6 \times \sqrt{100}$$

$$\Rightarrow 6 \times 10 = 60 \text{ cm}^2$$

Answer15 : (c) 336 cm²



Let $\triangle PQR$ be a right-angled triangle and $PQ \perp QR$.

Now,

$$PQ = \sqrt{PR^2 - QR^2}$$

$$= \sqrt{(50^2 - 48^2)}$$

$$= \sqrt{(2500 - 2304)}$$

$$= \sqrt{196} = 14 \text{ cm}$$

$$\therefore \text{Area of triangle} = \frac{1}{2} \times QR \times PQ = \frac{1}{2} \times 48 \times 14 = 336 \text{ cm}^2$$

Answer16 : (a) $9\sqrt{3}$ cm

Area of equilateral triangle = $81\sqrt{3}$ cm²

$$\Rightarrow \frac{\sqrt{3}}{4} (\text{side})^2 = 81\sqrt{3}$$

$$\Rightarrow (\text{Side})^2 = 81 \times 4$$

$$\Rightarrow (\text{Side})^2 = 324$$

$$\Rightarrow \text{Side} = 18 \text{ cm}$$

Now,

$$\text{Height} = \frac{\sqrt{3}}{2} \times \text{Side} = \frac{\sqrt{3}}{2} \times 18 = 9\sqrt{3} \text{ cm.}$$

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