

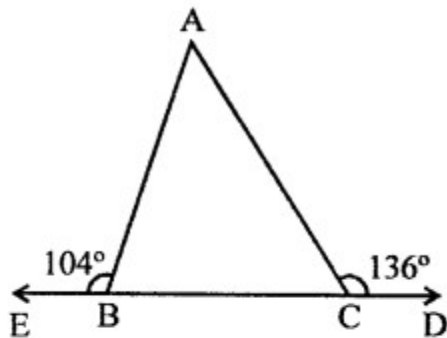
RD Sharma Solutions Class 9 Chapter 11 Coordinate Geometry Ex 11.2

Question 1.

The exterior angles obtained on producing the base of a triangle both ways are 104° and 136° . Find all the angles of the triangle.

Solution:

In $\triangle ABC$, base BC is produced both ways to D and E respectively forming $\angle ABE = 104^\circ$ and $\angle ACD = 136^\circ$



$$\therefore \angle ABC + \angle ABE = 180^\circ \quad (\text{Linear pair})$$

$$\Rightarrow \angle ABC + 104^\circ = 180^\circ$$

$$\Rightarrow \angle ABC = 180^\circ - 104^\circ$$

$$\therefore \angle ABC = 76^\circ$$

$$\text{Similarly, } \angle ACB + \angle ACD = 180^\circ$$

$$\Rightarrow \angle ACB + 136^\circ = 180^\circ$$

$$\Rightarrow \angle ACB = 180^\circ - 136^\circ = 44^\circ$$

$$\text{But } \angle ABC + \angle ACB + \angle BAC = 180^\circ$$

(Angles of a triangle)

$$\Rightarrow 76^\circ + 44^\circ + \angle BAC = 180^\circ$$

$$\Rightarrow 120^\circ + \angle BAC = 180^\circ$$

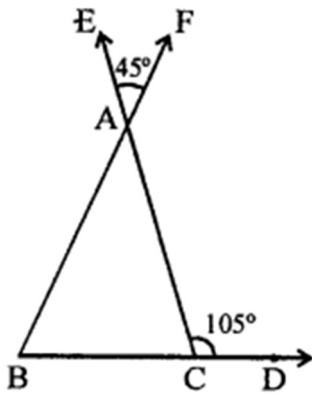
$$\Rightarrow \angle BAC = 180^\circ - 120^\circ = 60^\circ$$

Hence angles of the triangle are

$$60^\circ, 76^\circ, 44^\circ$$

Question 2.

In the figure, the sides BC , CA and AB of a $\triangle ABC$ have been produced to D , E and F respectively. If $\angle ACD = 105^\circ$ and $\angle EAF = 45^\circ$, find all the angles of the $\triangle ABC$.



Solution:

In $\triangle ABC$, sides BC, CA and BA are produced to D, E and F respectively.

$\angle ACD = 105^\circ$ and $\angle EAF = 45^\circ$

$\angle ACD + \angle ACB = 180^\circ$ (Linear pair)

$\Rightarrow 105^\circ + \angle ACB = 180^\circ$

$\Rightarrow \angle ACB = 180^\circ - 105^\circ = 75^\circ$

$\angle BAC = \angle EAF$ (Vertically opposite angles)

$= 45^\circ$

But $\angle BAC + \angle ABC + \angle ACB = 180^\circ$

$\Rightarrow 45^\circ + \angle ABC + 75^\circ = 180^\circ$

$\Rightarrow 120^\circ + \angle ABC = 180^\circ$

$\Rightarrow \angle ABC = 180^\circ - 120^\circ$

$\therefore \angle ABC = 60^\circ$

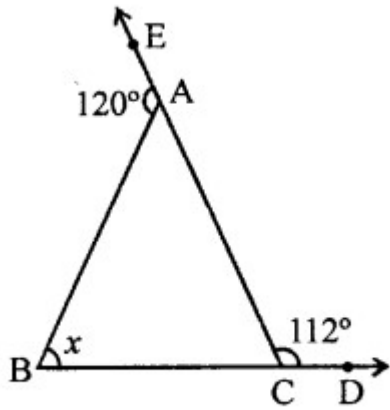
Hence $\angle ABC = 60^\circ$, $\angle BCA = 75^\circ$

and $\angle BAC = 45^\circ$

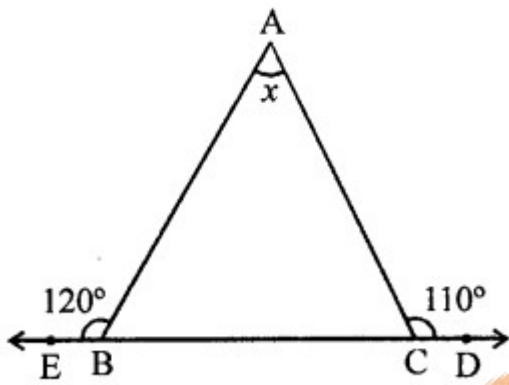
Question 3.

Compute the value of x in each of the following figures:

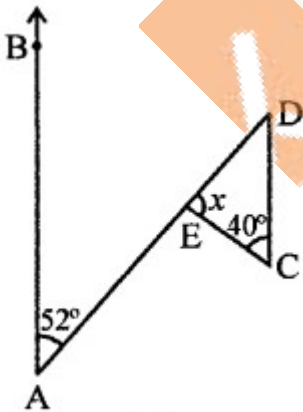
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(i)



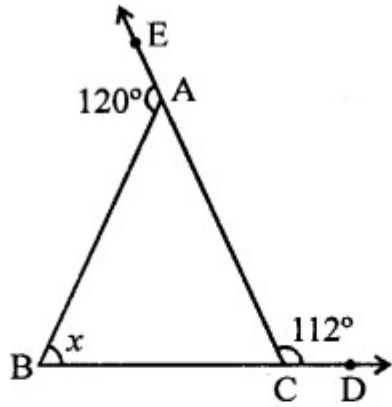
(ii)



(iii)

Solution:

(i) In $\triangle ABC$, sides BC and CA are produced to D and E respectively



$$\angle ACD = 112^\circ \text{ and } \angle BAE = 120^\circ$$

$$\angle ACB + \angle ACD = 180^\circ \quad (\text{Linear pair})$$

$$\Rightarrow \angle ACB + 112^\circ = 180^\circ$$

$$\Rightarrow \angle ACB = 180^\circ - 112^\circ = 68^\circ$$

Similarly,

$$\angle BAE + \angle BAC = 180^\circ \quad (\text{Linear pair})$$

$$\Rightarrow 120^\circ + \angle BAC = 180^\circ$$

$$\Rightarrow \angle BAC = 180^\circ - 120^\circ = 60^\circ$$

$$\text{But } \angle BAC + \angle ABC + \angle BCA = 180^\circ$$

(Angles of a triangle)

$$\Rightarrow 60^\circ + x + 68^\circ = 180^\circ$$

$$\Rightarrow 128^\circ + x = 180^\circ \Rightarrow x = 180^\circ - 128^\circ = 52^\circ$$

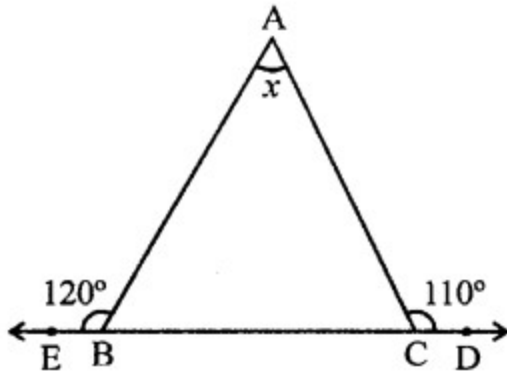
$$\therefore x = 52^\circ$$

(ii) In $\triangle ABC$, side BC is produced to either side to D and E respectively

$$\angle ABE = 120^\circ \text{ and } \angle ACD = 110^\circ$$

$$\therefore \angle ABE + \angle ABC = 180^\circ \text{ (Linear pair)}$$

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$$\Rightarrow 120^\circ + \angle ABC = 180^\circ$$

$$\Rightarrow \angle ABC = 180^\circ - 120^\circ = 60^\circ$$

Similarly,

$$\angle ACB + \angle ACD = 180^\circ \quad (\text{Linear pair})$$

$$\Rightarrow \angle ACB + 110^\circ = 180^\circ$$

$$\Rightarrow \angle ACB = 180^\circ - 110^\circ = 70^\circ$$

$$\text{But } \angle BAC + \angle ABC + \angle ACB = 180^\circ$$

(Angles of a triangle)

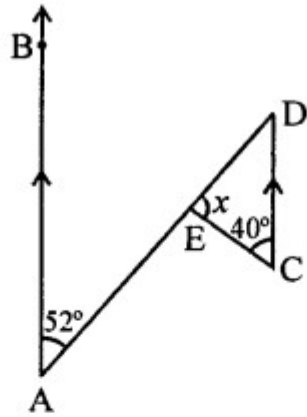
$$\Rightarrow x + 60^\circ + 70^\circ = 180^\circ$$

$$\Rightarrow x + 130^\circ = 180^\circ \Rightarrow x = 180^\circ - 130^\circ$$

$$\therefore x = 50^\circ$$

(iii) In the figure, $BA \parallel DC$

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$$\angle BAD = 52^\circ \text{ and } \angle DCE = 40^\circ$$

$\therefore BA \parallel DC$ and AD is the transversal

$$\therefore \angle ABD = \angle BDC \quad (\text{Alternate angles})$$

$$\therefore \angle ADC = 52^\circ \text{ or } \angle EDC = 52^\circ$$

Now in $\triangle DCE$,

$$\angle EDC + \angle ECD + \angle DEC = 180^\circ$$

(Angles of a triangle)

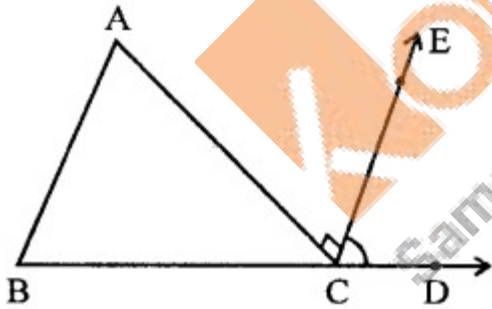
$$\Rightarrow 52^\circ + 40^\circ + x = 180^\circ$$

$$\Rightarrow 92^\circ + x = 180^\circ \Rightarrow x = 180^\circ - 92^\circ$$

$$\therefore x = 88^\circ$$

Question 4.

In the figure, $AC \perp CE$ and $\angle A : \angle B : \angle C = 3:2:1$, find the value of $\angle ECD$.



Solution:

In $\triangle ABC$, $\angle A : \angle B : \angle C = 3 : 2 : 1$

BC is produced to D and $CE \perp AC$

$\therefore \angle A + \angle B + \angle C = 180^\circ$ (Sum of angles of a triangles)

Let $\angle A = 3x$, then $\angle B = 2x$ and $\angle C = x$

$$\therefore 3x + 2x + x = 180^\circ \Rightarrow 6x = 180^\circ$$

$$\Rightarrow x = 180 \div 6 = 30^\circ$$

$$\therefore \angle A = 3x = 3 \times 30^\circ = 90^\circ$$

$$\angle B = 2x = 2 \times 30^\circ = 60^\circ$$

$$\angle C = x = 30^\circ$$

In $\triangle ABC$,

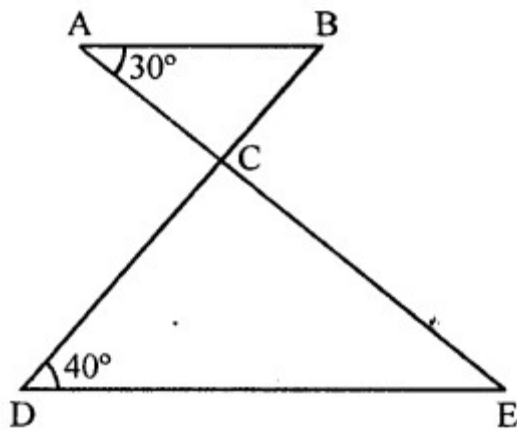
$$\text{Ext. } \angle ACD = \angle A + \angle B$$

$$\Rightarrow 90^\circ + \angle ECD = 90^\circ + 60^\circ = 150^\circ$$

$$\therefore \angle ECD = 150^\circ - 90^\circ = 60^\circ$$

Question 5.

In the figure, $AB \parallel DE$, find $\angle ACD$.



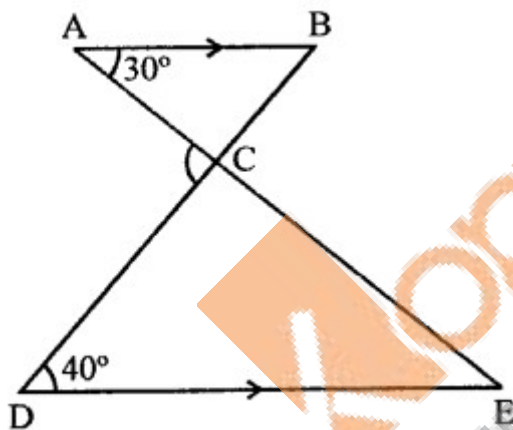
Solution:

In the figure, $AB \parallel DE$

AE and BD intersect each other at C $\angle BAC = 30^\circ$ and $\angle CDE = 40^\circ$

$\therefore AB \parallel DE$

$\therefore \angle ABC = \angle CDE$ (Alternate angles)



$$\Rightarrow \angle ABC = 40^\circ$$

In $\triangle ABC$, BC is produced

Ext. $\angle ACD = \text{Int. } \angle A + \angle B$

$$= 30^\circ + 40^\circ = 70^\circ$$

Question 6.

Which of the following statements are true (T) and which are false (F):

- (i) Sum of the three angles of a triangle is 180° .
- (ii) A triangle can have two right angles.
- (iii) All the angles of a triangle can be less than 60° .
- (iv) All the angles of a triangle can be greater than 60° .
- (v) All the angles of a triangle can be equal to 60° .
- (vi) A triangle can have two obtuse angles.
- (vii) A triangle can have at most one obtuse angles.
- (viii) If one angle of a triangle is obtuse, then it cannot be a right angled triangle.
- (ix) An exterior angle of a triangle is less than either of its interior opposite angles.

(x) An exterior angle of a triangle is equal to the sum of the two interior opposite angles.

(xi) An exterior angle of a triangle is greater than the opposite interior angles.

Solution:

(i) True.

(ii) False. A right triangle has only one right angle.

(iii) False. In this, the sum of three angles will be less than 180° which is not true.

(iv) False. In this, the sum of three angles will be more than 180° which is not true.

(v) True. As sum of three angles will be 180° which is true.

(vi) False. A triangle has only one obtuse angle.

(vii) True.

(viii) True.

(ix) False. Exterior angle of a triangle is always greater than its each interior opposite angles.

(x) True.

(xi) True.

Question 7.

Fill in the blanks to make the following statements true:

(i) Sum of the angles of a triangle is

(ii) An exterior angle of a triangle is equal to the two opposite angles.

(iii) An exterior angle of a triangle is always than either of the interior opposite angles.

(iv) A triangle cannot have more than right angles.

(v) A triangles cannot have more than obtuse angles.

Solution:

(i) Sum of the angles of a triangle is 180° .

(ii) An exterior angle of a triangle is equal to the two interior opposite angles.

(iii) An exterior angle of a triangle is always greater than either of the interior opposite angles.

(iv) A triangle cannot have more than one right angles.

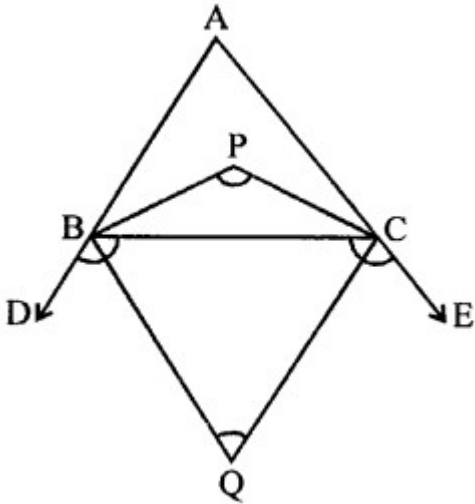
(v) A triangles cannot have more than one obtuse angles.

Question 8.

In a $\triangle ABC$, the internal bisectors of $\angle B$ and $\angle C$ meet at P and the external bisectors of $\angle B$ and $\angle C$ meet at Q. Prove that $\angle BPC + \angle BQC = 180^\circ$.

Solution:

Given : In $\triangle ABC$, sides AB and AC are produced to D and E respectively. Bisectors of interior $\angle B$ and $\angle C$ meet at P and bisectors of exterior angles B and C meet at Q.



To prove : $\angle BPC + \angle BQC = 180^\circ$

Proof : \because PB and PC are the internal bisectors of $\angle B$ and $\angle C$

$$\angle BPC = 90^\circ + \frac{1}{2} \angle A \dots (i)$$

Similarly, QB and QC are the bisectors of exterior angles B and C

$$\therefore \angle BQC = 90^\circ - \frac{1}{2} \angle A \dots (ii)$$

Adding (i) and (ii),

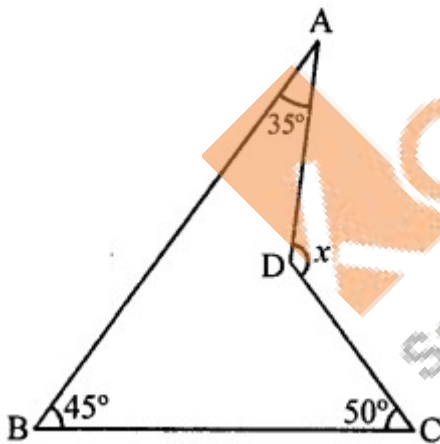
$$\angle BPC + \angle BQC = 90^\circ + \frac{1}{2} \angle A + 90^\circ - \frac{1}{2} \angle A$$

$$= 90^\circ + 90^\circ = 180^\circ$$

Hence $\angle BPC + \angle BQC = 180^\circ$

Question 9.

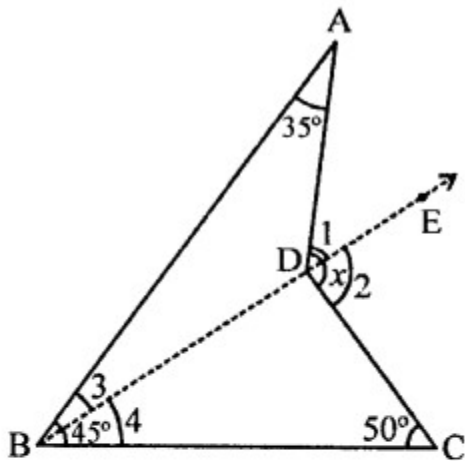
In the figure, compute the value of x.



Solution:

In the figure,

$\angle ABC = 45^\circ$, $\angle BAD = 35^\circ$ and $\angle BCD = 50^\circ$ Join BD and produce it E



In $\triangle ABD$,

$$\text{Ext. } \angle 1 = \angle A + \angle 3 \quad \dots(i)$$

and in $\triangle CBD$,

$$\text{Ext. } \angle 2 = \angle C + \angle 4 \quad \dots(ii)$$

Adding, we get

$$\angle 1 + \angle 2 = \angle A + \angle 3 + \angle C + \angle 4$$

$$\Rightarrow x = \angle A + \angle 3 + \angle 4 + \angle C$$

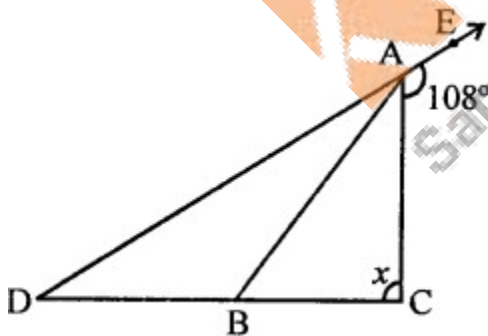
$$\Rightarrow x = \angle A + \angle B + \angle C$$

$$\Rightarrow x = 35^\circ + 45^\circ + 50^\circ = 130^\circ$$

$$\therefore x = 130^\circ$$

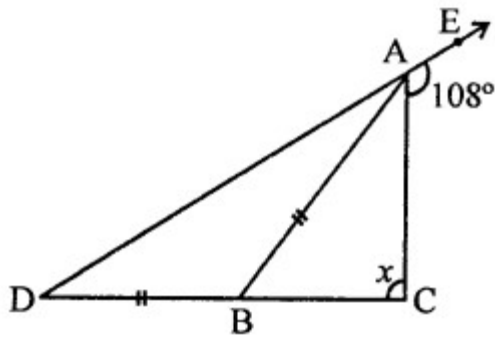
Question 10.

In the figure, AB divides $\angle DAC$ in the ratio 1 : 3 and $AB = DB$. Determine the value of x .



Solution:

In the figure $AB = DB$



AB divides $\angle DAC$ in the ratio 1 : 3 and $\angle CAE = 108^\circ$

But $\angle CAE + \angle DAC = 180^\circ$ (Linear pair)

$$\Rightarrow 108^\circ + \angle DAC = 180^\circ$$

$$\Rightarrow \angle DAC = 180^\circ - 108^\circ = 72^\circ$$

\therefore AB divides it in the ratio 1 : 3

$$\therefore \angle DAB = \frac{72^\circ \times 1}{1+3} = \frac{72^\circ \times 1}{4} = 18^\circ$$

$$\text{and } \angle CAB = \frac{72^\circ}{4} \times 3 = 54^\circ$$

$\therefore AB = BD$

$$\therefore \angle DAB = \angle ADB = 18^\circ$$

Now in $\triangle ADC$,

$$\text{Ext. } \angle CAE = \angle BDA + \angle ACD$$

$$\Rightarrow 108^\circ = 18^\circ + x$$

$$\Rightarrow x = 108^\circ - 18^\circ = 90^\circ$$

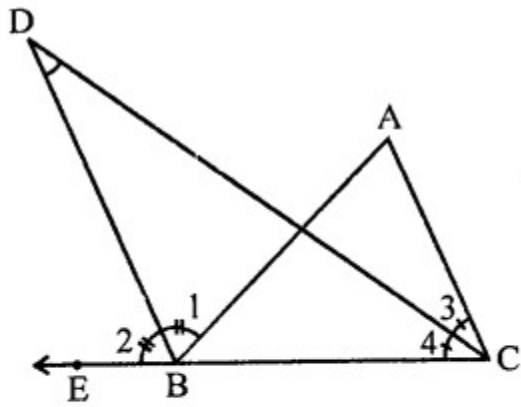
$$\therefore x = 90^\circ$$

Question 11.

ABC is a triangle. The bisector of the exterior angle at B and the bisector of $\angle C$ intersect each other at D. Prove that $\angle D = 12 \angle A$.

Solution:

Given : In $\triangle ABC$, CB is produced to E bisectors of ext. $\angle ABE$ and into $\angle ACB$ meet at D.



To prove : $\angle D = \frac{1}{2} \angle A$

Proof : In $\triangle BDC$,

Ext. $\angle ABE = \angle A + \angle C$

$$\frac{1}{2} \angle ABE = \frac{1}{2} \angle A + \frac{1}{2} \angle C$$

$$\angle 1 = \frac{1}{2} \angle A + \angle 4 \quad \dots(i)$$

(\because CD is bisector of $\angle C$)

In $\triangle BDC$,

Ext. $\angle 2 = \angle D + \angle 4$

$$\Rightarrow \angle D = \angle 2 - \angle 4$$

$$= \angle 1 - \angle 4 \quad (\because \text{BD is bisector of } \angle ABE)$$

$$= \left(\frac{1}{2} \angle A + \angle 4 \right) - \angle 4 \quad [\text{From (i)}]$$

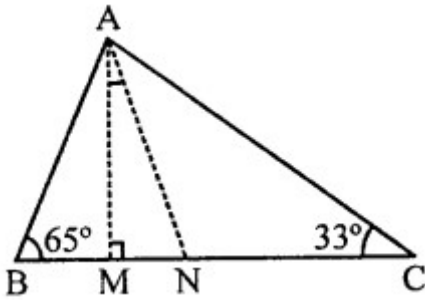
$$= \frac{1}{2} \angle A + \angle 4 - \angle 4$$

$$= \frac{1}{2} \angle A$$

$$\text{Hence } \angle D = \frac{1}{2} \angle A$$

Question 12.

In the figure, $AM \perp BC$ and AN is the bisector of $\angle A$. If $\angle B = 65^\circ$ and $\angle C = 33^\circ$, find $\angle MAN$.



Solution:

In $\triangle ABC$, $\angle B = 65^\circ$, $\angle C = 33^\circ$

$AM \perp BC$ and AN is bisector of $\angle A$

$\therefore AM \perp BC$

$\therefore \angle AMC = 90^\circ$

$\Rightarrow \angle AMN = 90^\circ$

In $\triangle ABC$,

$\angle A + \angle B + \angle C = 180^\circ$

(Sum of angles of a triangle)

$\Rightarrow \angle A + 65^\circ + 33^\circ = 180^\circ$

$\Rightarrow \angle A + 98^\circ = 180^\circ$

$\Rightarrow \angle A = 180^\circ - 98^\circ = 82^\circ$

$\therefore AN$ is the bisector of $\angle A$

$\therefore \angle NAC = \angle NAB = \frac{1}{2} \angle A$

$= \frac{1}{2} \times 82^\circ = 41^\circ$

In $\triangle AMN$,

Ext. $\angle ANM = \angle C + \angle NAC$

$= 33^\circ + 41^\circ = 74^\circ$

In $\triangle MAN$,

$\angle MAN + \angle AMN + \angle ANM = 180^\circ$

(Angles of a triangle)

$\angle MAN + 90^\circ + 74^\circ = 180^\circ$

$\Rightarrow \angle MAN + 164^\circ = 180^\circ$

$\Rightarrow \angle MAN = 180^\circ - 164^\circ = 16^\circ$

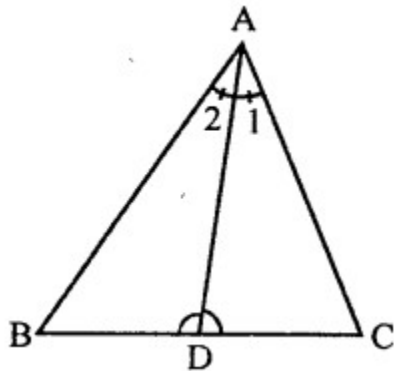
Hence $\angle MAN = 16^\circ$

Question 13.

In a $\triangle ABC$, AD bisects $\angle A$ and $\angle C > \angle B$. Prove that $\angle ADB > \angle ADC$.

Solution:

Given : In $\triangle ABC$,
 $\angle C > \angle B$ and AD is the bisector of $\angle A$



To prove : $\angle ADB > \angle ADC$

Proof: In $\triangle ABC$, AD is the bisector of $\angle A$

$$\therefore \angle 1 = \angle 2$$

In $\triangle ADC$,

$$\text{Ext. } \angle ADB = \angle 1 + \angle C$$

$$\Rightarrow \angle C = \angle ADB - \angle 1 \dots (i)$$

Similarly, in $\triangle ABD$,

$$\text{Ext. } \angle ADC = \angle 2 + \angle B$$

$$\Rightarrow \angle B = \angle ADC - \angle 2 \dots (ii)$$

From (i) and (ii)

$$\therefore \angle C > \angle B \text{ (Given)}$$

$$\therefore (\angle ADB - \angle 1) > (\angle ADC - \angle 2)$$

$$\text{But } \angle 1 = \angle 2$$

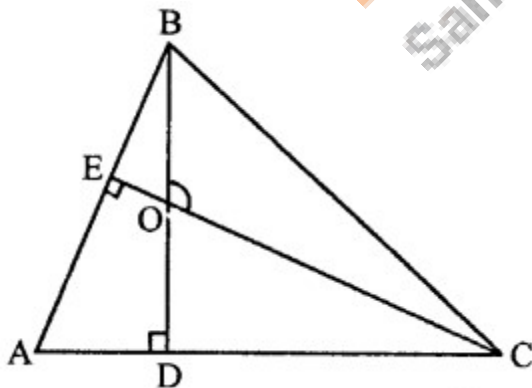
$$\therefore \angle ADB > \angle ADC$$

Question 14.

In $\triangle ABC$, $BD \perp AC$ and $CE \perp AB$. If BD and CE intersect at O, prove that $\angle BOC = 180^\circ - \angle A$.

Solution:

Given : In $\triangle ABC$, $BD \perp AC$ and $CE \perp AB$ BD and CE intersect each other at O



To prove : $\angle BOC = 180^\circ - \angle A$

Proof: In quadrilateral ADOE

$$\angle A + \angle D + \angle DOE + \angle E = 360^\circ \text{ (Sum of angles of quadrilateral)}$$

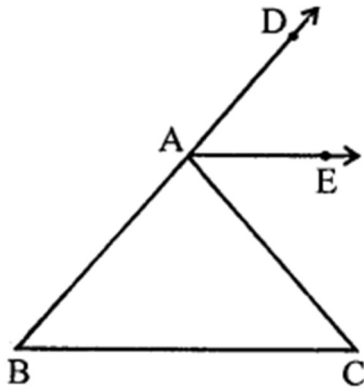
$$\Rightarrow \angle A + 90^\circ + \angle DOE + 90^\circ = 360^\circ$$

$$\angle A + \angle DOE = 360^\circ - 90^\circ - 90^\circ = 180^\circ$$

But $\angle BOC = \angle DOE$ (Vertically opposite angles)
 $\Rightarrow \angle A + \angle BOC = 180^\circ$
 $\therefore \angle BOC = 180^\circ - \angle A$

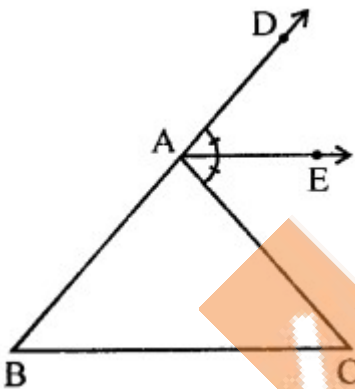
Question 15.

In the figure, AE bisects $\angle CAD$ and $\angle B = \angle C$. Prove that $AE \parallel BC$.



Solution:

Given : In $\triangle ABC$, BA is produced and AE is the bisector of $\angle CAD$
 $\angle B = \angle C$



To prove : $AE \parallel BC$

Proof: In $\triangle ABC$, BA is produced

\therefore Ext. $\angle CAD = \angle B + \angle C$

$\Rightarrow 2\angle EAC = \angle C + \angle C$ (\because AE is the bisector of $\angle CAE$) ($\because \angle B = \angle C$)

$\Rightarrow 2\angle EAC = 2\angle C$

$\Rightarrow \angle EAC = \angle C$

But there are alternate angles

$\therefore AE \parallel BC$