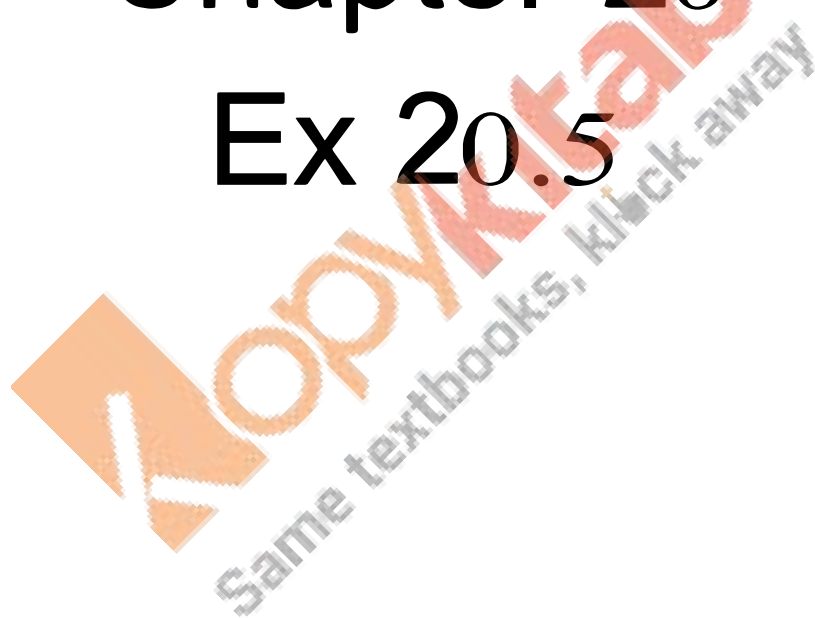


RD Sharma  
Solutions  
Class 11 Maths  
Chapter 20  
Ex 20.5



## Geometric Progressions Ex 20.5 Q 1

Here,

$a, b, c$  are in G.P.

$$b^2 = ac \quad \text{---(i)}$$

Now,

$$2 \log b = \log b^2$$

$$= \log ac$$

$$2 \log b = \log a + \log c$$

$$\log b - \log a = \log c - \log b$$

$\Rightarrow \log a, \log b, \log c$  are in A.P.

## Geometric Progressions Ex 20.5 Q 2

Here,

$a, b, c$  are in G.P., so

$$b^2 = ac$$

$$\frac{2}{\log_b m} = 2 \log_m b$$

$$= \log_m b^2$$

$$= \log_m ac$$

$$= \log_m a + \log_m c$$

$$\frac{2}{\log_b m} = \frac{1}{\log_a m} + \frac{1}{\log_c m}$$

$$\Rightarrow \frac{1}{\log_b m} - \frac{1}{\log_a m} = \frac{1}{\log_c m} - \frac{1}{\log_b m}$$

$$\Rightarrow \frac{1}{\log_a m}, \frac{1}{\log_b m}, \frac{1}{\log_c m} \text{ are in A.P.}$$

### Geometric Progressions Ex 20.5 Q 3

Here,

$a, b, c$  are in A.P.

$$2b = a + c \quad \text{--- (i)}$$

and  $a, b, d$  are in G.P., so

$$b^2 = ad \quad \text{--- (ii)}$$

Now,

$$\begin{aligned}(a - b)^2 &= a^2 + b^2 - 2ab \\ &= a^2 + ad - a(a + c)\end{aligned}$$

Using equation (i) and (ii)

$$\begin{aligned}&= a^2 + ad - a^2 - ac \\ &= ad - ac\end{aligned}$$

$$(a - b)^2 = a(d - c)$$

$$\frac{(a - b)}{a} = \frac{(d - c)}{(a - b)}$$

$\Rightarrow a, (a - b), (d - c)$  are in G.P.

### Geometric Progressions Ex 20.5 Q 4

Here, Let  $R$  be common ratio,

$a_p, a_q, a_r, a_s$  of AP are in GP

$$R = \frac{a_q}{a_p} = \frac{a_r}{a_q}$$

$$= \frac{a_q - a_r}{a_p - a_q} \quad \text{(Ratio property)}$$

$$= \frac{[a + (q - 1)d] - [a + (r - 1)d]}{[a + (p - 1)d] - [a + (q - 1)d]}$$

$$= \frac{(q-r)d}{(p-q)d}$$

$$R = \frac{q-r}{p-q} \text{----- (1)}$$

Now,

$$R = \frac{a_r}{a_q} = \frac{a_s}{a_r}$$

$$= \frac{a_r - a_s}{a_q - a_r} \quad (\text{Ratio property})$$

$$= \frac{[a + (r-1)d] - [a + (s-1)d]}{[a + (q-1)d] - [a + (r-1)d]}$$

$$= \frac{(r-s)d}{(q-r)d}$$

$$R = \frac{r-s}{q-r} \text{----- (2)}$$

From equation as (1) and (2)

$$\frac{q-r}{p-q} = \frac{r-s}{p-r}$$

$\Rightarrow (p-q), (q-r), (r-s)$  are in GP

### Geometric Progressions Ex 20.5 Q 5

$\frac{1}{a+b}, \frac{1}{2b}, \frac{1}{b+c}$  are in A.P.

$$\frac{2}{2b} = \frac{1}{(a+b)} + \frac{1}{(b+c)}$$

$$\frac{1}{b} = \frac{b+c+a+b}{(a+b)(b+c)}$$

$$\frac{1}{b} = \frac{2b+c+a}{ab+ac+b^2+bc}$$

$$ab+ac+b^2+bc = 2b^2+bc+ba$$

$$b^2+ac = 2b^2$$

$$b^2 = ac$$

So,

$a, b, c$  are in G.P.

### Geometric Progressions Ex 20.5 Q 6

$$x^a = x^{\frac{b}{2}} z^{\frac{b}{2}} = z^c = \lambda \text{ (say)}$$

$$x = \lambda^{\frac{1}{a}}, z = \lambda^{\frac{1}{c}}$$

$$x^{\frac{b}{2}} \times z^{\frac{b}{2}} = \lambda$$

$$\lambda^{\frac{1}{a} \left(\frac{b}{2}\right)} \times \lambda^{\frac{b}{2} \times \frac{1}{c}} = \lambda$$

$$\lambda^{\frac{b}{2a} + \frac{b}{2c}} = \lambda^1$$

$$\frac{b}{2a} + \frac{b}{2c} = 1$$

$$\frac{1}{a} + \frac{1}{c} = \frac{2}{b}$$

$$\Rightarrow \frac{1}{a}, \frac{1}{b}, \frac{1}{c} \text{ are in A.P.}$$

### Geometric Progressions Ex 20.5 Q 7

$k + 9, k - 6, 4$  are in G.P.

$$(k - 6)^2 = (k + 9)4$$

$$k^2 + 36 - 12k = 4k + 36$$

$$k^2 - 16k = 0$$

$$k(k - 16) = 0$$

$$k = 0, k = 16$$

### Geometric Progressions Ex 20.5 Q 8

Let  $a - d$ ,  $a$ ,  $a + d$  be numbers in A.P.

Here,

$$a - d + a + a + d = 15$$

$$3a = 15$$

$$a = 5$$

Find

$[(5 - d) + 1]$ ,  $(5 + 3)$ ,  $[(5 + d) + 9]$  are in G.P.

$\Rightarrow$   $(6 - d)$ ,  $8$ ,  $(14 + d)$  are in G.P.

$$(8)^2 = (6 - d)(14 + d)$$

$$64 = 84 + 6d - 14d - d^2$$

$$d^2 + 8d - 20 = 0$$

$$(d + 10)(d - 2) = 0$$

$$d = 2, -10$$

So,

Numbers are 3, 5, 7 or 15, 5, -5

### Geometric Progressions Ex 20.5 Q 9

Let three numbers in A.P. be  $a - d$ ,  $a$ ,  $a + d$

Here,

$$a - d + a + a + d = 21$$

$$3a = 21$$

$$a = 7$$

And,

$(7 - d)$ ,  $(7 - 1)$ ,  $(7 + d) + 1$  are in G.P.

$(7 - d)$ ,  $6$ ,  $(8 + d)$  are in G.P.

$$(6)^2 = (7 - d)(8 + d)$$

$$36 = 56 + 7d - 8d - d^2$$

$$d^2 + d - 20 = 0$$

$$(d + 5)(d - 4) = 0$$

$$d = 4, -5$$

So,

Numbers are 3, 7, 11 or 12, 7, 2.

### Geometric Progressions Ex 20.5 Q 10

Here,

$a, b, c$  are in A.P.

Let  $a = A - d$ ,  $b = A$ ,  $c = A + d$

Here,

$$a + b + c = 18$$

$$A - d + A + A + d = 18$$

$$3A = 18$$

$$A = 6$$

And,

$(a + 4)$ ,  $(b + 4)$ ,  $(c + 36)$  are in G.P.

$(6 - d + 4)$ ,  $(6 + 4)$ ,  $(6 + d + 36)$  are in G.P.

$(10 - d)$ ,  $(10)$ ,  $(42 + d)$  are in G.P.

$$(10)^2 = (10 - d)(42 + d)$$

$$100 = 420 + 10d - 42d - d^2$$

$$d^2 + 32d - 320 = 0$$

$$(d + 40)(d - 8) = 0$$

$$d = -40, 8$$

So,

Numbers of  $-2, 6, 14$  or  $46, 6, -34$ .

## Geometric Progressions Ex 20.5 Q 11

Let numbers are  $a, ar, ar^2$

$$a + ar + ar^2 = 56 \text{ ----- (1)}$$

$(a - 1), (ar - 7), (ar^2 - 21)$  are in AP

$$\begin{aligned} \Rightarrow 2(ar - 7) &= a - 1 + ar^2 - 21 \\ &= (ar^2 + a) - 22 \end{aligned}$$

$$2ar - 14 = (56 - ar) - 22 \quad \text{[using equation (1)]}$$

$$2ar - 14 = 34 - ar$$

$$3ar = 48$$

$$ar = 16 \text{ ----- (2)}$$

$$a = \frac{16}{r}$$

Put  $a$  in equation (1),

$$\frac{16 + 16r + 16r^2}{r} = 56$$

$$16 + 16r + 16r^2 = 56r$$

$$16r^2 - 40r + 16 = 0$$

$$2r^2 - 5r + 2 = 0$$

$$2r^2 - 4r - r + 2 = 0$$

$$2r(r - 2) - 1(r - 2) = 0$$

$$(r - 2)(2r - 1) = 0$$

$$r = 2, \frac{1}{2}$$

Put  $r$  in equation (2),

$$ar = 16$$

$$\text{for } r = \frac{2}{a} = 8$$

$$\text{for } r = \frac{1}{2}, a = 32$$

thus, there numbers are

$$8, 16, 32$$

in both cases.

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