

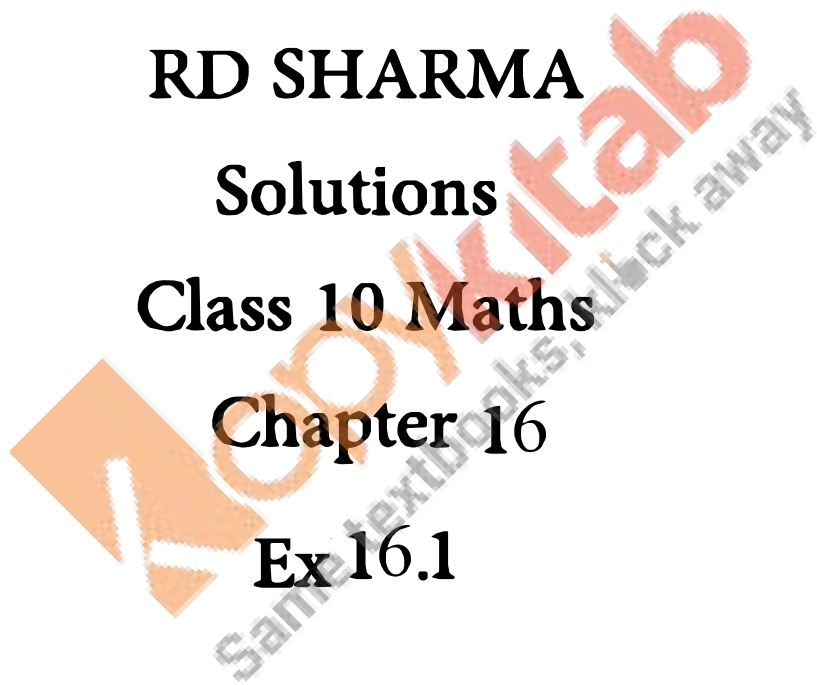
**RD SHARMA**

**Solutions**

**Class 10 Maths**

**Chapter 16**

**Ex 16.1**



**Question 1: How many balls, each of radiuses 1 cm can be made from a solid sphere of lead of radius 8 cm?**

**Solution:**

Given that a solid sphere of radius =8 cm

With this sphere, we have to make spherical balls = 1 cm

Since we don't know number of balls let us assume that number of balls be n

We know that,

$$\text{Volume of the sphere} = \frac{4}{3} \pi r^3$$

The volume of the solid sphere equal to sum of the n spherical balls.

$$= n \left( \frac{4}{3} \pi 1^3 \right) = \frac{4}{3} \pi n$$

$$= n = 8^3 = 512$$

Hence 512 numbers of balls can be made of radius 1 cm of a solid sphere of radius 8 cm.

**Question 2: How many spherical bullets each of 5 cm in diameter can be cast from a rectangular block of metal 11dm \*1m\*5dm?**

**Solution:**

Given that a metallic block which is rectangular of dimension 11dm\*1m\*5dm

Given that the diameter of each bullet is 5 cm

$$\text{Volume of the sphere} = \frac{4}{3} \pi r^3$$

Dimensions of the rectangular block = 11dm\*1m\*5dm

Since we know that 1 dm = 10<sup>-1</sup>m

$$11 \cdot 10^{-1} \cdot 1 \cdot 5 \cdot 10^{-1} = 55 \cdot 10^{-2} \dots\dots\dots(i)$$

Diameter of the bullet = 5cm

Radius of the bullet = 5/2 = 2.5 cm

So the volume of the rectangular block equals to the sum of the volumes of the n spherical bullets

Let the number of bullets be n

$$55 \times 10^{-2} = n \left( \frac{4}{3} \pi 1^3 \right) n \left( \frac{4}{3} \pi 1^3 \right)$$

$$= n = 8400$$

Numbers of bullets formed were 8400.

**Question.3: A spherical ball of radius 3cm is melted and recast into three spherical balls. The radii of the two balls are 2cm and 1.5cm respectively. Determine the diameter of the third ball?**

**Solution:**

According to the question

Radius of the spherical ball = 3cm

We know that the volume of the sphere =  $\frac{4}{3} \pi r^3$

So its volume (v) =  $\frac{4}{3} \pi r^3$

Given,

That the ball is melted and recast into 3 spherical balls.

Volume ( $V_1$ ) of first ball =  $\frac{4}{3} \pi 1.5^3$

Volume ( $V_2$ ) of second ball =  $\frac{4}{3} \pi 2^3$

Radii of the third ball be = r cm

Volume of third ball ( $V_3$ ) =  $\frac{4}{3} \pi r^3$

Volume of the spherical ball is equal to the volume of the 3 small spherical balls.

$$V = V_1 + V_2 + V_3$$

$$\frac{4}{3} \pi r^3 = \frac{4}{3} \pi 1.5^3 + \frac{4}{3} \pi 2^3 + \frac{4}{3} \pi r^3$$

Now,

Cancelling out the common part from both sides of the equation we get,

$$(3)^3 = (2)^3 + (1.5)^3 + r^3$$

$$r^3 = 3^3 - 2^3 - 1.5^3 \text{ cm}^3$$

$$r^3 = 15.6 \text{ cm}^3$$

$$r = (15.6)^{\frac{1}{3}} \text{ cm}$$

$$r=2.5\text{cm}$$

we know diameter = 2\* radius

$$=2*2.5 \text{ cm}$$

$$=5.0 \text{ cm}$$

The diameter of the third ball is 5.0 cm

**Question.4: 2.2 cubic dm of brass is to drawn into a cylindrical wire of 0.25cm diameters. Find the length of the wire?**

**Solution:**

Given,

2.2 dm<sup>3</sup> of brass is to be drawn into a cylindrical wire of 0.25cm diameter

Radius of the wire (r) = d/2

$$=0.25/2 = 0.125*10^{-2}\text{cm}$$

Now, 1cm =0.01m

So, 0.1cm=0.001m

Let the length of the wire be (h)

Volume of the cylinder=  $\pi r^2 h$

Volume of brass of 2.2 dm<sup>3</sup> is equal to volume of cylindrical wire.

$$227(0.125 \times 10^{-2})^2 \times h = 2.2 \times 10^{-3} \frac{22}{7} (0.125 \times 10^{-2})^2 \times h = 2.2 \times 10^{-3}$$

$$H=448 \text{ m}$$

The length of the cylindrical wire is 448m

**Question 5: What length of a solid cylinder 2 cm in diameter be taken to recast into a hollow cylinder of length 16 cm, external diameter 20cm and thickness 2.5mm?**

**Solution:**

According to the question

Diameter of the solid cylinder=2 cm

The solid cylinder is recast into a hollow cylinder of length 16 cm, external diameter of 20cm and thickness of 2.5 cm

$$\text{Volume of the cylinder} = \pi r^2 h - \pi r^2 h$$

Radius of the cylinder = 10 cm

$$\text{So, volume of the solid cylinder} = \pi 10^2 h - \pi 10^2 h$$

Let the length of the solid cylinder be l

$$\text{Volume of the hollow cylinder} = \pi h(R^2 - r^2) - \pi h(R^2 - r^2)$$

Thickness of the cylinder = (R-r)

$$0.25 = 10 - r$$

Internal radius of the cylinder is 9.75cm

$$\text{Volume of the hollow cylinder} = \pi 16(100 - 95.0625) - \pi 16(100 - 95.0625)$$

Hence, the volume of the solid cylinder is equal to the volume of the hollow cylinder

Equation I = equation ii

$$\pi 10^2 h - \pi 10^2 h = \pi * 16(100 - 95.06)$$

$$= h = 79.04 \text{ cm}$$

Length of the solid cylinder is 79.04 cm.

**Question 6: A cylindrical vessel having the diameter equal to its height is full of water which is poured into two identical cylindrical vessels with diameter 42 cm and height 21 cm which are filled completely. Find the diameter of the cylindrical vessel.**

**Sol:**

Given,

$$\text{The diameter is equal to the height of a cylinder} = \pi r^2 h - \pi r^2 h$$

$$\text{So, volume} = \pi r^2 2r - \pi r^2 2r \quad (h=2r) \dots \dots \dots (i)$$

$$2\pi r^3 - 2\pi r^3$$

$$\text{Volume of each vessel} = \pi r^2 h - \pi r^2 h$$

Diameter = 42 cm

Height = 21 cm

$$\text{Diameter} = 2r$$

$$2r = 42 \text{ cm}$$

$$r = 21 \text{ cm}$$

$$\text{Volume of vessel} = \pi \times 21^2 \times 21 \quad \dots\dots\dots(ii)$$

Since the volumes of equation i and ii are equal

So equating both the equations

$$r^3 = (21)^3$$

$$r = 21 \text{ cm}$$

$$d = 42 \text{ cm}$$

The diameter of the cylindrical vessel is 42cm

**Question 7: 50 circular plates each of diameter 14cm and thickness 0.5cm are placed one above the other to form right circular cylinder. Find its total surface area**

**Solution:**

Given that the 50 circular plates each with diameter 14 cm

Radius of circular plates = 7 cm

Thickness of plates = 0.5 cm

Since these plates are one above the other so total thickness of plates =  $0.5 \times 50 = 25 \text{ cm}$

$$\text{Total surface area of a cylinder} = 2\pi r \times h + 2\pi r^2$$

$$2\pi r(h+r) = 2 \times \frac{22}{7} \times 7(25+7) = 2 \times \frac{22}{7} \times 7(25+7)$$

$$\text{Total surface area} = 1408 \text{ cm}^2$$

The total surface area of the cylinder is  $1408 \text{ cm}^2$

**Question 8: 25 circular plates each of radius 10.5cm and thickness 1.6 cm are placed one above the other to form a solid circular cylinder. Find the curved surface area and volume of the cylinder so formed.**

**Solution:**

Given that 250 circular plates each with radius 10.5 cm

Thickness is 1.6 cm.

Since plates are placed one above the other so its height becomes =  $1.6 \times 25 = 40$  cm

$$\begin{aligned} \text{Volume of the cylinder} &= \pi r^2 h \\ &= \pi 10.5^2 \times 40 \end{aligned}$$

$$\begin{aligned} \text{Curved surface area of a cylinder} &= 2\pi r \times h \\ &= 2\pi 10.5 \times 40 \end{aligned}$$

Volume of the cylinder is  $13860 \text{ cm}^3$

Curved surface area of the cylinder is  $2640 \text{ cm}^2$

**Question 9: The diameter of a metallic sphere is equaled to 9 cm. It is melted and drawn into a long wire of diameter 2 mm having the uniform cross section. Find the length of the wire?**

**Solution:**

Given,

Diameter of the metallic sphere = 9 cm

Radius of the metallic sphere =  $\frac{9}{2} \text{ cm} = 4.5 \text{ cm}$

$$\begin{aligned} \text{Volume of the sphere} &= \frac{4}{3} \pi r^3 \\ &= \frac{4}{3} \pi \times 4.5^3 \\ &= 381.703 \text{ cm}^3 \dots\dots\dots (i) \end{aligned}$$

Diameter of the cylindrical wire = 2 mm =  $\frac{2}{10} \text{ cm} = 0.2 \text{ cm}$

The radius of the cylindrical wire be =  $\frac{0.2}{2} \text{ cm} = 0.1 \text{ cm}$

Let the height of the cylindrical wire be = h cm

$$\begin{aligned} \text{Volume of the cylindrical wire} &= \pi r^2 \times h \\ &= \pi \times 0.1^2 \times h \dots\dots\dots (ii) \end{aligned}$$

Since the metallic sphere is melted and recast into a long cylindrical wire.

So comparing and equating both the above-marked equations

We get,

$$381.703 = \pi \times 0.1^2 \times h \quad \pi \times 0.1^2 \times h \dots\dots\dots(ii)$$

$$H = 12150 = 12150 \text{ cm}$$

The required length of the wire after recasting of the metallic sphere is 12150 cm.

**Question 10: Find the number of smaller sphere required if the radius of the larger ball is four times the radius of the smaller ball.**

**Solution:**

According to the question,

Let the radius of the smaller ball be = r cm

Now, the radius of the larger ball be = 4r cm

$$\text{Volume of the smaller sphere} = \frac{4}{3} \pi \times r^3 \dots\dots(i)$$

$$\text{Volume of the larger sphere} = \frac{4}{3} \pi \times (4r)^3 \dots\dots(ii)$$

Now, dividing equation (ii) by (i) .we get,

Number of smaller balls (n)

$$n = \frac{\frac{4}{3} \pi \times (4r)^3}{\frac{4}{3} \pi \times r^3} = 64$$

The volume of the larger sphere is 8 times the volume of the smaller ball.

$$\text{Curved surface area of the smaller sphere} = 4 \pi \times r^2 \dots\dots(iii)$$

$$\text{Curved surface area of the larger sphere} = 4 \pi \times (2r)^2 \dots\dots(iv)$$

Now, dividing equation (iv) by (iii). We get,

Number of smaller spheres (N)

$$N = \frac{4 \pi \times (2r)^2}{4 \pi \times r^2} = 4$$

The curved surface area of large ball is four times the curved surface area of the smaller ball.

**Question 11: A copper sphere of radius 3 cm is melted and re-casted into a right circular cone of height 3 cm. Find the radius of the base of the cone?**



**Solution:**

Given,

Radius of the sphere = 5 cm

$$\text{Volume of the sphere} = \frac{4}{3} \pi \times (r)^3$$

$$= \frac{4}{3} \pi \times (5)^3 \dots\dots\dots(i)$$

The given sphere is melted and recast into a right circular cone

Height of the cone = 3cm

$$\text{Volume of the right circular cone} = \frac{1}{3} \pi \times (r)^2 \times h$$

$$= \frac{1}{3} \pi \times (r)^2 \times 3 \dots\dots\dots(ii)$$

Now comparing equation (i) and (ii) we get

$$r^2 = 36$$

$$r = 6 \text{ cm}$$

The radius of the cone is 6 cm

**Question 12:** A copper wire of diameter 1 cm and length 8 cm is drawn into a wire of length 18 m of uniform thickness. Find the thickness of the wire?

**Solution:**

Given,

Diameter of the copper wire = 1 cm

Radius of the copper wire = 1 / 2 cm = 0.5 cm

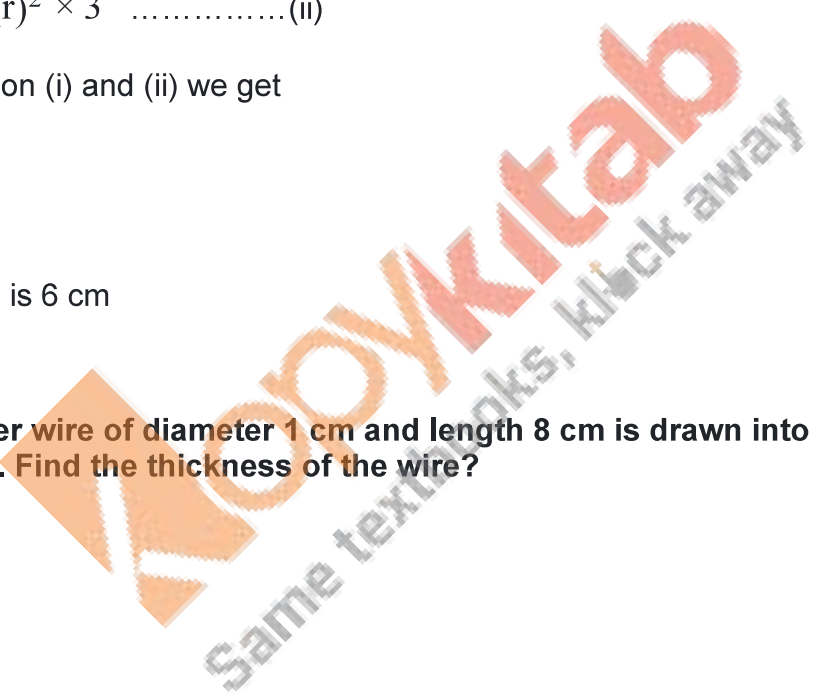
Length of the copper rod = 8 cm

$$\text{Volume of the cylinder} = \pi \times r^2 \times h$$

$$= \pi \times 0.5^2 \times 10 \dots\dots\dots(i)$$

Length of the wire = 18 m = 1800cm

$$\text{Volume of the wire} = \pi \times r^2 \times h$$



$$= \pi r^2 \times 1800 \quad \pi r^2 \times 1800 \dots\dots\dots (ii)$$

Now equating both the equations. We get,

$$r^2 = 200.00044$$

$$r = 0.033 \text{ cm}$$

The radius or thickness of the wire is 0.033 cm

**Question 13: The diameters of the internal and external surface area of hollow spherical shell are 10cm and 6 cm respectively. If it is melted and recast into a solid cylinder of length of  $2\frac{2}{3}$ , find the diameter of the cylinder?**

**Solution:**

Given,

Internal diameter of the hollow sphere = 6 cm

Internal radius of the hollow sphere =  $6/2 \text{ cm} = 3 \text{ cm}$

External diameter of the hollow sphere = 10 cm

External radius of the hollow sphere =  $10/2 \text{ cm} = 5 \text{ cm}$

$$\text{Volume of the hollow spherical shell} = \frac{4}{3} \pi R^3 - \frac{4}{3} \pi r^3$$

$$= \frac{4}{3} \pi \times 5^3 - \frac{4}{3} \pi \times 3^3 \dots\dots\dots (i)$$

Given the length of the solid cylinder =  $2\frac{2}{3} \text{ cm}$

Let the radius of the solid cylinder be  $r \text{ cm}$

$$\text{Volume of the cylinder} = \pi r^2 \times h$$

$$= \pi r^2 \times 2\frac{2}{3} \dots\dots\dots (ii)$$

Now equating both the above marked equations in order to obtain the radius of the cylinder

$$r^2 = 49$$

$$r = 7$$

$$d = 7 * 2 = 14 \text{ cm}$$

**Question 14:** How many coins 1.75cm in diameter and 2mm thick must be melted to form a cuboid 11cm\*10cm\*7cm?

**Solution:**

So its volume =  $11 \times 10 \times 7 \text{ cm}^3$

Given diameter = 1.75 cm

Radius = 0.875 cm

Volume of the cylinder =  $\pi r^2 h$

$$= \pi (0.875)^2 (0.2)$$

$$V_1 = V_2 \times n$$

By calculating the above problem we get,

$$N = 1600$$

Number of coins are 1600

**Question 15:** The surface area of the solid metallic sphere is  $616 \text{ cm}^2$ . It is melted and recast into a cone of height 28 cm. find the diameter of the base of the cone so formed?

**Solution:**

The height of the cone = 28 cm

Surface area of the sphere =  $616 \text{ cm}^2$

We know that the surface area of the sphere =  $4\pi r^2$

$$= 4\pi r^2 = 616$$

$$= r^2 = 49$$

$$= r = 7$$

Radius of the sphere = 7 cm

Let R be the radius of the cone

Volume of the cone =  $\frac{1}{3}\pi R^2 h$

$$= \frac{1}{3}\pi R^2 (28) \dots\dots\dots(i)$$

$$\text{Volume of the sphere} = \frac{4}{3} \pi r^3$$

$$= \frac{4}{3} \pi 7^3 \dots\dots\dots(ii)$$

Comparing equation (i) and (ii)

$$R^2 = 49$$

$$R = 7$$

$$\text{Diameter of the cone} = 7 \times 2 = 14 \text{ cm}$$

The diameter of the base of the cone is 14 cm

**Question 16: A spherical shell of internal and external diameter 6cm and 10cm respectively is melted and recast into a cylinder of diameter 14 cm. find the height of the cylinder ?**

**Solution:**

Internal diameter of a hollow spherical shell = 6 cm

Internal radius of a hollow spherical shell = 3 cm

External diameter of a hollow spherical shell = 10 cm

External radius of a hollow spherical shell = 5 cm

$$\text{Volume of the spherical shell} = \frac{4}{3} \pi (5^3 - 3^3) \dots\dots\dots(i)$$

Diameter of the cylinder = 14 cm

Radius of the cylinder = 7cm

Let the height of the cylinder be (x) cm

$$\text{Volume of the cylinder} = \pi \times 7^2 \times x \dots\dots\dots(ii)$$

According to the question,

Volume of the cylinder is equals to the volume of the spherical shell.

$$\frac{4}{3} \pi (5^3 - 3^3) = \pi \times 7^2 \times x$$

$$X = 2.666 \text{ cm}$$

**Question 17: A hollow sphere of internal and external diameters 4cm and 8cm is melted into a cone of base diameter 8 cm. Calculate the height of the cone?**

**Solution:**

Given,

Internal diameter of hollow sphere = 4 cm

Internal radius of hollow sphere = 2 cm

External diameter of hollow sphere = 8 cm

External radius of hollow sphere = 4 cm

$$\text{Volume of the hollow sphere} = \frac{4}{3}\pi \times (4^3 - 2^3) \dots\dots\dots(i)$$

Given, diameter of the cone = 8 cm

Radius of the cone = 4 cm

Let the height of the cone be x cm

$$\text{Volume of the cone} = \frac{1}{3}\pi \times 4^2 \times h \dots\dots\dots(ii)$$

Since the volume of the hollow sphere and cone are equal.

So, equating equations i and ii, we get,

$$\frac{4}{3}\pi \times (4^3 - 2^3) = \frac{1}{3}\pi \times 4^2 \times h$$

$$H = 12 \text{ cm}$$

The height of the cone so formed is having a height of 12 cm

**Question 18: A path 2m wide surrounds a circular pond of diameter of 40 m. How many cubic meters of sand are required to grave the path to a depth of 20 cm?**

**Solution:**

Given,

Diameter of the circular pond = 40 m

Radius of the pond =  $20\text{m}/2 = 10\text{m}$  ( $r = d/2$ )

Thickness = 2m

We know 1cm = 0.01m

10cm = 10/100 m = 0.10m

Since the whole view of the pond looks like a hollow cylinder. So,

Thickness (t) = R-r

2 = R-20

R = 22m

Volume of the hollow cylinder =  $\pi(R^2 - r^2) \times h$

$$\pi(22^2 - 20^2) \times 0.10$$

$$= 52.77 \text{m}^3$$

Volume of the cylinder is 52.77m<sup>3</sup>.

Since it is a hollow cylinder the volume of the cylinder indicates the required amount of sand needed to spread across to a depth of 20 m.

**Question 19: A 16 m deep well with diameter 3.5 m is dug up and the earth from it is spread evenly to form a platform 27.5 m by 7m. Find the height of the platform?**

**Solution:**

Let us assume the well is a solid right circular cylinder

Radius(r) of the cylinder = 3.5/2 m = 1.75 m

Height or depth of the well (h) = 16 m

Volume of the cylinder =  $\pi r^2 \times h$

$$\pi \times 1.75^2 \times 16 \dots\dots\dots (i)$$

Given,

The length of the platform (l) = 27.5 m

Breadth of the platform (b) = 7 m

Let the height of the platform be x m

Volume of the rectangle = l\*b\*h

$$V = 27.5 \times 7 \times x \dots\dots\dots (ii)$$

Since the well is spread evenly to form the platform

So equating equations (i) and (ii), we get .

$$V_1 = V_2$$

$$\pi \times 1.75^2 \times 16 = \pi \times 1.75^2 \times 16 = 27.5 \times 7 \times x$$

$$x = 0.8 \text{ m}$$

Therefore  $x = 80 \text{ cm}$

The height of the platform is 80 cm.

**Question 20:** A well of diameter 2 m is dug 14 m deep. The earth taken out of it is evenly spread all around it to form an embankment of height 40 cm. find the width of the embankment?

**Solution:**

Radius of the circular cylinder (r) = 2/2 m = 1 m

Height of the well (h) = 14 m

$$\text{Volume of the solid circular cylinder} = \pi r^2 \times h \quad \dots\dots\dots (i)$$

$$= \pi \times 1^2 \times 14 = \pi \times 1^2 \times 14$$

Given,

The height of the embankment (h) = 40 cm

$$= 0.4 \text{ m}$$

Let the width of the embankment be (x) m.

$$\text{Volume of the embankment} = \pi r^2 \times h = \pi r^2 \times h$$

$$= \pi \times ((1+x)^2 - (1)^2) \times 0.4 = \pi \times ((1+x)^2 - (1)^2) \times 0.4 \quad \dots\dots\dots (ii)$$

Since the well is spread evenly to form embankment so their volumes will be same

So equating equations i and ii, we get

$$\pi \times 1^2 \times 14 = \pi \times ((2.5+x)^2 - (2.5)^2) \times 0.20 = \pi \times ((2.5+x)^2 - (2.5)^2) \times 0.20$$

$$X = 5 \text{ m}$$

The width of the embankment is 5 m.

**Question 21:** A well with inner radius 4 m is dug up and 14 m deep. Earth taken out of it has been evenly all around a width of 3 m it to form an embankment. Find the height of the

**embankment?**

**Solution:**

Given,

Inner radius of the well = 4 m

Depth of the well = 14 m

$$\text{Volume of the cylinder} = \pi \times r^2 \times h$$

$$= \pi \times 4^2 \times 14 \quad \dots\dots\dots (i)$$

According to the question,

The earth taken out from the well is evenly spread all around it to form an embankment

Width of the embankment = 3 m

Outer radii of the well = 3 + 4 m = 7 m

$$\text{Volume of the hollow well} = \pi \times (R^2 - r^2) \times h$$

$$= \pi \times (7^2 - 4^2) \times h \quad \dots\dots\dots (ii)$$

Comparing both equations we get

$$H = 6.78 \text{ m}$$

The height of the well so formed is 6.78 m.

**Question 22: A well of diameter 3m is dug up to 14m deep. The earth taken out of it has been spread evenly all around it to a width of 3m to form an embankment. Find the height of the embankment.**

**Sol:**

Given

Diameter of the well = 3 m

Radius of the well =  $\frac{3}{2}$  m = 1.5m

Depth of the well = 14 m

Width of the embankment = 4 m

Radius of the outer surface of the embankment =  $4 + \frac{3}{2}$  m = 5.5 m



Let the height of the embankment be = h m

$$\begin{aligned} \text{Volume of the embankment} &= \pi \times (R^2 - r^2) \times h \\ &= \pi \times (5.5^2 - 1.5^2) \times h \end{aligned} \quad \dots\dots\dots (i)$$

$$\begin{aligned} \text{Volume of earth dug out} &= \pi \times (r^2) \times h \\ &= \pi \times (2^2) \times 14 \end{aligned} \quad \dots\dots\dots (ii)$$

Comparing both the equations we get,

$$H = 98 \frac{9}{8} \text{ m}$$

Height of the embankment is  $98 \frac{9}{8}$  m

**Question 23:** Find the volume largest right circular cone that can be cut out of a cone of a cube whose edge is 9 cm.

**Solution:**

Given,

The side of the cube = 9 cm

The largest cone is curved from cube diameter of base of cone = side of the cube

$$2r = 9$$

$$r = 9/2 \text{ cm} = 4.5 \text{ cm}$$

Height of cone = side of cube

$$\text{Height of cone (h)} = 9 \text{ cm}$$

$$\begin{aligned} \text{Volume of the largest cone to fit in} &= \frac{1}{3} \times \pi \times r^2 \times h \\ &= \frac{1}{3} \times \pi \times 4.5^2 \times 9 \\ &= 190.92 \text{ cm}^3 \end{aligned}$$

The volume of the largest cone to fit in is having a volume of 190.92 cm<sup>3</sup>

**Question 24:** Rain water which falls on a flat rectangular surface of length 6m and breadth 4m is transferred into a cylindrical vessel of internal radius 20 cm .What will be the height of water in the cylindrical vessel if a rainfall of 1cm has fallen?

**Solution:**

Given,

Length of the rectangular surface = 6 m = 600 cm

Breadth of the rectangular surface = 4m = 400cm

Height of the perceived rain = 1 cm

Volume of the rectangular surface = length \* breadth \* height

$$= 600 \times 400 \times 1 \text{ cm}^3$$

$$= 240000 \text{ cm}^3 \dots\dots\dots (i)$$

Given,

Radius of the cylindrical vessel = 20 cm

Let the height of the cylindrical vessel = h cm

Volume of the cylindrical vessel =  $\pi \times r^2 \times h$   $\pi \times r^2 \times h$

$$= \pi \times 20^2 \times h \pi \times 20^2 \times h \dots\dots\dots (ii)$$

Since rains are transferred to cylindrical vessel

So, equating both the above marked equations:

$$240000 = \pi \times 20^2 \times h \pi \times 20^2 \times h$$

$$H = 190.9 \text{ cm}$$

The height of the cylindrical vessel is 190.9 cm.

**Question 25: A conical flask of water. The flask has base radius(r) and height (h). The water is poured into a cylindrical flask of base radius  $M_r$ . Find the height of water in the cylindrical flask?**

**Solution**

Given:

Base radius of the conical flask = r m

Height of the conical flask = h m

$$\text{Volume of the cone} = \frac{1}{3} \pi \times r^2 \times h \pi \times r^2 \times h \dots\dots\dots (i)$$

Given,

Base radius of the cylindrical flask is  $M_r$ .

Let the height of the flask be  $h_1$ .

$$\text{Volume of the cylinder} = \pi \times r^2 \times h$$

$$\text{It's volume} = \frac{1}{3} \pi \times r^2 \times h \dots\dots\dots(ii)$$

Since water in conical flask is poured into cylindrical flask their volumes are same.

So, equations i and ii are same .

$$\pi \times r^2 \times h = \frac{1}{3} \pi \times r^2 \times h$$

$$h_1 = h/3$$

The required height of the cylindrical vessel is  $h/3$ .

**Question 26: A rectangular tank is 15 m long and 11m in breadth is required to receive entire liquid contents from a full cylindrical tank of internal diameter 21 m and length 5 m .Find the least height of the tank that will serve the purpose?**

**Solution:**

Given,

Length of the rectangular tank = 15 m

Breadth of the rectangular tank = 11 m

Let the height of the rectangular tank be =h m

Volume of the rectangular tank = length \*breadth \* height

$$=15 \times 11 \times h \text{ m}^3 \dots\dots\dots(i)$$

Given,

Radius of the cylindrical tank =  $21/2$  m = 10.5 m

Height of the tank = 5 m

$$\text{Volume of the cylindrical tank} = \pi \times r^2 \times h$$

$$= \pi \times 10.5^2 \times 5 \dots\dots\dots(ii)$$

Since equation i and ii are having same volumes so, equating both equations

We get,

$$165 * h = \pi \times 10.5^2 \times 5 \pi \times 10.5^2 \times 5$$

$$h = 10.5 \text{ m}$$

The height of the tank is 10.5 m.

**Question 27: A hemispherical bowl of internal radius 9 cm is full of liquid. This liquid is to be filled into cylindrical shaped small bottles each of diameter 3 cm and height 4 cm. How many bottles are necessary to empty the bowl?**

**Solution:**

Given,

The internal radius of the hemispherical bowl = 9 cm

$$\text{Volume of the hemisphere} = \frac{2}{3} \pi r^3$$

$$= \frac{2}{3} \pi \times 9^3 \dots\dots\dots(i)$$

Given,

Diameter of the cylindrical bottle = 3 cm

Radius =  $\frac{3}{2}$  cm = 1.5 cm

$$\text{Volume of the cylinder} = \pi r^2 h$$

$$= \pi \times 1.5^2 \times 4 \dots\dots\dots(ii)$$

Volume of the hemispherical bowl is equals to (n) multiplied by volume of the cylindrical bottles.

Now,

Comparing equations i and ii,

We get,

$$\frac{2}{3} \pi \times 9^3 = \pi \times 1.5^2 \times 4 \times n$$

$$n = 54$$

54 cylindrical bottles are required to empty a hemispherical bowl.

**Question 28: A cylindrical tube of radius 12 cm contains water to a depth of 20 cm. A spherical ball is dropped into the tube and the level of water is raised by 6.75 cm. Find the radius of the**

ball?

**Solution:**

Given,

The radius of a cylindrical tube (r) = 12 cm

Level of water raised in the tube (h) = 6.75 cm

$$\text{Volume of the cylinder} = \pi \times r^2 \times h$$

$$= \pi \times 12^2 \times 6.75$$

Let r be the radius of the spherical ball

$$\text{Volume of the sphere} = \frac{4}{3} \pi \times r^3 \dots\dots\dots(ii)$$

To find the radius of the spherical ball of unknown radius r we need to equate equations i and ii

We get,

$$\pi \times 12^2 \times 6.75 = \frac{4}{3} \pi \times r^3$$

$$r^3 = 729$$

$$r = 9 \text{ cm}$$

The radius of the spherical ball is 9 cm.

**Question 29:** 500 persons have to dip in a rectangular tank which is 80 m long and 50 m broad. What is the rise in the level of water in the tank, if the average displacement of water by a person is 0.04m<sup>3</sup>?

**Solution:**

Given,

The length of a rectangular tank (l) = 50 m

Breadth of the rectangular tank (b) = 10 m

Total displacement of water in a rectangular tank by 400 persons = 400 \* 0.02 m<sup>3</sup>

$$= 8 \text{ m}^3 \dots\dots\dots(i)$$

Let the depth of tank be h m

Volume of the rectangular tank = length \* breadth \* height

$$= l * b * h$$

$$= 50 * 10 * h \text{ m}^3 = 500hm^3 \dots\dots\dots(ii)$$

Now equating equations i and ii, we get ,

$$8 = 500 * h$$

$$H = 0.016 \text{ m}$$

The rise in water level of the rectangular tank is 0.016m.

**Question 30: A cylindrical jar of radius 6cm contains oil. Iron spheres each of radius 1.5 cm are immersed in the oil. How many spheres are necessary to raise the level of the oil by 2 cm?**

**Solution:**

Given,

The radius of the cylindrical jar (r) = 6 cm

Height of the cylindrical jar (h) = 2 cm

Let the number of balls be (n)

$$\text{Volume of the cylinder} = \pi * r^2 * h \quad \pi * r^2 * h$$

$$= \pi * 6^2 * 2 \quad \pi * 6^2 * 2 \dots\dots\dots(i)$$

Let the Radius of the sphere be 1.5 cm

$$\text{Volume of the sphere} = \frac{4}{3} \pi * r^3 \quad \dots\dots\dots(ii)$$

Volume of the cylindrical jar is equal to the sum of volume of (n) number of spheres.

Now, equating equations I and ii we get,

$$\pi * 6^2 * 2 = n * \left[ \frac{4}{3} \pi * r^3 \right] \quad \pi * 6^2 * 2 = n * \left[ \frac{4}{3} \pi * r^3 \right]$$

$$\pi * 6^2 * 2 \quad \pi * 6^2 * 2 = n * 4.1904$$

$$N = 16$$

$$= 16$$

16 spherical balls are required to raise the water level by 2 cm.

**Question 31: The metallic spheres each of radius 2 cm are packed into a rectangular box of internal dimension 16 cm\* 8cm\* 8cm where 16 spheres are packed the box is filled with**

**preservation liquid . Find the volume of this liquid ?**

**Solution:**

Given,

Radius of the metallic spheres = 2 cm

$$\text{Volume of the sphere} = \frac{4}{3} \pi \times (r)^3$$

$$= \frac{4}{3} \pi \times (2)^3 \dots\dots\dots(i)$$

$$\text{Total volume of the 16 spheres} = 16 * \frac{4}{3} \pi \times (2)^3$$

$$\text{Volume of the rectangular box} = 16 * 8 * 8 \text{ cm}^3 \dots\dots\dots(ii)$$

Subtracting equation (ii) from (i) we get the volume of the liquid

$$\text{Volume of the liquid} = (1024 - 536.16) \text{ cm}^3 = 488 \text{ cm}^3$$

The volume of the liquid is 488 cm<sup>3</sup>

**Question 32: A vessel in the shape of a cuboids' contains some water. If 3 identical spheres are immersed in the water, the level of water is increased by 2 cm. If the area of the base of the cuboids is 160 cm<sup>2</sup> and its height is 12 cm. determine the radius of any of the spheres?**

**Solution:**

Given,

The area of the cuboids' = 160 cm<sup>2</sup>

Level of water in the vessel increased = 2 cm

$$\text{Volume of the vessel} = 160 * 2 \text{ cm}^2$$

$$= 320 \text{ cm}^2 \dots\dots\dots(i)$$

$$\text{Volume of each sphere} = \frac{4}{3} \pi \times (r)^3$$

$$\text{Total volume of 3 spheres} = 3 * \frac{4}{3} \pi \times (r)^3 \dots\dots\dots(ii)$$

Now equating equation (i) and (ii) we get

$$320 = 3 * \frac{4}{3} \pi \times (r)^3$$

R = 2.94 cm.

The radius of the sphere so obtained is 2.94 cm.

**Question 33:** Water in a canal 1.5 m wide and 6 m deep is flowing with a speed of 10 km / hr .How much area will it irrigate in 30 minutes if 8 cm of standing water is desired?

**Solution:**

Given

Water is flowing at a speed of = 10 km / hr

In 30 minutes length of the flowing standing water =  $10 \times 30 / 60 = 5 \text{ km} = 5000 \text{ m}$

Width of the canal = 1.5m

Depth of the canal = 6m

Volume of water in 30 minutes =  $5000 \times \text{width} \times \text{depth} = 45000 \text{ m}^3$

Irrigated area in 30 minutes if 8 cm of standing water is desired =  $45000 / 0.08 \text{ m}^2 = 562500 \text{ m}^2$

Irrigated area in 30 minutes is  $562500 \text{ m}^2$

**Question 34:** A tent of height 77 dm is in the form of a right angled circular cylinder of diameter 36 m and height 44 dm surmounted by a right circular cone. Find the cost of canvas at the rate of Rs.3.5 per  $\text{m}^2$ .

**Solution:**

Given

The height of the tent = 77 dm

Height of the cone = 44 dm

Height of the tent without the cone =  $(77 - 44) \text{ dm} = 33 \text{ dm}$

= 3.3 m

Diameter of the cylinder = 36 m

Radius of the cylinder =  $36 / 2 \text{ m} = 18 \text{ m}$

Let us assume the slant height of the cone be (l)

$$L^2 = r^2 + h^2$$

$$L^2 = (18)^2 + (3.3)^2$$



$$l = 18.3 \text{ m}$$

The slant height of the cone is 18.3 m.

Curved surface area of the cylinder =  $2\pi rh$

$$= 2 * \pi * 18 * 4.4 \text{ m}^2 \dots\dots\dots (i)$$

Curved surface area of the cone =  $\pi rh$

$$= \pi * 18 * 18.3 \text{ m}^2 \dots\dots\dots (ii)$$

Now adding equation (i) and (ii) we will get the value of the total surface area

$$\text{Total surface area} = 1532.46 \text{ m}^2$$

$$\text{Cost of canvas} = 1532.46 \text{ m}^2 * \text{Rs } 3.5 = \text{Rs } 5363.61$$

**Question 35:** The largest sphere is to be curved out of a right circular cylinder of radius 7 cm and height 14 cm. find the volume of the sphere.

**Solution:**

Given radius of the cylinder = 7 cm

Height of the cylinder = 14 cm

Largest sphere is curved out from the cylinder.

Thus the diameter of sphere = diameter of cylinder

$$\text{Diameter of the sphere} = 2 * 7 = 14 \text{ cm}$$

$$\text{Volume of the sphere} = \frac{4}{3} \pi r^3$$

$$= \frac{4}{3} \pi * 7^3$$

$$= 1436.75 \text{ cm}^3$$

Volume of the sphere is 1436.75 cm<sup>3</sup>

**Question 36:** A right angled triangle whose sides are 3cm, 4cm and 5 cm is revolved about the sides containing the right angle in two ways. Find the difference in volumes of the two cones so formed. Also find the curved surfaces?

**Solution:**

Given:

I>

Radius of the cone = 4 cm

Height of the cone = 3 cm

Slant height of the cone = 5 cm

$$\text{Volume of the cone} = \frac{1}{3} \times \pi \times r^2 \times h$$

$$= \frac{1}{3} \times \pi \times 4^2 \times 3$$

$$= 16\pi \text{ cm}^3$$

II>

Radius of the second cone = 3 cm

Height of the cone = 4 cm

Slant height of the cone = 5 cm

$$\text{Volume of the cone} = \frac{1}{3} \times \pi \times r^2 \times h$$

$$= \frac{1}{3} \times \pi \times 3^2 \times 4$$

$$= 12\pi \text{ cm}^3$$

Difference of the volumes of two cone =  $(16-12) \pi \text{ cm}^3$

$$= 4\pi \text{ cm}^3$$

Curved surface area of the first cone =  $\pi r_1 l_1$

$$= \pi \times 4 \times 5 \text{ cm}^2$$

$$= 20\pi \text{ cm}^2$$

Curved surface area of the second cone =  $\pi r_2 l_2$

$$= \pi \times 3 \times 5 \text{ cm}^2 = 15\pi \text{ cm}^2$$

**Question 37:** The volume of the hemisphere is  $2425\frac{1}{2}$ . find it's curved surface area.

**Solution:**

Given,

$$\text{Volume of the hemisphere} = \frac{2}{3} \pi r^3$$

$$\frac{2}{3} \pi r^3 = 48512 \frac{4851}{2}$$

$$r^3 = 4851(3)2(2)(\pi) \frac{4851(3)}{2(2)(\pi)}$$

$$r = (1193.18)^{1/3}$$

$$r = 10.5 \text{ cm}$$

$$\text{Curved surface area of the hemisphere} = 2\pi r^2$$

$$2 * \pi * (10.5)^2 = 693 \text{ cm}^2$$

The curved surface area of the hemisphere is 693 cm<sup>2</sup>.

**Question 38:** The difference between the outer and inner curved surface areas of a hollow right circular cylinder 14 cm long is 88 cm<sup>2</sup>. If the volume of metal used in making cylinder is 176 cm<sup>3</sup>. Find the outer and inner diameters of the cylinder?

**Solution:**

Given,

Height of the cylinder = 14 cm

Let the inner and outer radii of the hollow sphere be (r) and (R) respectively.

The difference between inner and outer curved surface area is 88 cm<sup>2</sup>

Curved surface area of the hollow sphere = 2π(R-r) h

$$88 = 2\pi(R-r) h$$

$$88 = 2\pi(R-r) 14$$

$$R-r = 1 \dots\dots\dots (i)$$

Volume of the hollow cylinder = π(R<sup>2</sup>-r<sup>2</sup>)h

$$176 = \pi(R^2-r^2)h$$

$$176 = \pi(R^2-r^2)15$$

From equation (i) substituting the values of equation. We get,

$$R+r = 4 \dots\dots\dots (ii)$$

Now solving both the equations we get,

$$2R = 5$$

$$R = 2.5 \text{ cm} \ \& \ r = 1.5 \text{ cm}$$

Inner radius of the hollow cylinder = 1.5 cm

Inner diameter of the hollow cylinder =  $2 * 1.5 \text{ cm} = 3 \text{ cm}$

Outer radius of the hollow cylinder = 2.5 cm

Outer diameter of the hollow cylinder = 5 cm

**Question 39:** The internal and external diameters of a hollow hemispherical vessel are 21 cm and 25.2 cm. The cost of painting  $1 \text{ cm}^2$  of the surface is 10 paise. Find the total cost to paint the vessel all over.

### Solution

Given,

Internal diameter of the hollow hemisphere = 21 cm

Internal radius of the hollow hemisphere =  $21/2 = 10.5 \text{ cm}$

External diameter of the hollow hemisphere = 25.2 cm

External radius of the hollow hemisphere =  $25.2/2 = 12.6 \text{ cm}$

Total area of the hollow hemisphere =  $2\pi R^2 + 2\pi r^2 + \pi(R^2 - r^2)$

$$= 2\pi(12.6^2) + 2\pi(10.5^2) + \pi(12.6^2 - 10.5^2)$$

$$= 997.51 + 692.72 + 152.39 \text{ cm}^2$$

$$= 1843.38 \text{ cm}^2$$

According to the question,

The cost of painting of  $1 \text{ cm}^2$  of the surface is = 10 p = Rs 0.10

Then the total cost of painting =  $1843.38 * 0.10$

$$= \text{Rs } 184.338$$

The total cost of painting all over the vessel is Rs. 184.338.

**Question 40:** The difference between outer and inner curved surface area of a hollow right circular cylinder is  $14 \text{ cm}$  long is  $88 \text{ cm}^2$ . If the volume of metal used in making cylinder is  $176 \text{ cm}^3$ . Find the outer and inner diameters of the cylinder?

**Solution**

Given,

Height of the hollow cylinder = 14 cm

Let the internal and external diameters of the hollow cylinder be r and R respectively.

Given that the difference between inner and outer curved surface = 88 cm<sup>3</sup>

Curved surface area of a hollow cylinder =  $2\pi(R-r) \times h$

$$88 = 2\pi(R-r) \times h$$

$$88 = 2 \times 3.1428 \times (R-r) \times 14$$

$$R-r = 1 \dots\dots\dots(i)$$

Volume of the hollow cylinder =  $\pi(R^2-r^2) \times h$

Volume of the hollow cylinder = 176 cm<sup>3</sup>

$$\pi(R^2-r^2) \times h = 176$$

$$R^2-r^2 = 4$$

$$R+r = 4 \dots\dots\dots(ii)$$

Now, solving eq I and ii we get,

$$R-r = 1$$

$$R+r = 4$$

.....

$$2R = 5$$

$$R = 2.5 \text{ cm}$$

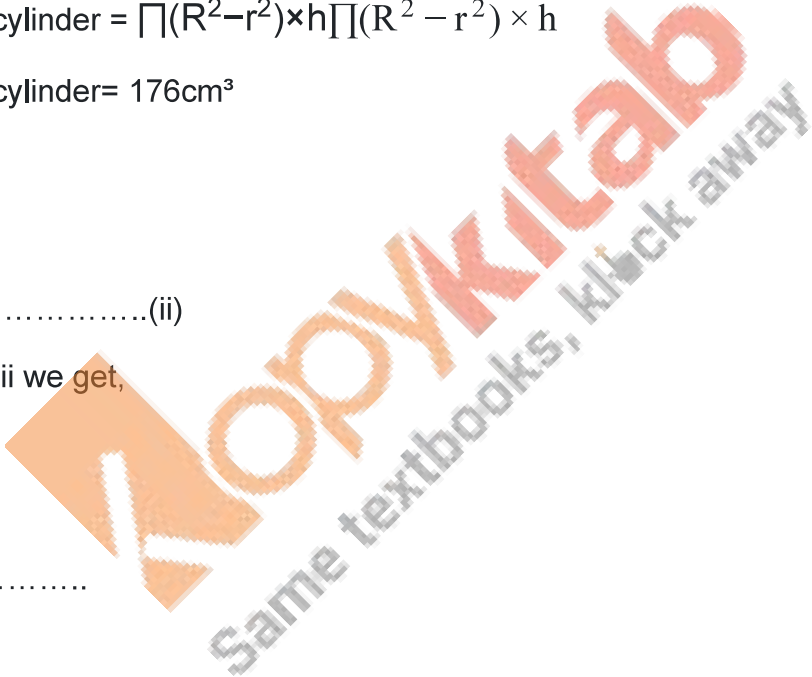
$$r = 1.5 \text{ cm}$$

The internal and external radii of the hollow cylinder are 1.5 cm and 2.5 cm respectively.

**Question 41: Prove that the surface area of a sphere is equal to the curved surface area of the circumscribed cylinder.**

**Solution:**

Let the radius of the sphere be (r)



Curved surface area of the sphere  $=4\pi r^2$  ..... (i)

$$S_1 = 4\pi r^2$$

Let the radius of the cylinder be (r)

Let the height of the cylinder be (2r)

Curved surface area of the cylinder  $= 2\pi rh$

$$S_2 = 2\pi r (2r)$$

$$=4\pi r^2 \text{ ..... (ii)}$$

From the above equations, it is proven that surface area of the sphere is equal to the curved surface area of the circumscribed cylinder.

