

Surface Area and volume of cuboid and cube-18.1

1.

Sol:

It is given that

Cuboid length = $80\text{cm} = L$

Breath = $40\text{cm} =$

Height = $20\text{cm} = h$

WKT,

$$\text{Total surface area} = 2[lb + bh + hl]$$

$$= 2[(80)(40) + 40(20) + 20(80)]$$

$$= 2[3200 + 800 + 1600]$$

$$= 2[5600]$$

$$= 11,200\text{m}^2$$

$$\text{Lateral surface area} = 2[l + b]h = 2[80 + 40]20$$

$$= 40(120)$$

$$= 4800\text{cm}^2$$

2.

Sol:

Cube of edge $a = 10\text{cm}$

WKT,

$$\text{Cube lateral surface area} = 4a^2$$

$$= 4 \times 10 \times 10 \quad [\because a = 10]$$

$$= 400\text{cm}^2$$

$$\text{Total surface area} = 6a^2$$

$$= 6 \times (10)^2$$

$$= 600\text{cm}^2$$

3.

Sol:

$$\text{Cube total surface area} = 6a^2$$

Where, a = edge of cube

$$\text{And, lateral surface area} = LSA = 4a^2$$

Where a = edge of cube

$$\therefore \text{Ratio of TSA and LSA} = \frac{6a^2}{4a^2} \text{ is } \frac{3}{2} \text{ is } 3:2$$

4.

Sol:

Given that Mary wants to paste the paper on the outer surface of the box; The quantity of the paper required would be equal to the surface area of the box which is of the shape of cuboid. The dimension of the box are

Length (l) = 80cm Breadth (b) = 40cm and height (h) = 20cm

The surface area of the box = $2[lb + bh + hl]$

$$= 2[80(40) + 40(20) + 20(80)]$$

$$= 2(5600) = 11,200\text{cm}^2$$

The area of the each sheet of paper = $40 \times 10\text{cm}^2$

$$= 1600\text{cm}^2$$

$$\therefore \text{Number of sheets required} = \frac{\text{Surface area of box}}{\text{area of one sheet of paper}}$$

$$= \frac{11,200}{1600} = 7$$

5.

Sol:

Total area to be washed = $lb + 2(l+b)h$

Where length (l) = 5m

Breadth (b) = 4m

Height (h) = 3m

$$\therefore \text{Total area to be white washed} = (5 \times 4) + 2(5+4) \times 3$$

$$= 20 + 54 = 74\text{m}^2$$

Now,

Cost of white washing 1m^2 is Rs 7.50

$$\therefore \text{Cost of white washing } 74\text{m}^2 \text{ is } \text{Rs}(74 \times 7.50)$$

$$= \text{Rs } 555$$

6.

Sol:

Length of new cuboid = $3a$

Breadth of cuboid = a

Height of new cuboid = a

The total surface area of new cuboid

$$\Rightarrow (TSA)_1 = 2[lb + bh + hl]$$

$$\Rightarrow (TSA)_1 = 2[3a \times a + a \times a + 3a \times a]$$

$$\Rightarrow (TSA)_1 = 14a^2$$

Total surface area of three cubes

$$\Rightarrow (TSA)_2 = 3 \times 6a^2 = 18a^2$$

$$\therefore \frac{(TSA)_1}{(TSA)_2} = \frac{14a^2}{18a^2} = \frac{7}{9}$$

\therefore Ratio is 7 : 9

7.

Sol:

Edge of cube = $4cm$

Volume of $4cm$ cube = $(4cm)^3 = 64cm^3$

Edge of cube = $1cm$

Volume of $1cm$ cube = $(1cm)^3 = 1cm^3$

$$\therefore \text{Total number of small cubes} = \frac{64cm^3}{1cm^3} = 64$$

\therefore Total surface area of $64cm$ all cubes

$$= 64 \times 6 \times (1cm)^2$$

$$= 384cm^2$$

8.

Sol:

Length of the hall = $18m$

Width of hall = $12m$

Now given,

Area of the floor and the flat roof = sum of the areas of four walls.

$$\Rightarrow 2lb = 2lh + 2bh$$

$$\Rightarrow lb = lh + bh$$

$$\Rightarrow h = \frac{lb}{l+b} = \frac{18 \times 12}{18+12} = \frac{216}{30}$$

$$= 7.2m.$$

9.

Sol:

Given that

Hameed is giving 5 outer faces of the tank covered with tiles he would need to know the surface area of the tank, to decide on the number of tiles required.

Edge of the cubic tank $= 1.5m = 150cm = a$

So, surface area of tank $= 5 \times 150 \times 150cm^2$

Area of each square tile $= \frac{\text{surface area of tank}}{\text{area of each tile}}$

$$= \frac{5 \times 150 \times 150}{25 \times 25} = 180$$

Cost of 1 dozen tiles i.e., cost of 12 tiles = Rs 360

Therefore, cost of 12 balls tiles = Rs 360

$$\therefore \text{cost of one tube} = \frac{360}{12} = \text{Rs } 30$$

$$\therefore \text{The cost of 180 tiles} = 180 \times \text{Rs } 30 \\ = \text{Rs } 5,400$$

10.

Sol:

Let d be the edge of the cube

$$\therefore \text{surface area of cube} = 6 \times a^2$$

$$\text{i.e., } S_1 = 6a^2$$

According to problem when edge increased by 50% then the new edge becomes

$$= a + \frac{50}{100} \times a$$

$$= \frac{3}{2}a$$

$$\text{New surface area becomes} = 6 \times \left(\frac{3}{2}a \right)^2$$

$$\text{i.e., } S_2 = 6 \times \frac{9}{4}a^2$$

$$S_2 = \frac{27}{2}a^2$$

$$\therefore \text{Increased in surface Area} = \frac{27}{2}a^2 - 6aa^2$$

$$= \frac{15}{2}a^2$$

$$\begin{aligned}\text{So, increase in surface area} &= \frac{\frac{15}{2}a^2}{6a^2} \times 100 \\ &= \frac{15}{12} \times 100 \\ &= 125\%\end{aligned}$$

11.

Sol:

Let the ratio be x

$$\therefore \text{length} = 2x$$

$$\text{Breath} = 3x$$

$$\text{Height} = 4x$$

$$\therefore \text{Total surface area} = 2[lb + bh + hl]$$

$$= 2[6x^2 + 12x^2 + 8x^2]$$

$$= 52x^2 m^2$$

When cost is at Rs 8 per m^2

$$\therefore \text{Total cost of } 52x^2 m^2 = Rs\ 8 \times 52x^2$$

$$= Rs\ 416x^2$$

And when the cost is at 95 per m^2

$$\therefore \text{Total cost of } 52x^2 m^2 = Rs\ 9.5 \times 52x^2$$

$$= Rs\ 499x^2$$

$$\therefore \text{Different in cost} = Rs\ 499x^2 - Rs\ 416x^2$$

$$\Rightarrow 1248 = 499x^2 - 416x^2$$

$$\Rightarrow 78x^2 = 1248$$

$$\Rightarrow x^2 = 16$$

$$\Rightarrow x = 4$$

12.

Sol:

Given length = $12m$, Breadth = $9m$ and Height = $4m$.

$$\text{Total surface area of tank} = 2(lb + bh + hl)$$

$$= 2[12 \times 9 + 9 \times 4 + 12 \times 4]$$

$$= 2[108 + 36 + 48]$$

$$= 384m^2$$

$$\text{Now length of iron sheet} = \frac{384}{\text{width of iron sheet}}$$

$$= \frac{384}{2} = 192m.$$

$$\begin{aligned}\text{Cost of iron sheet} &= \text{length of sheet} \times \text{cost rate} \\ &= 192 \times 5 = \text{Rs } 960.\end{aligned}$$

13.

Sol:

Given that

Shelter length = 4m

Breadth = 3m

Height = 2.5m

The tarpaulin will be required for to P and four sides of the shelter

Area of tarpaulin in required = $2(lb + bh + hl)$

$$= [2(4) \times 2.5 + (3 \times 2.5)] + 4 \times 3] m^2$$

$$= [2(10 + 7.5) + 12] m^2$$

$$= 47m^2 = 47m^2.$$

14.

Sol:

Given

Length = $1.48m = 148cm$.

Breath = $1.16m = 116cm$

Height = $8.3dm = 83cm$

Thickness of wood = 3cm

\therefore inner dimensions:

Length $(148 - 2 \times 3)cm = 142cm$

Breadth $(116 - 2 \times 3)cm = 110cm$

Height = $(83 - 3)cm = 80cm$.

Inner surface area = $2(l + b) + lb$

$$= 2[(142) + 110]80 + 142 \times 110cm^2$$

$$= 2(252)[80] + 142 \times 110cm^2 = 55,940cm^2$$

$$= 55940m^2$$

Hence, cost of painting inner surface area

$$= 5,5940 \times Rs \ 50$$

$$= Rs \ 279.70$$

15.

Sol:

Given that

Length of room = 12m.

Let a height of room be 'n' m.

$$\text{Area of 4 walls} = 2(l + b) \times h$$

According to question

$$\Rightarrow 2(l + b) \times h \times 1.35 = 340.20$$

$$\Rightarrow 2(12 + b) \times h \times 1.35 = 340.20$$

$$\Rightarrow (12 + b) \times h = \frac{170.10}{1.35} = 126 \quad \dots(1)$$

Also area of floor = $l \times b$

$$\therefore l \times b \times 0.85 = 91.80$$

$$\Rightarrow 12 \times b \times 0.85 = 91.80$$

$$\Rightarrow b = 9m \quad \dots(2)$$

Substituting $b = 9m$ in equation (1)

$$\Rightarrow (12 + 9) \times h = 126$$

$$\Rightarrow h = 6m$$

16.

Sol:

Given length of room = 12.5m

Breadth of room = 9m

Height of room = 7m

\therefore Total surface area of 4 walls

$$= 2(l + b) \times h$$

$$= 2(12.5 + 9) \times 7$$

$$= 301m^2$$

$$\text{Area of 2 doors} = 2[2.5 \times 1.2]$$

$$= 6m^2$$

Area to be painted on 4 walls

$$= 301 - (6 + 6)$$

$$= 301 - 12 = 289m^2$$

\therefore cost of painting = 289×3.50
Rs 1011.5.

17.

Sol:

Let the length be $4x$ and breadth be $3x$

Height = $5.5m$ [given]

Now it is given that cost of decorating 4 walls at the rate of Rs $6.601m^2$ is Rs 5082

\Rightarrow Area of four walls \times rate = total cost of painting

$$\Rightarrow 7x = \frac{5082}{5.5 \times 2.6 \times 2}$$

$$\Rightarrow 7x = 10$$

$$\Rightarrow x = 10$$

Length = $4x = 4 \times 10 = 40m$

Breadth = $3x = 3 \times 10 = 30m$

18.

Sol:

External length of book shelf = $85cm = l$

Breadth = $25cm$

Height = $110cm$.

External surface area of shelf while leaving front face of shelf

$$= (h + 2(lb + bh))$$

$$= [85 \times 110 + 2(85 \times 25 + 25 \times 110)] cm^2$$

$$= 19100 cm^2$$

$$\text{Area of front face} = (85 \times 110 - 75 \times 100 + 2(75 \times 5)) cm^2$$

$$= 1850 + 750 cm^2$$

$$= 2600 cm^2$$

$$\text{Area to be polished} = 19100 + 2600 cm^2$$

$$= 21700 cm^2$$

$$\text{Cost of polishing } 1 cm^2 \text{ area} = \text{Rs } 0.20$$

$$\text{Cost of polishing } 21700 cm^2 \text{ area} = \text{Rs } [21700 \times 0.20]$$

$$= \text{Rs } 4340$$

Now, length (l), breadth (b), height (h) of each row of book shelf is 75cm, 20cm and 30cm

$$= \left(\frac{110 - 20}{3} \right) \text{ respectively.}$$

Area to be painted in row $= 2(l + h)b + lh$

$$= [2(75 + 30) \times 20 + 75 \times 30] \text{ cm}^2$$

$$= (4200 + 2250) \text{ cm}^2$$

$$= 6450 \text{ cm}^2$$

Area to be painted in 3 rows $= (3 \times 6450) \text{ cm}^2$

$$= 19350 \text{ cm}^2$$

Cost of painting 1 cm^2 area $= \text{Rs } 0.10$.

Cost of painting 19350 area $= \text{Rs } (19350 \times 0.10) = \text{Rs } 1935$

Total expense required for polishing and painting the surface of the bookshelf

$$= \text{Rs } (4340 + 1935) = \text{Rs } 6275.$$

19.

Sol:

We know that

Total surface area of one brick $= 2(lb + bh + hl)$

$$= 2[22.5 \times 10 + 10 \times 7.5 + 22.5 \times 75] \text{ cm}^2$$

$$= 2[468.75] \text{ cm}^2$$

$$= 937.5 \text{ cm}^2$$

Let n number of bricks be painted by the container

Area of brick $= 937.50 \text{ cm}^2$

Area that can be painted in the container

$$= 93755 \text{ m}^2 = 93750 \text{ cm}^2$$

$$93750 = 937.5n$$

$$n = 100$$

Thus, 100 bricks can be painted out by the container.

Surface Area and volume of cuboid and cube – 18.2

1.

Sol:

Given length = $6m$

Breath = $5m$

Height = $4.5m$

Volume of the tank = $l \times b \times h = 6 \times 5 (4.5) = 135m^3$ It is given that

$1m^3 = 1000$ liters

$\therefore 135m^3 = (135 \times 1000)$ liters

$= 1,35,000$ liters

\therefore The tank can hold 1,35,000 liters of water

2.

Sol:

Given that

Length of vessel (l) = $10m$

Width of vessel (b) = $8m$

Let height of the cuboidal vessel be ' h '

Volume of vessel = $380m^3$

$\therefore l \times b \times h = 380$

$10 \times 8 \times h = 380$

$h = 4.75$

\therefore height of the vessel should be $4.75m$.

3.

Sol:

Given length of the cuboidal P it (l) = $8m$

Width (b) = $6m$

Depth (h) = $3m$

Volume of cuboid pit = $l \times b \times h = (8 \times 6 \times 3)m^3$

$= 144m^3$

Cost of digging $1m^3 = Rs\ 30$

Cost of digging $144m^3 = 144(Rs\ 30) = Rs\ 4320$.

4.

Sol:

Given that

Length = a

Breadth = b

Height = c

Volume (v) = $l \times b \times h$

= $a \times b \times c = abc$

Surface area = $2(lb + bh + hl)$

= $2(ab + bc + ac)$

Now, $\frac{2}{5} \left[\frac{1}{a} + \frac{1}{b} + \frac{1}{c} \right] = \frac{2}{2(ab + bc + ca)} \frac{[ab + bc + ca]}{abc}$

= $\frac{1}{abc} = \frac{1}{v}$

5.

Sol:

Let a, b, d be the length, breath and height of cuboid then,

$x = ab$

$y = bd,$

$z = da,$ and

$v = abd$ $[v = l \times b \times h]$

$\Rightarrow xyz = ab \times bc \times ca = (abc)^2$

And $v = abc$

$v^2 = (abc)^2$

$v^2 = xyz$

6.

Sol:

WKT, if x, y, z denote the areas of three adjacent faces of a cuboid

$\Rightarrow x = l \times b, y = b \times h, z = l \times h.$

Volume V is given by

$V = l \times b \times h.$

Now, $xyz = l \times b \times b \times h \times l \times h = V^2$

Here $x = 8$

$$y = 18$$

$$\text{And } z = 25$$

$$\therefore v^2 = 8 \times 18 \times 25 = 3600$$

$$\Rightarrow v = 60 \text{ cm}^3.$$

7.

Sol:

We have,

$$b = 2h \text{ and } b = \frac{1}{2}.$$

$$\Rightarrow \frac{l}{2} = 2h$$

$$\Rightarrow l = 4h$$

$$\Rightarrow l = 4h, b = 2h$$

Now,

$$\text{Volume} = 512 \text{ dm}^3$$

$$\Rightarrow 4h \times 2h \times h = 512$$

$$\Rightarrow h^3 = 64$$

$$\Rightarrow h = 4$$

$$\text{So, } l = 4 \times h = 16 \text{ dm}$$

$$b = 2 \times h = 8 \text{ dm}$$

$$\text{And } h = 4 \text{ dm}$$

8.

Sol:

$$\text{Radius of water flow} = 2 \text{ km per hour} = \left(\frac{2000}{60} \right) \text{ m / min}$$

$$= \left(\frac{100}{3} \right) \text{ m / min}$$

$$\text{Depth (h) of river} = 3 \text{ m}$$

$$\text{Width (b) of river} = 40 \text{ m}$$

$$\text{Volume of water followed in 1 min} = \frac{100}{3} \times 40 \times 3 \text{ m}^2 = 4000 \text{ m}^3$$

Thus, 1 minute $4000 \text{ m}^3 = 4000000$ liters of water will fall in sea.

9.

Sol:

Given that,

Water in the canal forms a cuboid of

width $(h) = 300d\ m = 3m$

height $= 12\ m = 1.2m$

length of cuboid is equal to the distance travelled in 30 min with the speed of 100 km per hour

$$\therefore \text{length of cuboid} = 100 \times \frac{30}{60} \text{ km} = 50000 \text{ meters}$$

So, volume of water to be used for irrigation $= 50000 \times 3 \times 1.2 m^3$

Water accumulated in the field forms a cuboid of base area equal to the area of the field

and height equal to $\frac{8}{100} \text{ meters}$

$$\therefore \text{Area of field} \times \frac{8}{100} = 50,000 \times 3 \times 1.2$$

$$\Rightarrow \text{Area of field} = \frac{50000 \times 3 \times 1.2 \times 100}{8}$$

$$= 2,250000 \text{ meters}$$

10.

Sol:

Let the length of each edge by of the new cube be a cm

Then,

$$a^3 = (6^3 + 8^3 + 10^3) \text{ cm}^3$$

$$\Rightarrow a^3 = 1728$$

$$\Rightarrow a = 12$$

$$\therefore \text{Volume of new cube} = a^3 = 1728 \text{ cm}^3$$

$$\begin{aligned} \text{Surface area of the new cube} &= 5a^2 = 6 \times 12^2 \text{ cm}^2 \\ &= 864 \text{ cm}^2. \end{aligned}$$

$$\text{Diagonals of the new cube} = \sqrt{3a} = 12\sqrt{3} \text{ cm}.$$

11.

Sol:

Given that

$$\text{Volume of cube} = 512 \text{ cm}^3$$

$$\Rightarrow \text{side}^3 = 512$$

$$\Rightarrow side^3 = 8^3$$

$$\Rightarrow side = 8cm$$

Dimensions of new cuboid formed

$$l = 8 + 8 = 16cm, b = 8cm, h = 8cm$$

$$\text{Surface area} = 2(lb + bh + hl)$$

$$= 2[16(8) + 8(8) + 16(8)] = 2[256 + 64]$$

$$= 640cm^2$$

\therefore Surface area is $640cm^2$.

12.

Sol:

Given that

$$\text{Volume of gold} = 0.5m^3$$

$$\text{Area of gold sheet} = 1 \text{ hectare} = 10000m^2$$

$$\therefore \text{Thickness of gold sheet} = \frac{\text{Volume of gold}}{\text{Area of gold sheet}}$$

$$= \frac{0.5m^3}{1 \text{ Hectare}}$$

$$= \frac{0.5m^3}{1000000m^2}$$

$$= \frac{5}{10000} \times 10m$$

$$= \frac{100}{20000}m$$

$$\text{Thickness of gold sheet} = \frac{1}{200}cm.$$

13.

Sol:

$$\text{Volume of large cube} = V_1 + V_2 + V_3$$

Let the edge of the third cube be x cm

$$123^3 = 6^3 + 8^3 + x^3 \quad [\text{Volume of cube} = side^3]$$

$$1728 = 216 + 512 + x^3$$

$$\Rightarrow x^3 = 1728 - 728 = 1000$$

$$\Rightarrow x = 10cm$$

\therefore Side of third side = $10cm$.

14.

Sol:

Given that

$$\text{Volume of cinema hall} = 100 \times 50 \times 18 m^3$$

$$\text{Volume air required by each person} = 150 m^3$$

Number of person who can sit in the hall

$$= \frac{\text{volume of cinema hall}}{\text{volume of air req each person}}$$

$$= \frac{100 \times 50 \times 18 m^3}{150 m^3} = 600 \quad [\because V = l \times b \times h]$$

\therefore number of person who can sit in the hall

= 600 members

15.

Sol:

Let the length of the block be 1cm

$$\text{Then, volume} = l \times 28 \times 5 \text{ cm}^3$$

$$\therefore \text{weight} = 140 \times 0.25 \text{ kg}$$

According to the question

$$\Rightarrow 112 = 140l \times 0.25$$

$$\Rightarrow l = \frac{112}{140 \times 0.25} = 3.2 \text{ cm}$$

16.

Sol:

Given external dimensions of cuboid are

$$l = 25 \text{ cm}, b = 18 \text{ cm}, h = 15 \text{ cm}.$$

$$\therefore \text{External volume} = l \times b \times h$$

$$= 25 \times 15 \times 15 \text{ cm}^3$$

$$= 6750 \text{ cm}^3.$$

$$\text{Internal volume} = l \times b \times h$$

$$= 21 \times 14 \times 11 \text{ cm}^3$$

$$= 3234 \text{ cm}^3$$

$$\therefore \text{Volume of liquid that can be placed} = 3234 \text{ cm}^3$$

Now, volume of wood = external volume – Internal volume

$$= 6750 - 3234$$

$$= 3516 \text{ cm}^3$$

17.

Sol:

Given internal dimensions are

$$l = 48 - 2 \times \text{thickness} = 48 - 3 = 45 \text{ cm}$$

$$b = 36 - 3 = 33 \text{ cm}$$

$$h = 30 - 3 = 27 \text{ cm}$$

$$\therefore \text{Internal volume} = 45 \times 33 \times 27 \text{ cm}^3$$

$$\text{Volume of brick} = 5 \times 3 \times 0.75 \text{ cm}^3$$

$$\text{Hence, number of bricks} = \frac{\text{Internal volume}}{\text{volume of 1 brick}}$$

$$= \frac{45 \times 33 \times 27}{6 \times 3 \times 0.37}$$

$$= \frac{38880}{13.5}$$

$$= 2970$$

\therefore 2970 bricks can be kept inside the box

18.

Sol:

Outer dimensions

$$l = 36 \text{ cm}$$

$$b = 25 \text{ cm}$$

$$h = 16.5 \text{ cm}$$

Inner dimensions

$$l = 36 - (2 \times 1.5) = 33 \text{ cm}$$

$$b = 25 - (3) = 22 \text{ cm}$$

$$h = 16.5 - 1.5 = 15 \text{ cm}$$

Volume of iron = outer volume – inner volume

$$= (36 \times 25 \times 16.5 - 33 \times 22 \times 15) \text{ cm}^3 = 3960 \text{ cm}^3$$

$$\text{Weight of iron} = 3960 \times 1.59 \text{ m} = 59400 \text{ gm} = 59.4 \text{ kg}$$

19.

Sol:

$$\text{Volume of cube} = s^3 = 9^3 = 729 \text{ cm}^3$$

$$\text{Area of base } l \times b = 15 \times 12 = 180 \text{ cm}^2$$

$$\begin{aligned}\text{Rise in water level} &= \frac{\text{Volume of cube}}{\text{Area of base of rectangular vessel}} \\ &= \frac{729}{180} = 4.05 \text{ cm}\end{aligned}$$

20.

Sol:

Let the length of each edge of the cube be x cm

Then,

Volume of cube = volume of water inside the tank + volume of water that over flowed

$$x^3 = (5 \times 5 \times 1) + 2 = 25 + 2$$

$$x^3 = 27$$

$$x = 3 \text{ cm}$$

Hence, volume of cube = 27 cm^3

And edge of cube = 3 cm .

21.

Sol:

Volume of earth dug out = $50 \times 40 \times 7 \text{ m}^3$

$$= 14000 \text{ m}^3$$

Let the height of the field rises by h meters

\therefore volume of field (cuboidal) = Volume of earth dug out

$$\Rightarrow 200 \times 150 \times h = 1400$$

$$\Rightarrow h = \frac{1400}{200 \times 150} = 0.47 \text{ m}$$

22.

Sol:

Let the level of the field be risen by h meters volume of the earth taken out from the pit

$$= 7.5 \times 6 \times 0.8 \text{ m}^3$$

Area of the field on which the earth taken out is to be spread = $18 \times 15 - 7.5 \times 6 = 225 \text{ m}^2$

Now, area of the field Yh = volume of the earth taken out from the pit

$$\Rightarrow 225 \times h = 7.5 \times 6 \times 0.8$$

$$\Rightarrow h = \frac{36}{225} = 0.16 \text{ m} = 16 \text{ cm}$$

23.

Sol:

Let the level of water be risen by h cm.

Then,

$$\text{Volume of water in the tank} = 8000 \times 2500 \times h \text{ cm}^3$$

$$\text{Area of cross-section of the pipe} = 25 \text{ cm}^2.$$

Water coming out of the pipe forms a cuboid of base area 25 cm^2 and length equal to the distance travelled in 45 minutes with the speed 16 km/hour.

$$\text{i.e., length} = 16000 \times 100 \times \frac{45}{60} \text{ cm}$$

\therefore Volume of water coming out of pipe in 45 minutes

$$= 25 \times 16000 \times 100 \left(\frac{45}{60} \right)$$

Now, volume of water in the tank = volume of water coming out of the pipe in 45 minutes

$$\Rightarrow 8000 \times 2500 \times h = 16000 \times 100 \times \frac{45}{60} \times 25$$

$$\Rightarrow h = \frac{16000 \times 100 \times 45 \times 25}{8000 \times 2500 \times 60} \text{ cm} = 1.5 \text{ cm}.$$

24.

Sol:

Given that,

$$\text{Flow of water} = 15 \text{ km/hr}$$

$$= 15000 \text{ m/hr}.$$

Volume of water coming out of the pipe in one hour

$$= \frac{20}{100} \times \frac{20}{100} \times 15000 = 600 \text{ m}^3$$

$$\text{Volume of the tank} = 80 \times 60 \times 6.5$$

$$= 31200 \text{ m}^3$$

\therefore Time taken to empty the tank

$$= \frac{\text{Volume of tank}}{\text{volume of water coming out of the pipe in one hour}}$$

$$= \frac{31200}{600}$$

$$= 52 \text{ hours}.$$

25.

Sol:

Given that

Length of the cuboidal tank (l) = $20m$

Breath of the cuboidal tank (b) = $15m$.

Height of the tank = $l \times b \times h = (20 \times 15 \times 6)m^3$

$$= 1800m^3$$

$$= 1800000 \text{ liters.}$$

Water consumed by people of village in one day

$$= 4000 \times 150 \text{ litres.}$$

$$= 600000 \text{ litres.}$$

Let water of this tank lasts for n days

Water consumed by all people of village in n days = capacity of tank

$$n \times 600000 = 1800000$$

$$n = 3$$

Thus, the water of tank will last for 3 days.

26.

Sol:

Volume of each cube = edge \times edge \times edge

$$= 3 \times 3 \times 3cm^3 = 27cm^3.$$

Number of cubes in the surface structure = 15

$$\therefore \text{Volume of the structure} = 27 \times 15cm^3$$

$$= 405cm^3.$$

27.

Sol:

Given go down length (l_1) = $40m$.

Breath (b_1) = $25m$.

Height (h_1) = $10m$.

Volume of go down = $l_1 \times b_1 \times h_1 = 40 \times 25 \times 10m^3$

$$= 10000m^3$$

Wood of wooden crate = $l_2 \times b_2 \times h_2$

$$= 1.5 \times 1.25 \times 0.25m^3 = 0.9375m^3$$

Let m wooden crates be stored in the go down volume of m wood crates = volume of go down

$$0.9375 \times n = 10000$$

$$n = \frac{10000}{0.9375} = 10,666.66,$$

Thus, 10,666.66 wooden crates can be stored in go down.

28.

Sol:

Given that

The wall with all its bricks makes up the space occupied by it we need to find the volume of the wall, which is nothing but cuboid.

Here, length = 10m = 1000cm

Thickness = 24cm

Height = 4m = 400cm

∴ The volume of the wall

= length × breadth × height

$$= 1000 \times 24 \times 400 \text{ cm}^3$$

Now, each brick is a cuboid with length = 24cm,

Breadth = 12cm and height = 8cm.

So, volume of each brick = length × breadth × height

$$= 24 \times 12 \times 8 \text{ cm}^3.$$

So, number of bricks required = $\frac{\text{Volume of the wall}}{\text{Volume of each brick}}$

$$= \frac{1000 \times 24 \times 400}{24 \times 12 \times 8}$$

$$= 4166.6.$$

So, the wall requires 167 bricks.