# Exercise 21.2

Question 1: Find the volume of a sphere whose radius is: (i) 2 cm (ii) 3.5 cm (iii) 10.5 cm.

## **Solution:** Volume of a sphere = $4/3\pi r^3$ Cubic Units Where, r = radius of a sphere

(i) Radius = 2 cm

Volume =  $4/3 \times 22/7 \times (2)^3$ 

= 33.52

Volume =  $33.52 \text{ cm}^{3}$ 

(ii) Radius = 3.5cm

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Therefore volume = 4/3 \times 22/7 \times (3.5)^3
= 179.666
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Volume = 179.666 cm<sup>3</sup>

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(iii) Radius = 10.5 cm
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Volume = 4/3 \times 22/7 \times (10.5)^3
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= 4851

Volume =  $4851 \text{ cm}^3$ 

Question 2: Find the volume of a sphere whose diameter is: (i) 14 cm (ii) 3.5 dm (iii) 2.1 m

### Solution:

Volume of a sphere =  $4/3\pi r^3$  Cubic Units Where, r = radius of a sphere

(i) diameter =14 cm So, radius = diameter/2 = 14/2 = 7cm

Volume =  $4/3 \times 22/7 \times (7)^3$ 

= 1437.33

Volume = 1437.33 cm<sup>3</sup>

(ii) diameter = 3.5 dm

So, radius = diameter/2 = 3.5/2 = 1.75 dm

Volume =  $4/3 \times 22/7 \times (1.75)^3$ 

= 22.46

Volume = 22.46 dm<sup>3</sup>

(iii) diameter = 2.1 m

So, radius = diameter/2 = 2.1/2 = 1.05 m

Volume = 4/3×22/7×(1.05)<sup>3</sup> = 4.851

Volume =  $4.851 \text{ m}^3$ 

#### Question 3: A hemispherical tank has the inner radius of 2.8 m. Find its capacity in liters.

#### Solution:

Radius of hemispherical tank = 2.8 m

Capacity of hemispherical tank =  $2/3 \pi r^3$ 

 $=2/3\times22/7\times(2.8)^3$  m<sup>3</sup>

= 45.997 m<sup>3</sup>

[Using 1m<sup>3</sup> = 1000 liters]

Therefore, capacity in litres = 45997 litres

Question 4: A hemispherical bowl is made of steel 0.25 cm thick. The inside radius of the bowl is 5 cm. Find the volume of steel used in making the bowl.

### Solution:

Inner radius of a hemispherical bowl = 5 cm

Outer radius of a hemispherical bowl = 5 cm + 0.25 cm = 5.25 cm

Volume of steel used = Outer volume - Inner volume

 $= 2/3 \times \pi \times ((5.25)^3 - (5)^3)$ 

 $= 2/3 \times 22/7 \times ((5.25)^3 - (5)^3)$ 

= 41.282

Volume of steel used is 41.282 cm<sup>3</sup>

Question 5: How many bullets can be made out of a cube of lead, whose edge measures 22 cm, each bullet being 2 cm in diameter?

### Solution:

Edge of a cube = 22 cm Diameter of bullet = 2 cm So, radius of bullet (r) = 1 cm

Volume of the cube =  $(side)^3 = (22)^3 \text{ cm}^3 = 10648 \text{ cm}^3$ 

And,

Volume of each bullet which will be spherical in shape =  $4/3\pi r^3$ 

 $= 4/3 \times 22/7 \times (1)^3$  cm<sup>3</sup>

 $= 4/3 \times 22/7 \text{ cm}^3$ 

= 8821 cm<sup>3</sup>

Number of bullets = (Volume of cube) / (Volume of bullet)

= 10648/8821

= 2541

Therefore, 2541 bullets can be made.

Question 6: A shopkeeper has one laddoo of radius 5 cm. With the same material, how many laddoos of radius 2.5 cm can be made?

### Solution:

Volume of laddoo having radius 5 cm (V1) =  $4/3 \times 22/7 \times (5)^3$ 

= 11000/21 cm<sup>3</sup>

Also, Volume of laddoo having radius 2.5 cm (V2) =  $4/3\pi r^3$ 

 $= 4/3 \times 22/7 \times (2.5)^3$  cm<sup>3</sup>

= 1375/21 cm<sup>3</sup>

Therefore,

Number of laddoos of radius 2.5 cm that can be made = V1/V2 = 11000/1375 = 8

Question 7: A spherical ball of lead 3 cm in diameter is melted and recast into three spherical balls. If the diameters of two balls be 3/2cm and 2 cm, find the diameter of the third ball.

### Solution:

Volume of lead ball with radius  $3/2 \text{ cm} = 4/3\pi r^3$ 

 $= 4/3 \times \pi \times (3/2)^3$ 

Let, Diameter of first ball (d1) = 3/2cm

Radius of first ball (r1) = 3/4 cm

Diameter of second ball (d2) = 2 cm

Radius of second ball  $(r_2) = 2/2 \text{ cm} = 1 \text{ cm}$ 

Diameter of third ball (d3) = d

Radius of third ball (r3) = d/2 cm

Now,

Volume of lead ball= 
$$\frac{4}{3} \times \pi \times \left(\frac{3}{4}\right)^3 + \frac{4}{3} \times \pi \times \left(1\right)^3 + \frac{4}{3} \times \pi \times \left(\frac{d}{2}\right)^3$$
  
 $\frac{4}{3} \times \pi \times \left(\frac{3}{2}\right)^3 = \frac{4}{3} \times \pi \times \left(\frac{3}{4}\right)^3 + \frac{4}{3} \times \pi \times \left(1\right)^3 + \frac{4}{3} \times \pi \times \left(\frac{d}{2}\right)^3$   
 $\frac{4}{3} \pi \left[ \left(\frac{3}{2}\right)^3 \right] = \frac{4}{3} \pi \left[ \left(\frac{3}{4}\right)^3 + \left(1\right)^3 + \left(\frac{d}{2}\right)^3 \right]$   
 $\frac{27}{8} = \frac{27}{64} + 1 + \frac{d^3}{8}$   
 $d^3 = 8 \left[ \frac{27}{8} - \frac{27}{64} - 1 \right]$   
 $\frac{d^3}{8} = \frac{125}{64}$   
 $\frac{d}{2} = \frac{5}{4}$   
 $d = \frac{10}{4}$   
 $d = 2.5$ 

So, diameter of third ball is 2.5 cm.

Question 8: A sphere of radius 5 cm is immersed in water filled in a cylinder, the level of water rises 5/3 cm. Find the radius of the cylinder.

#### Solution:

Radius of sphere = 5 cm (Given) Let 'r' be the radius of cylinder. We know, Volume of sphere =  $4/3\pi r^3$ 

By putting values, we get

 $= 4/3 \times \pi \times (5)^3$ 

Height (h) of water rises is 5/3 cm (Given)

Volume of water rises in cylinder =  $\pi r^2 h$ 

Therefore, Volume of water rises in cylinder = Volume of sphere

So,  $\pi r^2 h = 4/3\pi r^3$ 

 $\pi r^2 \times 5/3 = 4/3 \times \pi \times (5)^3$ 

or r<sup>2</sup> = 100

or r = 10

Therefore, radius of the cylinder is 10 cm.

Question 9: If the radius of a sphere is doubled, what is the ratio of the volume of the first sphere to that of the second sphere?

### Solution:

Let r be the radius of the first sphere then 2r be the radius of the second sphere.

Now,

Volume of first sphere =  $\frac{\frac{4}{3}\pi r^3}{\frac{4}{3}\pi (2r)^3} = \frac{1}{8}$ 

Ratio of volume of the first sphere to the second sphere is 1:8.

Question 10: A cone and a hemisphere have equal bases and equal volumes. Find the ratio of their heights.

### Solution:

Volume of the cone = Volume of the hemisphere (Given)

 $1/3\pi r^2 h = 2/3\pi r^3$ (Using respective formulas)

 $r^{2}h = 2r^{3}$ 

or h = 2r

Since, cone and a hemisphere have equal bases which implies they have the same radius. h/r = 2

or h : r = 2 : 1

Therefore, Ratio of their heights is 2:1

Question 11: A vessel in the form of a hemispherical bowl is full of water. Its contents are emptied in a right circular cylinder. The internal radii of the bowl and the cylinder are 3.5 cm and 7 cm respectively. Find the height to which the water will rise in the cylinder.

#### Solution:

Volume of water in the hemispherical bowl = Volume of water in the cylinder ... (Given)

Inner radius of the bowl ( $r_1$ ) = 3.5cm

Inner radius of cylinder  $(r_2) = 7$ cm

Volume of water in the hemispherical bowl = Volume of water in the cylinder

 $2/3\pi r_1^3 = \pi r_2^2 h$ [Using respective formulas]

Where h be the height to which water rises in the cylinder.

 $2/3\pi(3.5)^3 = \pi(7)^2h$ 

or h = 7/12

Therefore, 7/12 cm be the height to which water rises in the cylinder.

Question 12: A cylinder whose height is two thirds of its diameter, has the same volume as a sphere of radius 4 cm. Calculate the radius of the base of the cylinder.

Solution: Radius of a sphere (R)= 4 cm (Given) Height of the cylinder = 2/3 diameter (given) We know, Diameter = 2(Radius)

Let h be the height and r be the base radius of a cylinder, then

 $h = 2/3 \times (2r) = 4r/3$ 

Volume of the cylinder = Volume of the sphere

 $\pi r^{2}h = 4/3\pi R^{3}$ 

 $\pi \times r^2 \times (4r/3) = 4/3 \pi (4)^3$ 

 $(r)^3 = (4)^3$ 

or r = 4

Therefore, radius of the base of the cylinder is 4 cm.

Question 13: A vessel in the form of a hemispherical bowl is full of water. The contents are emptied into a cylinder. The internal radii of the bowl and cylinder are respectively 6 cm and 4 cm. Find the height of water in the cylinder.

#### Solution:

Radius of a bowl (R)= 6 cm (Given)

Radius of a cylinder (r) = 4 cm (given)

Let h be the height of a cylinder. Now, Volume of water in hemispherical bowl = Volume of cylinder

 $2/3 \pi R^3 = \pi r^2 h$ 

 $2/3 \pi (6)^3 = \pi (4)^2 h$ 

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or h = 9
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Therefore, height of water in the cylinder 9 cm.

Question 14: A cylindrical tub of radius 16 cm contains water to a depth of 30 cm. A spherical iron ball is dropped into the tub and thus level of water is raised by 9 cm. What is the radius of the ball?

### Solution:

Let r be the radius of the iron ball.

Radius of the cylinder (R) = 16 cm (Given)

A spherical iron ball is dropped into the cylinder and thus the level of water is raised by 9 cm. So, height (h) = 9 cm

From statement,

Volume of iron ball = Volume of water raised in the hub

 $4/3\pi r^{3} = \pi R^{2}h$ 

4/3 r<sup>3</sup> = (16)<sup>2</sup> × 9

or r<sup>3</sup> = 1728

or r = 12

Therefore, radius of the ball = 12cm.