Lines and Angles

Q1

Answer:

(i) The given angle measures 35°. Let the measure of its complement be x.

$$x + 35^{\circ} = 90^{\circ}$$

or
$$x = (90 - 35)^{\circ} = 55^{\circ}$$

Hence, the complement of the given angle will be 55°.

(ii) The given angle measures 47°.

Let the measure of its complement be x.

$$x + 47^{\circ} = 90^{\circ}$$

or
$$x = (90 - 47)^{\circ} = 43^{\circ}$$

Hence, the complement of the given angle will be 43°.

(iii) The given angle measures 60°.

$$x + 60^{\circ} = 90^{\circ}$$

or
$$x = (90 - 60)^{\circ} = 30^{\circ}$$

$$x + 73^{\circ} = 90^{\circ}$$

or
$$x = (90 - 73)^{\circ} = 17$$

angle will be 30°.

Lare of its complement be x. $x + 73^\circ = 90^\circ$ or $x = (90 - 73)^\circ = 17^\circ$ Hence, the complement of the given angle will be 17° .

Answer:

(i) The given angle measures 80°

Let the measure of its supplement be x.

$$x + 80^{\circ} = 180^{\circ}$$

or
$$x = (180 - 80)^{\circ} = 100^{\circ}$$

Hence, the complement of the given angle will be 100°.

(ii) The given angle measures 54°.

Let the measure of its supplement be x.

$$x + 54^{\circ} = 180^{\circ}$$

or
$$x = (180 - 54)^{\circ} = 126^{\circ}$$

Hence, the complement of the given angle will be 126°.

(iii) The given angle measures 105°.

Let the measure of its supplement be x.

$$x + 105^{\circ} = 180^{\circ}$$

or,
$$x = (180 - 105)^{\circ} = 75^{\circ}$$

Hence, the complement of the given angle will be 75°.

(iv)

The given angle measures 123°.

Let the measure of its supplement be x.

$$x + 123^{\circ} = 180^{\circ}$$

Q3

Answer:

Let the two supplementary angles be x° and (180 - x)°

Since it is given that the measure of the larger angle is 36° more than the smaller angle, let the larger angle be x°.

$$\therefore (180 - x)^{\circ} + 36^{\circ} = x^{\circ}$$

Larger angle = 108°

Smaller angle = (108 - 36

Q4

Answer:

Let the measure of the required angle be x

Since it is its own supplement

$$x + x = 180^{\circ}$$

$$\begin{array}{l} or\ 2x\ =\ 180\degree\\ or\ x\ =\ 90\degree \end{array}$$

Therefore, the required angle is 90°.

Q5

Answer:

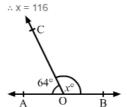
- (i) No. If both the angles are acute, i.e. less than 90°, they cannot be supplementary as their sum will always be less than 180°.
- (ii) No. If both the angles are obtuse, i.e. more than 90°, they cannot be supplementary as their sum will always be more than 180°.
- (iii) Yes. If both the angles are right, i.e. they both measure 90°, then they form a supplementary pair. 90° + 90° = 180°

Answer:

By linear pair property:

$$\angle AOC + \angle COB = 180^{\circ}$$

 $64^{\circ} + \angle COB = 180^{\circ}$
 $\angle COB = x^{\circ} = 180^{\circ} - 64^{\circ} = 116^{\circ}$



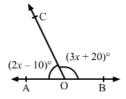
Q7

Answer:

By linear pair property:

$$\angle AOC + \angle BOC = 180^{\circ}$$

or $(2x-10)^{\circ} + (3x+20)^{\circ} = 180^{\circ}$ (given)
or $5x + 10 = 180$
or $5x = 170$
or $x = 34$
 $\therefore \angle AOC = (2x-10)^{\circ} = (2 \times 34 - 10)^{\circ} = 58^{\circ}$
 $\angle BOC = (3x+20)^{\circ} = (3 \times 34 + 20)^{\circ} = 122^{\circ}$



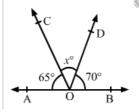
Q8

Answer:

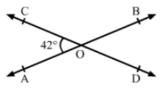
Since AOB is a straight line, we have:

$$\angle AOC + \angle BOD + \angle COD = 180^{\circ}$$

or $65^{\circ} + 70^{\circ} + x^{\circ} = 180^{\circ}$ (given
or $135^{\circ} + x^{\circ} = 180^{\circ}$
or $x^{\circ} = 45^{\circ}$
Thus, the value of x is 45



Answer:



AB and CD intersect at O and CD is a straight line.

(i)
$$\angle COA + \angle AOD = 180^{\circ}$$
 (linear pair)

$$42^{\circ} + \angle AOD = 180^{\circ}$$

$$\angle AOD = 138^{\circ}$$

(ii) \angle COA and \angle BOD are vertically opposite angles.

$$\therefore \angle COA = \angle BOD = 42^{\circ} [from (i)]$$

(iii) \angle COB and \angle AOD are vertically opposite angles.

$$\therefore \angle COB = \angle AOD = 138^{\circ} \text{ [from (i)]}$$

Q10

Answer:

(i) $\angle POS + \angle POR = 180^{\circ}$ (linear pair)

or
$$114^{\circ} + \angle POR = 180^{\circ}$$

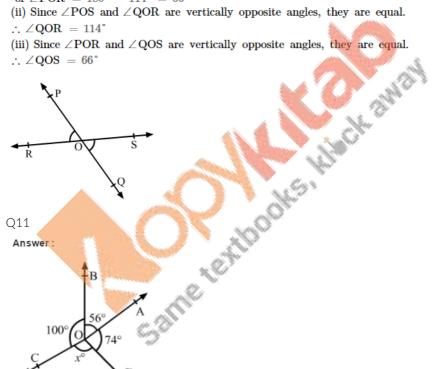
or
$$\angle POR = 180^{\circ} - 114^{\circ} = 66^{\circ}$$

(ii) Since ∠POS and ∠QOR are vertically opposite angles, they are equal.

$$\therefore \angle QOR = 114^{\circ}$$

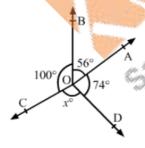
(iii) Since ∠POR and ∠QOS are vertically opposite angles, they are equal.

$$\therefore \angle QOS = 66^{\circ}$$



Q11

Answer:



Sum of all the angles around a point is 360°.

$$\therefore \angle AOB + \angle BOC + \angle COD + \angle DOA = 360^{\circ}$$

or
$$56^{\circ} + 100^{\circ} + x^{\circ} + 74^{\circ} = 360^{\circ}$$
 (given)

or
$$230^{\circ} + x^{\circ} = 360^{\circ}$$

or $x^{\circ} = 130^{\circ}$

or
$$x^{\circ} = 130^{\circ}$$

or
$$x = 130$$