We have,

$$5x + 7y = -2$$

$$4x + 6y = -3$$

The above system of equations can be written in the matrix form as

$$\begin{bmatrix} 5 & 7 \\ 4 & 6 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -2 \\ -3 \end{bmatrix}$$

or

$$AX = B$$

where
$$A = \begin{bmatrix} 5 & 7 \\ 4 & 6 \end{bmatrix} X = \begin{bmatrix} x \\ y \end{bmatrix}$$
 and $B = \begin{bmatrix} -2 \\ -3 \end{bmatrix}$

Now,
$$|A| = 30 - 28 = +2 \neq 0$$

So the above system has a unique solution, given by

$$X = A^{-1}B$$

Let C_{ii} be the co-factor of a_{ii} in A, then

$$C_{11} = 6$$

$$C_{12} = -4$$

$$C_{24} = -7$$

$$C_{--} = 5$$

Also,

The above system has a unique solution, given by
$$X = A^{-1}B$$

$$C_{ij} \text{ be the co-factor of } a_{ij} \text{ in } A, \text{ then } C_{11} = 6$$

$$C_{12} = -4$$

$$C_{21} = -7$$

$$C_{22} = 5$$

$$A^{-1} = \frac{1}{|A|} \text{ adj } A = \frac{1}{+2} \begin{bmatrix} 6 & -7 \\ -4 & 5 \end{bmatrix}$$

$$X = A^{-1}B$$

$$X = A^{-1}B$$

$$A^{-1} = \frac{1}{|A|} \operatorname{adj} A = \frac{1}{+2} \begin{bmatrix} 6 & -7 \\ -4 & 5 \end{bmatrix}$$

$$X = A^{-2}B$$

$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \frac{+1}{2} \begin{bmatrix} 6 & -7 \\ -4 & 5 \end{bmatrix} \begin{bmatrix} -2 \\ -3 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \frac{+1}{2} \begin{bmatrix} -12 & +21 \\ 8 & -15 \end{bmatrix} = \begin{bmatrix} \frac{9}{2} \\ \frac{-7}{2} \end{bmatrix}$$

Hence,
$$x = \frac{9}{2}$$
, $y = \frac{-7}{2}$

Solution of Simultaneous Linear Equations Ex 8.1 Q1(ii)

The above system can be written in matrix form as

$$\begin{bmatrix} 5 & 2 \\ 3 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 \\ 5 \end{bmatrix}$$

or
$$AX = B$$

Where,

$$A = \begin{bmatrix} 5 & 2 \\ 3 & 2 \end{bmatrix}, \quad X = \begin{bmatrix} x \\ y \end{bmatrix}, \quad B = \begin{bmatrix} 3 \\ 5 \end{bmatrix}$$

Now,
$$|A| = 10 - 6 = 4 \neq 0$$

So the above system has a unique solution, given by

$$X = A^{-1}B$$

$$C_{11} = 2$$

$$C_{12} = -3$$

$$C_{21} = -2$$

$$C_{22} = 5$$

Let
$$C_{ij}$$
 be the co-factor of a_{ij} in A , then
$$C_{11} = 2$$

$$C_{12} = -3$$

$$C_{21} = -2$$

$$C_{22} = 5$$
Also,
$$A dj A = \begin{bmatrix} 2 & -3 \\ -2 & 5 \end{bmatrix}^T = \begin{bmatrix} 2 & 2 \\ -3 & 5 \end{bmatrix}$$

$$\therefore A^{-1} = \frac{1}{|A|} a dj A = \frac{1}{4} \begin{bmatrix} 2 & -2 \\ -3 & 5 \end{bmatrix}$$
Now, $X = A^{-1}B$

$$= \frac{1}{4} \begin{bmatrix} 2 & -2 \\ 3 & 5 \end{bmatrix} \begin{bmatrix} 3 \\ 5 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} \text{ adj } A = \frac{1}{4} \begin{bmatrix} 2 & -2 \\ -3 & 5 \end{bmatrix}$$

Now,
$$X = A^{-1}B$$

$$= \frac{1}{4} \begin{bmatrix} 2 & -2 \\ -3 & 5 \end{bmatrix} \begin{bmatrix} 3 \\ 5 \end{bmatrix}$$
$$= \frac{1}{4} \begin{bmatrix} -4 \\ 16 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -1 \\ 4 \end{bmatrix}$$

Hence,
$$x = -1$$

$$y = 4$$

Solution of Simultaneous Linear Equations Ex 8.1 Q1(iii)

The above system can be written in matrix form as:

$$\begin{bmatrix} 3 & 4 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 5 \\ -3 \end{bmatrix}$$

or
$$AX = B$$

Where,

$$A = \begin{bmatrix} 3 & 4 \\ 1 & -1 \end{bmatrix}, \quad X = \begin{bmatrix} x \\ y \end{bmatrix}, \quad B = \begin{bmatrix} 5 \\ -3 \end{bmatrix}$$

Now,
$$|A| = -7 \neq 0$$

So the above system has a unique solution, given by

$$X = A^{-1}B$$

Let C_{ij} be the co-factor of a_{ij} in A, then

$$C_{11} = -1$$

$$C_{12} = -1$$

$$C_{ox} = -4$$

$$C_{22} = 3$$

Now,

$$Adj A = \begin{bmatrix} -1 & -1 \\ -4 & 3 \end{bmatrix}^T = \begin{bmatrix} -1 & -4 \\ -1 & 3 \end{bmatrix}$$

the above system has a unique solution, given by
$$X = A^{-1}B$$

$$C_{ij} \text{ be the co-factor of } a_{ij} \text{ in } A, \text{ then } C_{11} = -1$$

$$C_{12} = -1$$

$$C_{21} = -4$$

$$C_{22} = 3$$

$$W,$$

$$Adj A = \begin{bmatrix} -1 & -1 \\ -4 & 3 \end{bmatrix}^T = \begin{bmatrix} -1 & -4 \\ -1 & 3 \end{bmatrix}$$

$$\therefore A^{-1} = \frac{1}{|A|} \text{ adj } A = \frac{1}{-7} \begin{bmatrix} -1 & -4 \\ -1 & 3 \end{bmatrix}$$

$$W, \quad X = A^{-1}B$$

$$\Rightarrow \begin{bmatrix} X \\ \end{bmatrix} = \frac{-1}{-1} \begin{bmatrix} -1 & -4 \\ -1 \end{bmatrix} \begin{bmatrix} 5 \\ \end{bmatrix}$$

Now,
$$X = A^{-1}B$$

$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \frac{-1}{7} \begin{bmatrix} -1 & -4 \\ -1 & 3 \end{bmatrix} \begin{bmatrix} 5 \\ -3 \end{bmatrix}$$
$$= \frac{-1}{7} \begin{bmatrix} 7 \\ -14 \end{bmatrix}$$
$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$$

Hence,
$$x = -1$$

$$y = 2$$

Solution of Simultaneous Linear Equations Ex 8.1 Q1(iv)

The above system can be written in matrix form as:

$$\begin{bmatrix} 3 & 1 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 19 \\ 23 \end{bmatrix}$$

AX = Bor

Where,

$$A = \begin{bmatrix} 3 & 1 \\ 3 & -1 \end{bmatrix}, \quad X = \begin{bmatrix} X \\ y \end{bmatrix}, \quad B = \begin{bmatrix} 19 \\ 23 \end{bmatrix}$$

Now, $|A| = -6 \neq 0$

So, the above system has a unique solution, given by

$$X = A^{-1}B$$

Let C_{ii} be the co-factor of a_{ij} in A, then

$$C_{11} = -1$$

$$C_{12} = -3$$

$$C_{22} = 3$$

Now,

the above system has a unique solution, given by
$$X = A^{-1}B$$

$$C_{ij} \text{ be the co-factor of } a_{ij} \text{ in } A \text{, then }$$

$$C_{11} = -1$$

$$C_{12} = -3$$

$$C_{21} = -1$$

$$C_{22} = 3$$

$$N,$$

$$A \text{ dj } A = \begin{bmatrix} -1 & -3 \\ -1 & 3 \end{bmatrix}^T = \begin{bmatrix} -1 & -1 \\ -3 & 3 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} \text{ adj } A = \frac{1}{-6} \begin{bmatrix} -1 & -1 \\ -3 & 3 \end{bmatrix}$$

$$N, \quad X = A^{-1}B$$

$$A = \begin{bmatrix} X \\ -1 \end{bmatrix} = -1 \begin{bmatrix} -1 & -1 \\ -1 \end{bmatrix} \begin{bmatrix} 19 \\ -1 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} \operatorname{adj} A = \frac{1}{-6} \begin{bmatrix} -1 & -1 \\ -3 & 3 \end{bmatrix}$$

Now, $X = A^{-1}B$

$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \frac{-1}{6} \begin{bmatrix} -1 & -1 \\ -3 & 3 \end{bmatrix} \begin{bmatrix} 19 \\ 23 \end{bmatrix}$$
$$= \frac{-1}{6} \begin{bmatrix} -19 & -23 \\ -57 & +69 \end{bmatrix}$$
$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 7 \\ -2 \end{bmatrix}$$

Hence,
$$x = 7$$

$$y = -2$$

Solution of Simultaneous Linear Equations Ex 8.1 Q1(v)

The above system can be written in matrix form as:

$$\begin{bmatrix} 3 & 7 \\ 1 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 \\ -1 \end{bmatrix}$$

or
$$AX = B$$

where
$$A = \begin{bmatrix} 3 & 7 \\ 1 & 2 \end{bmatrix}$$
, $X = \begin{bmatrix} x \\ y \end{bmatrix}$ and $B = \begin{bmatrix} 4 \\ -1 \end{bmatrix}$

Now,

$$|A| = -1 \neq 0$$

 $Adj A = \begin{bmatrix} 2 & -1 \\ -7 & 3 \end{bmatrix}^T = \begin{bmatrix} 2 & -7 \\ -1 & 3 \end{bmatrix}$ $A^{-1} = \frac{1}{|A|} \cdot adj A = \frac{1}{(-1)} \begin{bmatrix} 2 & 17 \\ -1 & 3 \end{bmatrix}$ $= A^{-1}B$ So the above system has a unique solution, given by

$$X = A^{-1}B$$

Now, let
$$C_{ij}$$
 be the co-factor of a_{ij} in A

$$C_{11} = 2$$

$$Adj A = \begin{bmatrix} 2 & -1 \end{bmatrix}^T = \begin{bmatrix} 2 & -7 \\ -7 & 3 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} \cdot \text{adj } A = \frac{1}{(-1)} \begin{bmatrix} 2 & 7 \\ -1 & 3 \end{bmatrix}$$

Now,
$$X = A^{-1}B$$

$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{-1} \begin{bmatrix} 2 & -7 \\ -1 & 3 \end{bmatrix} \begin{bmatrix} 4 \\ -1 \end{bmatrix}$$
$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{-1} \begin{bmatrix} 15 \\ -7 \end{bmatrix} = \begin{bmatrix} -15 \\ 7 \end{bmatrix}$$

Hence,
$$x = -15$$

 $y = 7$

Solution of Simultaneous Linear Equations Ex 8.1 Q1(vi)

The given system can be written in matrix form as:

$$\begin{bmatrix} 3 & 1 \\ 5 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 7 \\ 12 \end{bmatrix}$$

or
$$AX = B$$

Where,

$$A = \begin{bmatrix} 3 & 1 \\ 5 & 3 \end{bmatrix}, X = \begin{bmatrix} x \\ y \end{bmatrix}, B = \begin{bmatrix} 7 \\ 12 \end{bmatrix}$$

Since, $|A| = 4 \neq 0$, the above system has a unique solution, given by

$$X = A^{-1}B$$

Let C_{ii} be the co-factor of a_{ii} in A

$$C_{11} = 3$$

 $C_{12} = -5$

$$C_{21} = -1$$

 $C_{22} = 3$

Solution be the co-factor of
$$a_{ij}$$
 in A

$$C_{11} = 3$$

$$C_{12} = -5$$

$$C_{21} = -1$$

$$C_{22} = 3$$

$$adj A = \begin{bmatrix} 3 & -5 \\ -1 & 3 \end{bmatrix}^{7} = \begin{bmatrix} 3 & -1 \\ -5 & 3 \end{bmatrix}$$

$$\therefore A^{-1} = \frac{1}{|A|} adj A = \frac{1}{4} \begin{bmatrix} 3 & -1 \\ -5 & 3 \end{bmatrix} \begin{bmatrix} 7 \\ 12 \end{bmatrix}$$

$$X = A^{-1}B$$

$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{4} \begin{bmatrix} 3 & -1 \\ -5 & 3 \end{bmatrix} \begin{bmatrix} 7 \\ 12 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} \operatorname{adj} A = \frac{1}{4} \begin{bmatrix} -5 & 3 \end{bmatrix}$$

Now.

$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{4} \begin{bmatrix} 3 & -1 \\ -5 & 3 \end{bmatrix} \begin{bmatrix} 7 \\ 12 \end{bmatrix}$$
$$\Rightarrow \begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{4} \begin{bmatrix} 9 \\ 1 \end{bmatrix} = \begin{bmatrix} \frac{9}{4} \\ \frac{1}{4} \end{bmatrix}$$

Hence,
$$x = \frac{9}{4}$$

$$y = \frac{1}{4}$$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(i)

The given system can be written in matrix form as:

$$\begin{bmatrix} 1 & 1 & -1 \\ 2 & 3 & 1 \\ 3 & -1 & -7 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ 10 \\ 1 \end{bmatrix}$$

or AX = B

Where,

$$A = \begin{bmatrix} 1 & 1 & -1 \\ 2 & 3 & 1 \\ 3 & -1 & -7 \end{bmatrix}, \quad X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}, \quad B = \begin{bmatrix} 3 \\ 10 \\ 1 \end{bmatrix}$$

Now,
$$|A| = 1 \begin{bmatrix} 3 & 1 \\ -1 & -7 \end{bmatrix} - 1 \begin{bmatrix} 2 & 1 \\ 3 & -7 \end{bmatrix} - 1 \begin{bmatrix} 2 & 3 \\ 3 & -1 \end{bmatrix}$$

= $(-20) - 1(-17) - 1(-11)$
= $-20 + 17 + 11 = 8 \neq 0$

So, the above system has a unique solution, given by

$$X = A^{-1}B$$

Let C_{ij} be the co-factor of a_{ij} in A

$$C_{11} = -20$$
 $C_{21} = 8$ $C_{31} = 4$ $C_{12} = -(-17) = 17$ $C_{22} = -4$ $C_{32} = -3$ $C_{13} = -11$ $C_{23} = -(-4) = 4$ $C_{33} = 1$

$$adj A = \begin{bmatrix} -20 & 17 & -11 \\ 8 & -4 & 4 \\ 4 & -3 & 1 \end{bmatrix}^{7} = \begin{bmatrix} -20 & 8 & 4 \\ 17 & -4 & -3 \\ -11 & 4 & 1 \end{bmatrix}$$

Now,
$$X = A^{-1}B = \frac{1}{8} \begin{bmatrix} -20 & 8 & 4 \\ 17 & -4 & -3 \\ -11 & 4 & 1 \end{bmatrix} \begin{bmatrix} 3 \\ 10 \\ 1 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{8} \begin{bmatrix} 24 \\ 8 \\ 8 \end{bmatrix} = \begin{bmatrix} 3 \\ 1 \\ 1 \end{bmatrix}$$

Hence,
$$x = 3$$

$$y = 1$$

$$z = 1$$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(ii)

The above system can be written in matrix form as:

$$\begin{bmatrix} 1 & 1 & 1 \\ 2 & -1 & 1 \\ 2 & 1 & -3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ -1 \\ -9 \end{bmatrix}$$

AX = Bor

Where,

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 2 & -1 & 1 \\ 2 & 1 & -3 \end{bmatrix}, \quad X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}, \quad B = \begin{bmatrix} 3 \\ -1 \\ -9 \end{bmatrix}$$

Since, $|A| = 14 \neq 0$, the above system has a unique solution, given by $X = A^{-1}B$

Let C_{ij} be the co-factor of a_{ij} in A

$$C_{11} = 2$$

$$C_{21} = 4$$

$$C_{\alpha i} = 2$$

$$C_{12} = 1$$

$$C_{22} = -5$$

$$C_{\infty} = 1$$

$$C_{12} = 0$$

$$C_{23} = 1$$

$$C_{22} = -3$$

Let
$$C_{ij}$$
 be the co-factor of a_{ij} in A

$$C_{11} = 2 C_{21} = 4 C_{31} = 2$$

$$C_{12} = 8 C_{22} = -5 C_{32} = 1$$

$$C_{13} = 4 C_{23} = 1 C_{33} = -3$$

$$Adj A = \begin{bmatrix} 2 & 8 & 4 \\ 4 & -5 & 1 \\ 2 & 1 & -3 \end{bmatrix}^T = \begin{bmatrix} 2 & 4 & 2 \\ 8 & -5 & 1 \\ 4 & 1 & -3 \end{bmatrix}$$

$$Now, X = A^{-1}B = \frac{1}{|A|} \times Adj A \times B$$

$$= \frac{1}{14} \begin{bmatrix} 2 & 4 & 2 \\ 8 & -5 & 1 \\ 4 & 1 & -3 \end{bmatrix} \begin{bmatrix} 3 \\ -1 \\ 4 & 1 & -3 \end{bmatrix}$$

$$= \frac{1}{14} \begin{bmatrix} -16 \\ 20 \\ 38 \end{bmatrix}$$

Now,
$$X = A^{-1}B = \frac{1}{|A|} \times Adj A \times B$$

$$= \frac{1}{14} \begin{bmatrix} 2 & 4 & 2 \\ 8 & -5 & 1 \\ 4 & 1 & -3 \end{bmatrix} \begin{bmatrix} 3 \\ -1 \\ -9 \end{bmatrix}$$

$$= \frac{1}{14} \begin{bmatrix} -16 \\ 20 \\ 38 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} \frac{-8}{7} \\ \frac{10}{7} \\ \frac{19}{7} \end{bmatrix}$$

Hence,
$$x = \frac{-8}{7}$$
, $y = \frac{10}{7}$, $z = \frac{19}{7}$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(iii)

The above system can be written in matrix form as:

$$\begin{bmatrix} 6 & -12 & 25 \\ 4 & 15 & -20 \\ 2 & 18 & 15 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 4 \\ 3 \\ 10 \end{bmatrix}$$

or
$$AX = B$$

Where,

$$A = \begin{bmatrix} 6 & -12 & 25 \\ 4 & 15 & -20 \\ 2 & 18 & 15 \end{bmatrix}, \quad X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}, \quad B = \begin{bmatrix} 4 \\ 3 \\ 10 \end{bmatrix}$$

Now,

$$|A| = 6 (225 + 360) + 12(60 + 40) + 25(72 - 30)$$

$$= 6 (585) + 1200 + 25(42)$$

$$= 3510 + 1200 + 1050$$

$$= 5760 \neq 0$$

So, the above system will have a unique solution, given by

$$X = A^{-1}B$$

$$C_{11} = 585$$
 $C_{21} = -(-180 - 450) = 630$ $C_{31} = -135$
 $C_{12} = -100$ $C_{22} = 40$ $C_{32} = 220$
 $C_{13} = 42$ $C_{23} = -132$ $C_{33} = 138$

$$X = A^{-1}B = \frac{1}{|A|} (AdjA) \times B = \frac{1}{5760} \begin{bmatrix} 585 & 630 & -135 \\ -100 & 40 & 220 \\ 42 & -132 & 138 \end{bmatrix} \begin{bmatrix} 2880 \\ 1920 \\ 1152 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{5760} \begin{bmatrix} 2880 \\ 1920 \\ 1152 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} \frac{1}{2} \\ \frac{1}{3} \\ \frac{1}{5} \end{bmatrix}$$

Hence,
$$x = \frac{1}{2}$$

 $y = \frac{1}{3}$
 $z = \frac{1}{5}$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(iv)

The above system can be written as

$$\begin{bmatrix} 3 & 4 & 7 \\ 2 & -1 & 3 \\ 1 & 2 & -3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 14 \\ 4 \\ 0 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 3(-3) - 4(-9) + 7(5)$$

= -9 + 36 + 35
= 62 \neq 0

So, the above system will have a unique solution, given by

$$X = A^{-1}B$$

Now,
$$C_{11} = -3$$
 $C_{21} = 26$ $C_{31} = 19$ $C_{12} = 9$ $C_{22} = -16$ $C_{32} = 5$ $C_{13} = 5$ $C_{23} = -2$ $C_{33} = -11$

$$adj A = \begin{bmatrix} -3 & 26 & 19 \\ 9 & -16 & 5 \\ 5 & -2 & -11 \end{bmatrix}$$

$$X = A^{-1}B = \frac{1}{|A|} (Adj A)B$$

$$= \frac{1}{62} \begin{bmatrix} -3 & 26 & 19 \\ 9 & -16 & 5 \\ 5 & -2 & -11 \end{bmatrix} \begin{bmatrix} 14 \\ 4 \\ 0 \end{bmatrix}$$

$$= \frac{1}{62} \begin{bmatrix} -42 + 104 + 0 \\ 126 - 64 + 0 \\ 70 - 8 + 0 \end{bmatrix} = \frac{1}{62} \begin{bmatrix} 62 \\ 62 \\ 62 \end{bmatrix}$$

$$\begin{vmatrix} x \\ y \\ z \end{vmatrix} = \begin{vmatrix} 1 \\ 1 \\ 1 \end{vmatrix}$$

Hence,
$$x = 1, y = 1, z = 1$$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(v)

The above system can be written as

$$\begin{bmatrix} 2 & 6 & 0 \\ 3 & 0 & -1 \\ 2 & -1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ -8 \\ -3 \end{bmatrix}$$

Or
$$AX = B$$

$$|A| = 2(-1) - 6(5) + 0(-3) = -32 \neq 0$$

So, the above system has a unique solution, given by $X = A^{-1}B$

Let
$$C_{ii}$$
 be the co-factor of a_{ii} in A

Let
$$C_{ij}$$
 be the co-factor of a_{ij} in A

Let
$$C_{ij}$$
 be the co-factor of a_{ij} in A

$$C_{11} = -1 \qquad C_{21} = -6$$

$$C_{11} = -1$$
 $C_{21} = -6$
 $C_{12} = -5$ $C_{23} = 2$

$$C_{11} = -1$$
 $C_{21} = -6$
 $C_{12} = -5$ $C_{23} = 2$

$$C_{11} = -1$$
 $C_{21} = -6$
 $C_{12} = -5$ $C_{22} = 2$

$$C_{11} = -1$$
 $C_{21} = -6$

$$C_{11} = -1$$
 $C_{21} = -6$

$$C_{11} = -1$$
 $C_{21} = -6$ C_{31}

$$C_{22} = 2$$
 $C_{32} = 2$

$$C_{23} = 14 \qquad C_{33} = -18$$

$$C_{23} = 14$$
 $C_{33} = -18$

$$\begin{vmatrix} 1 & -5 & -3 \\ 5 & 2 & 14 \end{vmatrix} = \begin{vmatrix} -5 & 2 & 2 \end{vmatrix}$$

th
$$C_{ij}$$
 be the co-factor of a_{ij} in A

$$C_{11} = -1 \qquad C_{21} = -6 \qquad C_{31} = -6$$

$$C_{12} = -5 \qquad C_{22} = 2 \qquad C_{32} = 2$$

$$C_{13} = -3 \qquad C_{23} = 14 \qquad C_{33} = -18$$

$$adjA = \begin{bmatrix} -1 & -5 & -3 \\ -6 & 2 & 14 \\ -6 & 2 & -18 \end{bmatrix}^T = \begin{bmatrix} -1 & -6 & -6 \\ -5 & 2 & 2 \\ -3 & 14 & -18 \end{bmatrix}$$
ow,
$$X = A^{-1}B = \frac{1}{|A|}(AdjA) \times B$$

$$X = A^{-1}B = \frac{1}{|A|} (AdjA) \times B$$

$$= \frac{1}{-32} \begin{bmatrix} -1 & -6 & -6 \\ -5 & 2 & 2 \\ -3 & 14 & -18 \end{bmatrix} \begin{bmatrix} 2 \\ -8 \\ -3 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{-32} \begin{bmatrix} 64 \\ -32 \end{bmatrix} = \begin{bmatrix} -2 \\ 1 \\ 2 \end{bmatrix}$$

Hence,
$$x = -2$$
, $y = 1$, $z = 2$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(v)

Let
$$\frac{1}{x} = u, \frac{1}{y} = v, \frac{1}{z} = w$$

Let
$$\frac{z}{x} = \alpha, \frac{z}{y} = \sqrt{z} = \sqrt{z}$$

$$2u - 3v + 3w = 10$$

 $u + v + w = 10$
 $3u - v + 2w = 13$

Which can be written as

$$\begin{bmatrix} 2 & -3 & 3 \\ 1 & 1 & 1 \\ 3 & -1 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 10 \\ 10 \\ 13 \end{bmatrix}$$

$$|A| = 2(3) + 3(-1) + 3(-4)$$

= 6 - 3 - 12 = -9 \neq 0

Hence, the system has a unique solution, given by

$$X = A^{-1} \times B$$

$$C_{11} = 3$$
 $C_{21} = 3$ $C_{31} = -6$

$$C_{11} = 3$$
 $C_{21} = 3$ $C_{31} = -6$
 $C_{12} = 1$ $C_{22} = -5$ $C_{32} = 1$
 $C_{13} = -4$ $C_{23} = -7$ $C_{33} = 5$

$$X = \frac{1}{|A|} (\operatorname{Adj} A) \times (B)$$

$$\begin{bmatrix} 3 & 3 & -6 \\ 1 & 5 & 1 \end{bmatrix} \begin{bmatrix} 10 \\ 10 & 5 \end{bmatrix}$$

$$= \frac{1}{-9} \begin{bmatrix} 3 & 3 & -6 \\ 1 & -5 & 1 \\ -4 & -7 & 5 \end{bmatrix} \begin{bmatrix} 10 \\ 10 \\ 13 \end{bmatrix}$$
$$= \frac{-1}{9} \begin{bmatrix} 30 + 30 - 78 \\ 10 - 50 + 13 \\ -40 - 70 + 65 \end{bmatrix}$$

$$\begin{bmatrix} u \\ v \\ w \end{bmatrix} = \frac{-1}{9} \begin{bmatrix} -18 \\ -27 \\ -45 \end{bmatrix} = \begin{bmatrix} 2 \\ 3 \\ 5 \end{bmatrix}$$

Hence,
$$x = \frac{1}{2}$$
, $y = \frac{1}{3}$, $z = \frac{1}{5}$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(vi)

$$\begin{bmatrix} 5 & 3 & 1 \\ 2 & 1 & 3 \\ 1 & 2 & 4 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 16 \\ 19 \\ 25 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = \begin{bmatrix} 5 & 3 & 1 \\ 2 & 1 & 3 \\ 1 & 2 & 4 \end{bmatrix}$$
$$= 5(-2) - 3(5) + 1(3)$$

$$X = A^{-1} \times B$$

it has a unique solution, given by
$$X = A^{-1} \times B$$

$$C_{11} = -2 \qquad C_{21} = -10 \qquad C_{31} = 8$$

$$C_{12} = -5 \qquad C_{22} = 19 \qquad C_{32} = -13$$

$$C_{13} = 3 \qquad C_{23} = -7 \qquad C_{33} = -1$$

$$X = A^{-1} \times B = \frac{1}{|A|} (AdjA) \times B$$

$$= \frac{1}{-22} \begin{bmatrix} -2 & -10 & 8 \\ -5 & 19 & -13 \\ 3 & -7 & -1 \end{bmatrix} \begin{bmatrix} 16 \\ 19 \\ 25 \end{bmatrix}$$

$$= \frac{-1}{22} \begin{bmatrix} -32 - 190 + 200 \\ -80 + 361 - 325 \\ 48 - 133 - 25 \end{bmatrix}$$

$$\begin{bmatrix} -22 \end{bmatrix}$$

$$C_{13} = 3$$
 $C_{23} = -7$ C_{33}

$$X = A^{-1} \times B = \frac{1}{|A|} (Adj A) \times B$$

$$\begin{bmatrix} -2 & -10 & 8 \end{bmatrix} \begin{bmatrix} 16 & 6 & 6 \\ 6 & 6 & 6 \end{bmatrix}$$

$$=\frac{-1}{22}\begin{bmatrix} -22\\ -44\\ -110 \end{bmatrix}$$

$$\begin{bmatrix} y \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ 5 \end{bmatrix}$$

Hence,
$$x = 1, y = 2, z = 5$$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(vii)

$$\begin{bmatrix} 3 & 4 & 2 \\ 0 & 2 & -3 \\ 1 & -2 & 6 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 8 \\ 3 \\ -2 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 3(6) - 4(3) + 2(-2)$$

= 18 - 12 - 4
= 2 \neq 0

Hence, the system has a unique solution, given by
$$V = A^{-1}B$$

$$X = A^{-1}B$$

the system has a unique solution, given by
$$X = A^{-1}B$$
 $C_{11} = 6$ $C_{21} = -28$ $C_{31} = -16$ $C_{12} = -3$ $C_{22} = 16$ $C_{32} = 9$ $C_{13} = -2$ $C_{23} = 10$ $C_{33} = 6$
 $X = A^{-1}B = \frac{1}{|A|} (Adj A) \times B$
 $= \frac{1}{2} \begin{bmatrix} 6 & -28 & -16 \\ -3 & 16 & 9 \\ 2 & 10 & 6 \end{bmatrix} \begin{bmatrix} 8 \\ 3 \\ -2 \end{bmatrix}$
 $= \frac{1}{2} \begin{bmatrix} 48 - 84 + 32 \\ -24 + 48 - 18 \\ -16 + 30 - 12 \end{bmatrix}$
 $= \frac{1}{2} \begin{bmatrix} -4 \\ 6 \\ 0 \end{bmatrix}$

Next,
$$X = A^{-1}B = \frac{1}{|A|} (Adj A) \times B$$

$$A = A^{-1}B = \frac{1}{|A|} (Adj A) \times B$$

$$= \frac{1}{A} = \frac{1}$$

$$\begin{bmatrix} y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ 1 \end{bmatrix}$$

Hence,
$$x = -2, y = 3, z = 1$$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(viii)

$$\begin{bmatrix} 2 & 1 & 1 & | & x \\ 1 & 3 & -1 & | & y \\ 3 & 1 & -2 \end{bmatrix} \begin{bmatrix} z \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ 5 \\ 6 \end{bmatrix}$$

$$|A| = 2(-5) - 1(1) + 1(-8)$$

= -10 - 1 - 8 = -19 \neq 0

Hence, the unique solution, given by

$$X = A^{-1} \times B$$

$$C_{11} = -5$$
 $C_{21} = 3$ $C_{31} = -4$ $C_{12} = -1$ $C_{22} = -7$ $C_{32} = 3$ $C_{13} = -8$ $C_{23} = 1$ $C_{33} = 5$

$$X = A^{-1} \times B = \frac{1}{|A|} \begin{bmatrix} -5 & 3 & -4 \\ -1 & -7 & 3 \\ -8 & 1 & 5 \end{bmatrix} \begin{bmatrix} 2 \\ 5 \\ 6 \end{bmatrix}$$

$$C_{11} = -5 \qquad C_{21} = 3 \qquad C_{31} = -4$$

$$C_{12} = -1 \qquad C_{22} = -7 \qquad C_{32} = 3$$

$$C_{13} = -8 \qquad C_{23} = 1 \qquad C_{33} = 5$$

$$Next, \quad X = A^{-1} \times B \qquad = \frac{1}{|A|} \begin{bmatrix} -5 & 3 & -4 \\ -1 & -7 & 3 \\ -8 & 1 & 5 \end{bmatrix} \begin{bmatrix} 2 \\ 5 \\ 6 \end{bmatrix}$$

$$= \frac{1}{-19} \begin{bmatrix} -10 + 15 - 24 \\ -2 - 35 + 18 \\ -16 + 5 + 30 \end{bmatrix}$$

$$= \frac{-1}{19} \begin{bmatrix} -19 \\ -19 \\ 10 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ -1 \end{bmatrix}$$

Hence,
$$x = 1, y = 1, z = -1$$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(x)

The above system of equations can be written as

$$\begin{bmatrix} 1 & -1 & 1 \\ 2 & -1 & 0 \\ 0 & 2 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ 0 \\ 1 \end{bmatrix}$$

AX = Bor

$$|A| = 1(1) + 1(-2) + 1(4) = 1 - 2 + 4 = 3 \neq 0$$

So, the above system has a unique solution, given by

$$X = A^{-1}B$$

Let C_{ij} be the co-factor of a_{ij} in A

$$C_{11} = 1$$
 $C_{21} = 1$

$$C_{11} = 1$$
 $C_{21} = 1$

$$C_{12} = 2$$
 $C_{22} = -1$ $C_{32} = 2$

$$C_{13} = 4$$
 $C_{23} = -2$ $C_{33} = 1$

$$C_{ij} \text{ be the co-factor of } a_{ij} \text{ in } A$$

$$C_{11} = 1 \qquad C_{21} = 1 \qquad C_{31} = +1$$

$$C_{12} = 2 \qquad C_{22} = -1 \qquad C_{32} = 2$$

$$C_{13} = 4 \qquad C_{23} = -2 \qquad C_{33} = 1$$

$$adj A = \begin{bmatrix} 1 & 2 & 4 \\ 1 & -1 & -2 \\ +1 & 2 & 1 \end{bmatrix}^{T} = \begin{bmatrix} 1 & 1 & +1 \\ 2 & -1 & 2 \\ 4 & -2 & 1 \end{bmatrix}$$

$$X = A^{-1}B = \frac{1}{|A|} (Adj A) \times B$$

$$= \frac{1}{3} \begin{bmatrix} 1 & 1 & +1 \\ 2 & -1 & 2 \\ 4 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 0 \\ 1 \end{bmatrix}$$

$$= A^{-1}B = \frac{1}{|A|} (Adj A) \times B$$

$$= \frac{1}{3} \begin{bmatrix} 1 & 1 & +1 \\ 2 & -1 & 2 \\ 4 & -2 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 0 \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 3 \\ 6 \\ 9 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$$

Hence,
$$x = 1, y = 2, z = 3$$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(xi)

The above system can be written as

$$\begin{bmatrix} 8 & 4 & 3 \\ 2 & 1 & 1 \\ 1 & 2 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 18 \\ 5 \\ 5 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 8(-1) - 4(1) + 3(3) = -8 - 4 + 9 = -3 \neq 0$$

So, the above system has a unique solution, given by

 $X = A^{-1}B$

Let
$$C_{ij}$$
 be the co-factor of a_{ij} in A

Cu = -1
$$C_{01} = 2$$

$$C_{11} = -1$$
 $C_{21} = 2$

$$C_{11} = -1$$
 $C_{21} = 2$ $C_{12} = -1$ $C_{22} = 5$

$$C_{12} = -1$$
 $C_{22} = 5$ $C_{13} = 3$ $C_{23} = -12$

$$C_{12} = -1$$
 $C_{22} = 5$ $C_{12} = 3$ $C_{22} = -12$

$$C_{13} = 3$$
 $C_{23} = -12$ $C_{33} = 0$

$$dj A = \begin{bmatrix} -1 & -1 & 3 \\ 2 & 5 & -12 \end{bmatrix} = \begin{bmatrix} -1 & 2 & 1 \\ -1 & 5 & -2 \end{bmatrix}$$

$$X = A^{-1}B$$

$$C_{ij} \text{ be the co-factor of } a_{ij} \text{ in } A$$

$$C_{11} = -1 \qquad C_{21} = 2 \qquad C_{31} = 1$$

$$C_{12} = -1 \qquad C_{22} = 5 \qquad C_{32} = -2$$

$$C_{13} = 3 \qquad C_{23} = -12 \qquad C_{33} = 0$$

$$adj A = \begin{bmatrix} -1 & -1 & 3 \\ 2 & 5 & -12 \\ 1 & -2 & 0 \end{bmatrix}^T = \begin{bmatrix} -1 & 2 & 1 \\ -1 & 5 & -2 \\ 3 & -12 & 0 \end{bmatrix}$$

$$X = A^{-1}B = \frac{1}{|A|}(Adj A) \times B$$

$$\begin{bmatrix} -1 & 2 & 1 \end{bmatrix}[18]$$

Now,
$$X = A^{-1}B = \frac{1}{|A|} (Adj A) \times B$$

$$X = A^{-1}B = \frac{1}{|A|} (Adj A) \times B$$

$$\begin{bmatrix} -1 & 2 \end{bmatrix}$$

$$X = A^{-1}B = \frac{1}{|A|} (Adj A) \times B$$

$$= \frac{-1}{3} \begin{bmatrix} -1 & 2 & 1 \\ -1 & 5 & -2 \\ 3 & -12 & 0 \end{bmatrix} \begin{bmatrix} 18 \\ 5 \\ 5 \end{bmatrix}$$

$$= \frac{-1}{3} \begin{bmatrix} -1 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ -3 \end{bmatrix} = \frac{-1}{3} \begin{bmatrix} -3 \\ -3 \\ -3 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 3 \end{bmatrix}$$

Hence,
$$x = 1, y = 1, z = 2$$



Solution of Simultaneous Linear Equations Ex 8.1 Q2(xii)

This system can be written as

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 0 & 2 \\ 3 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 6 \\ 7 \\ 12 \end{bmatrix}$$

AX = Bor

$$|A| = 1(-2) - 1(-5) + 1(1) = -2 + 5 + 1 = 4 \neq 0$$

So,
$$AX = B$$
 has a unique solution, given by
$$X = A^{-1}B$$

Let
$$C_{ij}$$
 be the co-factor of a_{ij} in A

Let
$$C_{ij}$$
 be the co-factor of a_{ij} in A

$$C_{11} = -2$$
 $C_{21} = 0$

$$C_{12} = +5$$
 $C_{22} = -2$ $C_{32} =$

$$C_{13} = 1$$
 $C_{23} = 2$ $C_{33} = -1$

$$X = A^{-1}B$$

$$C_{ij} \text{ be the co-factor of } a_{ij} \text{ in } A$$

$$C_{11} = -2 \qquad C_{21} = 0 \qquad C_{31} = 2$$

$$C_{12} = +5 \qquad C_{22} = -2 \qquad C_{32} = -1$$

$$C_{13} = 1 \qquad C_{23} = 2 \qquad C_{33} = -1$$

$$adj A = \begin{bmatrix} -2 & 5 & 1 \\ 0 & -2 & 2 \\ 2 & -1 & -1 \end{bmatrix}^{T} = \begin{bmatrix} -2 & 0 & 2 \\ 5 & -2 & -1 \\ 1 & 2 & -1 \end{bmatrix}$$

$$X = A^{-1} \times B = \frac{1}{|A|} (Adj A) \times B$$

$$[X] \qquad [-2 \quad 0 \quad 2] [6]$$

$$^{-1} \times B = \frac{1}{|A|} (Adj A) \times B$$

$$X = A^{-1} \times B = \frac{1}{|A|} (Adj A) \times B$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{4} \begin{bmatrix} -2 & 0 & 2 \\ 5 & -2 & -1 \\ 1 & 2 & -1 \end{bmatrix} \begin{bmatrix} 6 \\ 7 \\ 12 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{4} \begin{bmatrix} -12 \\ 4 \\ 8 \end{bmatrix} = \begin{bmatrix} 3 \\ 1 \\ 2 \end{bmatrix}$$

Hence,
$$x = -3, y = 1, z = 2$$

Solution of Simultaneous Linear Equations Ex 8.1 Q2(xiii)

Let

$$\frac{1}{x} = u, \frac{1}{v} = v, \frac{1}{z} = w$$

The above system can be written as

$$\begin{bmatrix} 2 & 3 & 10 \\ 4 & -6 & 5 \\ 6 & 9 & -20 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \\ 2 \end{bmatrix}$$

AX = BOr

$$|A| = 2(75) - 3(-110) + 10(72) = 1200 \neq 0$$

So, the above system has a unique solution, given by

$$X = A^{-1}B$$

Let C_{ii} be the co-factor of a_{ii} in A

$$C_{11} = 75$$
 $C_{21} = 150$ $C_{31} = 75$
 $C_{12} = 110$ $C_{22} = -100$ $C_{32} = 30$
 $C_{13} = 72$ $C_{23} = 0$ $C_{33} = -24$

$$C_{ij} \text{ be the co-factor of } a_{ij} \text{ in } A$$

$$C_{11} = 75 \qquad C_{21} = 150 \qquad C_{31} = 75$$

$$C_{12} = 110 \qquad C_{22} = -100 \qquad C_{32} = 30$$

$$C_{13} = 72 \qquad C_{23} = 0 \qquad C_{33} = -24$$

$$adjA = \begin{bmatrix} 75 & 110 & 72 \\ 150 & -100 & 0 \\ 75 & 30 & -24 \end{bmatrix}^{T} = \begin{bmatrix} 75 & 150 & 75 \\ 110 & -100 & 30 \\ 72 & 0 & -24 \end{bmatrix}$$

$$X = A^{-1}B = \frac{1}{|A|}(AdjA) \times B$$

Now.

$$X = A^{-1}B = \frac{1}{|A|} (AdjA) \times B$$

$$= \frac{1}{1200} \begin{bmatrix} 75 & 150 & 75\\ 110 & -100 & 30\\ 72 & 0 & -24 \end{bmatrix} \begin{bmatrix} 4\\ 1\\ 2 \end{bmatrix}$$

$$\begin{bmatrix} u \\ v \\ w \end{bmatrix} = \frac{1}{1200} \begin{bmatrix} 600 \\ 400 \\ 240 \end{bmatrix} = \begin{bmatrix} \frac{1}{2} \\ \frac{1}{3} \\ \frac{1}{5} \end{bmatrix}$$

Hence, x = 2, y = 3, z = 5

Solution of Simultaneous Linear Equations Ex 8.1 Q2(xiv)

The above system can be written as

$$\begin{bmatrix} 1 & -1 & 2 \\ 3 & 4 & -5 \\ 2 & -1 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 7 \\ -5 \\ 12 \end{bmatrix}$$

Or
$$AX = B$$

$$|A| = 1(7) + 1(19) + 2(-11) = 4 \neq 0$$

So, the above system has a unique solution, given by $X = A^{-1}B$

Let C_{ii} be the co-factor of a_{ii} in A

$$C_{11} = 7$$
 $C_{21} = 1$

$$C_{11} = 7$$
 $C_{21} = 1$ $C_{22} = -1$

$$C_{11} = 7$$
 $C_{21} = 1$ C_{31}
 $C_{12} = -19$ $C_{22} = -1$ C_{32}

$$C_{12} = -19$$
 $C_{22} = -1$ $C_{32} = 11$
 $C_{13} = -11$ $C_{23} = -1$ $C_{33} = 7$

$$C_{13} = -11$$
 $C_{23} = -1$ $C_{33} = 7$

Now.

$$C_{ij} \text{ be the co-factor of } a_{ij} \text{ in } A$$

$$C_{11} = 7 \qquad C_{21} = 1 \qquad C_{31} = -3$$

$$C_{12} = -19 \qquad C_{22} = -1 \qquad C_{32} = 11$$

$$C_{13} = -11 \qquad C_{23} = -1 \qquad C_{33} = 7$$

$$\text{adj} A = \begin{bmatrix} 7 & -19 & -11 \\ 1 & -1 & -1 \\ -3 & 11 & 7 \end{bmatrix}^T = \begin{bmatrix} 7 & 4 & -3 \\ -19 & -1 & 11 \\ -11 & -1 & 7 \end{bmatrix}$$

$$X = A^{-1}B = \frac{1}{|A|}(AdjA) \times B$$

$$X = A^{-1}B = \frac{1}{|A|} (A \operatorname{dj} A) \times B$$

$$= \frac{1}{4} \begin{bmatrix} 7 & 1 & -3 \\ -19 & -1 & 11 \\ -11 & -1 & 7 \end{bmatrix} \begin{bmatrix} 7 \\ -5 \\ 12 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{4} \begin{bmatrix} 8 \\ 4 \\ 12 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ 3 \end{bmatrix}$$

Hence,
$$x = 2$$
, $y = 1$, $z = 3$

Solution of Simultaneous Linear Equations Ex 8.1 Q3(i)

The above system can be written as

$$\begin{bmatrix} 6 & 4 \\ 9 & 6 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$

$$A X = B$$

or AX = B

$$|A| = 36 - 36 = 0$$

So, A is singular. Now, X will be consistent if $(adjA) \times B = 0$

$$C_{11} = 6$$
 $C_{12} = -9$

$$C_{21} = -4$$

 $C_{22} = 6$

$$\operatorname{adj} A = \begin{bmatrix} 6 & -9 \\ -4 & 6 \end{bmatrix}^T = \begin{bmatrix} 6 & -4 \\ -9 & 6 \end{bmatrix}$$

(Adj A)
$$\times B = \begin{bmatrix} 6 & -4 \\ -9 & 6 \end{bmatrix} \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$
$$= \begin{bmatrix} 12 - 12 \\ -18 + 18 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Thus, AX = B will have infinite solutions.

Let
$$y = k$$

Hence,
$$6x = 2 - 4k$$
 or $9x = 3 - 6k$

$$x = \frac{1 - 2k}{3}$$
 or $x = \frac{1 - 2k}{3}$

Hence,
$$x = \frac{1 - 2k}{3}, y = k$$

Solution of Simultaneous Linear Equations Ex 8.1 Q3(ii)

The system can be written as

$$\begin{bmatrix} 2 & 3 \\ 6 & 9 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 5 \\ 15 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 18 - 18 = 0$$

So, A is singular. Now the system will be inconsistent if $(adj A) \times B \neq 0$

$$C_{11} = 9$$
 $C_{21} = -3$ $C_{12} = -6$ $C_{22} = 2$

$$\operatorname{adj} A = \begin{bmatrix} 9 & -6 \\ -3 & 2 \end{bmatrix}^T = \begin{bmatrix} 9 & -3 \\ -6 & 2 \end{bmatrix}$$

$$(Adj A) \times B = \begin{bmatrix} 9 & -3 \\ -6 & 2 \end{bmatrix} \begin{bmatrix} 5 \\ 15 \end{bmatrix}$$

$$= \begin{bmatrix} 45 - 45 \\ -30 + 30 \end{bmatrix} = \begin{bmatrix} 0 \end{bmatrix}$$

Since, $(Adj A \times B) = 0$, the system will have infinite solutions.

Now, Let v = k

$$2x = 5 - 3k$$
 or $x = \frac{5 - 3k}{2}$
 $x = 15 - 9k$ or $x = \frac{5 - 3k}{2}$

Hence,
$$x = \frac{5 - 3k}{2}, y = k$$

Solution of Simultaneous Linear Equations Ex 8.1 Q3(iii)

This can be written as

$$\begin{bmatrix} 5 & 3 & 7 \\ 3 & 26 & 2 \\ 7 & 2 & 10 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 4 \\ 9 \\ 5 \end{bmatrix}$$

AX = Bor

$$|A| = 5(256) - 3(16) + 7(6 - 182)$$

= 0

So, A is singular. Thus, the given system is either inconsistent or it is consistent with infinitely many solutions according as

$$(Adj A) \times B \neq 0$$
 or $(Adj A) \times B = 0$

Let C_{ij} be the co-factor of a_{ij} in A

$$C_{11} = 256$$
 $C_{21} = -16$ $C_{31} = -176$
 $C_{12} = -16$ $C_{22} = 1$ $C_{32} = 11$
 $C_{13} = -176$ $C_{23} = 11$ $C_{33} = 121$

$$adj A = \begin{bmatrix} 256 & -16 & -176 \\ -16 & 1 & 11 \\ -176 & 11 & 121 \end{bmatrix}^{7} = \begin{bmatrix} 256 & -16 & -176 \\ -16 & 1 & 11 \\ -176 & 11 & 121 \end{bmatrix}$$

adj
$$A = \begin{bmatrix} -16 & 1 & 11 \\ -176 & 11 & 121 \end{bmatrix} = \begin{bmatrix} -16 & 1 & 11 \\ -176 & 11 & 121 \end{bmatrix}$$

adj $A \times B = \begin{bmatrix} 256 & -16 & -176 \\ -16 & 1 & 11 \\ -176 & 11 & 121 \end{bmatrix} \begin{bmatrix} 4 \\ 9 \\ 5 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$

AX = B has infinite many solutions.

let $z = k$
 $5x + 3y = 4 - 7k$
 $3x + 26y = 9 - 2k$

can be written as
$$\begin{bmatrix} 5 & 3 \\ 3 & 66 \end{bmatrix} \begin{bmatrix} x \\ y \\ z & 66 \end{bmatrix} = \begin{bmatrix} 4 - 7k \\ 3 & 66 \end{bmatrix}$$

Thus, AX = B has infinite many solutions.

Now, let
$$z = k$$

then, $5x + 3y = 4 - 7k$
 $3x + 26y = 9 - 2k$

Which can be written as

$$\begin{bmatrix} 5 & 3 \\ 3 & 26 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 - 7k \\ 9 - 2k \end{bmatrix}$$
or $A X = B$

$$|A| = 2$$

$$adj A = \begin{bmatrix} 26 & -3 \\ -3 & 5 \end{bmatrix}$$

Now,
$$X = A^{-1}B = \frac{1}{|A|} \times \operatorname{adj} A \times B$$

$$= \frac{1}{121} \begin{bmatrix} 26 & -3 \\ -3 & 5 \end{bmatrix} \begin{bmatrix} 4 - 7k \\ 9 - 2k \end{bmatrix}$$

$$= \frac{1}{121} \begin{bmatrix} 77 - 176k \\ 11k + 33 \end{bmatrix}$$

$$\begin{bmatrix} 7 - 16k \\ 1 - 16k \end{bmatrix}$$

Hence,
$$x = \frac{7 - 16k}{11}$$
, $y = \frac{k + 3}{11}$, $z = k$

Solution of Simultaneous Linear Equations Ex 8.1 Q3(iv)

This above system can be written as

$$\begin{bmatrix} 1 & -1 & 1 \\ 2 & 1 & -1 \\ -1 & -2 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ 2 \\ 1 \end{bmatrix}$$

or AX = B

$$|A| = 1(2-2) + 1(4-1) + 1(-3)$$

= 0 + 3 - 3

So, A is singular. Thus, the given system is either inconsistent or consistent with infinitely many solutions according as

$$(Adj A) \times (B) \neq 0$$
 or $(Adj A) \times B = 0$

Let C_{ij} be the co-factor of a_{ij} in A

$$C_{11} = 0$$
 $C_{21} = 0$ $C_{31} = 0$ $C_{12} = -3$ $C_{22} = 3$ $C_{32} = 3$ $C_{13} = -3$ $C_{23} = -3$ $C_{33} = 3$

$$C_{12} = 3$$
 $C_{23} = -3$ $C_{33} = 3$

$$Adj A = \begin{bmatrix} 0 & -3 & -3 \\ 0 & 3 & 3 \\ 0 & 3 & 3 \end{bmatrix}^T = \begin{bmatrix} 0 & 0 & 0 \\ -3 & 3 & 3 \\ -3 & 3 & 3 \end{bmatrix}^T = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

(adj A) $\times B = \begin{bmatrix} 0 & 0 & 0 \\ -3 & 3 & 3 \\ -3 & 3 & 3 \end{bmatrix} \begin{bmatrix} 3 \\ 2 \\ -3 & 3 & 3 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$

(AX = B has infinite many solutions:

$$AX = B \text{ has infinite many solutions:}$$

$$(adj A) \times B = \begin{bmatrix} 0 & 0 & 0 \\ -3 & 3 & 3 \\ -3 & 3 & 3 \end{bmatrix} \begin{bmatrix} 3 \\ 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

Thus, AX = B has infinite many solutions.

Now, let
$$z = k$$

So, $x - y = 3 - k$
 $2x + y = 2 + k$

Which can be written as

$$\begin{bmatrix} 1 & -1 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3-k \\ 2+k \end{bmatrix}$$
or $AX = B$

$$|A| = 1 + 2 = 3 \neq 0$$

$$\operatorname{adj} A = \begin{bmatrix} 1 & -2 \\ 1 & 1 \end{bmatrix}^T = \begin{bmatrix} 1 & 1 \\ -2 & 1 \end{bmatrix}$$

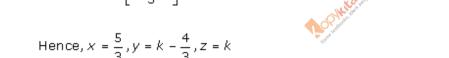
and,
$$X = A^{-1}B$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{|A|} \begin{bmatrix} 1 & 1 \\ -2 & 1 \end{bmatrix} \begin{bmatrix} 3-5 \\ 2+k \end{bmatrix}$$

$$= \frac{1}{3} \begin{bmatrix} 3-k+2+k \\ -6+2k+2+k \end{bmatrix}$$

$$\begin{bmatrix} 5 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 \\ 3k - 4 \\ 3 \end{bmatrix}$$
Hence $k = 5$, $k = 4$,



Solution of Simultaneous Linear Equations Ex 8.1 Q3(v)

This system can be written as

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 1 & 4 & 7 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 6 \\ 14 \\ 30 \end{bmatrix}$$

AX = Bor

$$|A| = 1(2) - 1(4) + 1(2)$$

= 2 - 4 + 2
= 0

So, A is singular. Thus, the given system has either no solution or infinite solutions depending on as

$$(Adj A) \times (B) \neq 0$$
 or $(Adj A) \times (B) = 0$

Let C_{ij} be the co-factor of a_{ij} in A

$$C_{11} = 2$$
 $C_{21} = -3$ $C_{31} = 1$ $C_{12} = -4$ $C_{22} = 6$ $C_{32} = -2$ $C_{13} = 2$ $C_{23} = -3$ $C_{33} = 1$

$$adj A = \begin{bmatrix} 2 & -4 & 2 \\ -3 & 6 & -3 \\ 1 & -2 & 1 \end{bmatrix}^{T} = \begin{bmatrix} 2 & -3 & 1 \\ -4 & 6 & -2 \\ 2 & -3 & 1 \end{bmatrix}$$

adj
$$A = \begin{bmatrix} 2 & -4 & 2 \\ -3 & 6 & -3 \\ 1 & -2 & 1 \end{bmatrix}^T = \begin{bmatrix} 2 & -3 & 1 \\ -4 & 6 & -2 \\ 2 & -3 & 1 \end{bmatrix}$$

$$\text{(adj } A \text{)} \times B = \begin{bmatrix} 2 & -3 & 1 \\ -4 & 6 & -2 \\ 2 & -3 & 1 \end{bmatrix} \begin{bmatrix} 6 \\ 14 \\ 30 \end{bmatrix} = \begin{bmatrix} 12 - 42 + 30 \\ -24 + 84 - 60 \\ 12 - 42 + 30 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$\text{(} = B \text{ has infinite solutions.)}$$

$$\text{let } z = k$$

$$x + y = 6 - k$$

$$x + 2y = 14 - 3k$$

So, AX = B has infinite solutions.

Now, let
$$z = k$$

So, $x + y = 6 - k$
 $x + 2y = 14 - 3k$

Which can be written as

$$\begin{bmatrix} 1 & 1 \\ 1 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 6 - k \\ 14 - 3k \end{bmatrix}$$
$$A X = B$$

$$|A| = 1 \neq 0$$

or

$$\operatorname{adj} A = \begin{bmatrix} 2 & -1 \\ -1 & 1 \end{bmatrix}^{T} = \begin{bmatrix} 2 & -1 \\ -1 & 1 \end{bmatrix}$$

$$X = A^{-1}B = \frac{1}{|A|}\operatorname{adj} A \times B$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{1} \begin{bmatrix} 2 & -1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} 6 - k \\ 14 - 3k \end{bmatrix}$$

$$= \begin{bmatrix} 12 - 2k - 14 + 3k \\ -6 + k + 14 - 3k \end{bmatrix}$$

$$\begin{bmatrix} x \\ -6 + k \end{bmatrix}$$

$$[y]^{-}[8-2k]$$

Hence,
$$x = k - 2$$

$$y = 8 - 2k$$

$$z = k$$

Solution of Simultaneous Linear Equations Ex 8.1 Q3(vi)

This system can be written as

$$\begin{bmatrix} 2 & 2 & -2 \\ 4 & 4 & -1 \\ 6 & 6 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 2(14) - 2(14) - 2(0) = 0$$

So, A is singular and the system has either no solution or infinite solutions according as

$$(Adj A) \times (B) \neq 0$$
 or $(Adj A) \times (B) = 0$

Let C_{ij} be the co-factor of a_{ij} in A

$$C_{11} = 14$$

$$C_{21} = -16$$

$$C_{31} = 6$$

$$C_{11} = 14$$
 $C_{21} = -16$ $C_{31} = 6$ $C_{12} = -14$ $C_{22} = 16$ $C_{32} = -6$ $C_{13} = 0$ $C_{23} = 0$ $C_{33} = 0$

$$C_{22} = 16$$

$$C_{13} = 0$$

$$C_{23} = 0$$

$$C_{33} = 0$$

$$adj A = \begin{bmatrix} 14 & -14 & 0 \\ -16 & 16 & 0 \\ 6 & -6 & 0 \end{bmatrix}^{T} = \begin{bmatrix} 14 & -16 & 6 \\ -14 & 16 & -6 \\ 0 & 0 & 0 \end{bmatrix}$$

$$(adj A) \times B = \begin{bmatrix} 14 & -16 & 6 \\ -14 & 16 & -6 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 14 - 32 + 18 \\ -14 + 32 - 18 \\ 0 + 0 + 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

So, AX = B has infinite solutions.

Now, let
$$z = k$$

So,
$$2x + 2y = 1 + 2k$$

$$4x + 4y = 2 + k$$

Which can be written as

$$\begin{bmatrix} 2 & 2 \\ 4 & 4 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 1 + 2k \\ 2 + k \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 0, z = 0$$

Again,

$$2x + 2y = 1$$

$$4x + 4y = 2$$

Solution of Simultaneous Linear Equations Ex 8.1 Q4(i)

The above system can be written as

$$\begin{bmatrix} 2 & 5 \\ 6 & 15 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 7 \\ 13 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 0$$

So, A is singular, and the above system will be inconsistent if
$$(adj A) \times B \neq 0$$

Now,
$$C_{11} = 15$$

 $C_{12} = -6$

$$C_{21} = -5$$

 $C_{22} = 2$

$$\operatorname{adj} A = \begin{bmatrix} 15 & -6 \\ -5 & 2 \end{bmatrix}^{T} = \begin{bmatrix} 15 & -5 \\ -6 & 2 \end{bmatrix}$$

$$(adj A) \times (B) = \begin{bmatrix} 15 & -5 \\ -6 & 2 \end{bmatrix} \begin{bmatrix} 7 \\ 13 \end{bmatrix}$$

$$= \begin{bmatrix} 105 - 65 \\ -42 + 26 \end{bmatrix}$$

$$= \begin{bmatrix} 40 \\ -16 \end{bmatrix}$$

$$\neq 0$$

Hence, the above system is inconsistent

Solution of Simultaneous Linear Equations Ex 8.1 Q4(ii)

This system can be written as

$$\begin{bmatrix} 2 & 3 \\ 6 & 9 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 5 \\ 10 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 0$$

So, the above system will be inconsistent, if
$$(adj A) \times B \neq 0$$

$$C_{11} = 9$$

$$C_{12} = -6$$
 $C_{24} = -3$

$$C_{22} = 2$$

$$\operatorname{dj} A = \begin{bmatrix} 9 & -6 \\ -3 & 2 \end{bmatrix}^{T} = \begin{bmatrix} 9 & -3 \\ -6 & 2 \end{bmatrix}$$

(adj A)
$$\times B \neq 0$$

$$C_{11} = 9$$

$$C_{12} = -6$$

$$C_{21} = -3$$

$$C_{22} = 2$$

adj $A = \begin{bmatrix} 9 & -6 \end{bmatrix}^{7} = \begin{bmatrix} 9 & -3 \\ -6 & 2 \end{bmatrix} \begin{bmatrix} 5 \\ 10 \end{bmatrix}$

$$= \begin{bmatrix} 45 - 30 \\ -30 + 20 \end{bmatrix}$$

$$= \begin{bmatrix} 15 \\ -10 \end{bmatrix}$$

$$\begin{bmatrix} -30 + 20 \\ 15 \\ -10 \end{bmatrix}$$

$$\neq 0$$

Hence, the above system is inconsistent

Solution of Simultaneous Linear Equations Ex 8.1 Q4(iii)

This system can be written as

$$\begin{bmatrix} 4 & -2 \\ 6 & -3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 \\ 5 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = -12 + 12 = 0$$

So, A is singular. Now system will be inconsistent, if
$$(adj A) \times B \neq 0$$

$$C_{11} = -3$$

$$C_{12} = -6$$

 $C_{21} = 2$

$$C_{22} = 4$$

$$\operatorname{adj} A = \begin{bmatrix} -3 & -6 \\ 2 & 4 \end{bmatrix}^{T} = \begin{bmatrix} -3 & 2 \\ -6 & 4 \end{bmatrix}$$

$$(adj A) \times (B) = \begin{bmatrix} -3 & 2 \\ -6 & 4 \end{bmatrix} \begin{bmatrix} 3 \\ 5 \end{bmatrix}$$

$$= \begin{bmatrix} -9+10 \\ -18+20 \end{bmatrix}$$

Hence, the above system is inconsistent

Solution of Simultaneous Linear Equations Ex 8.1 Q4(iv)

The above system can be written as

$$\begin{bmatrix} 4 & -5 & -2 \\ 5 & -4 & 2 \\ 2 & 2 & 8 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ -2 \\ -1 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 4(-36) + 5(36) - 2(18)$$

= -144 + 180 - 36
= 0

So, A is singular and the above system will be inconsistent, if

(adj
$$A$$
) $\times B \neq 0$

$$C_{11} = -36 \qquad C_{21} = 36 \qquad C_{31} = -18$$

$$C_{12} = -36 \qquad C_{22} = 36 \qquad C_{32} = -18$$

$$C_{13} = 18 \qquad C_{23} = -18 \qquad C_{33} = 9$$

$$\begin{bmatrix} -36 & -36 & 18 \end{bmatrix}^T \qquad \begin{bmatrix} -36 & 36 & -18 \end{bmatrix}$$

$$(adj A) = \begin{bmatrix} -36 & -36 & 18 \\ 36 & 36 & -18 \\ -18 & -18 & 9 \end{bmatrix} = \begin{bmatrix} -36 & 36 & -18 \\ -36 & 36 & -18 \\ 18 & -18 & 9 \end{bmatrix}$$

$$(adj A) \times (B) = \begin{bmatrix} -36 & 36 & -18 \\ -36 & 36 & -18 \\ 18 & -18 & 9 \end{bmatrix} \begin{bmatrix} 2 \\ -2 \\ -1 \end{bmatrix} = \begin{bmatrix} -72 - 72 + 18 \\ -72 - 72 + 18 \\ +36 + 36 - 9 \end{bmatrix} \neq 0$$

Hence, the above system is inconsistent.

Solution of Simultaneous Linear Equations Ex 8.1 Q4(v)

The above system can be written as

$$\begin{bmatrix} 3 & -1 & -2 \\ 0 & 2 & -1 \\ 3 & -5 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 3(-5) + 1(3) - 2(-6) = -15 + 3 + 12 = 0$$

So, A is singular and the above system of equations will be inconsistent, if

(adj A)
$$\times B \neq 0$$

$$C_{11} = -5 \qquad C_{21} = +10 \qquad C_{31} = 5$$

$$C_{12} = 3 \qquad C_{22} = 6 \qquad C_{32} = 3$$

$$C_{13} = -6 \qquad C_{23} = 12 \qquad C_{33} = 6$$
(adj A) $= \begin{bmatrix} -5 & 3 & -6 \\ 10 & 6 & 12 \\ 5 & 3 & 6 \end{bmatrix}^T = \begin{bmatrix} -5 & 10 & 5 \\ 3 & 6 & 3 \\ -6 & 12 & 6 \end{bmatrix}$

$$(adj A) = \begin{bmatrix} -5 & 3 & -6 \\ 10 & 6 & 12 \\ 5 & 3 & 6 \end{bmatrix} = \begin{bmatrix} -5 & 10 & 5 \\ 3 & 6 & 3 \\ -6 & 12 & 6 \end{bmatrix}$$

$$(adj A) \times (B) = \begin{bmatrix} -5 & 10 & 5 \\ 3 & 6 & 3 \\ -6 & 12 & 6 \end{bmatrix} \begin{bmatrix} 2 \\ -1 \\ 3 \end{bmatrix} = \begin{bmatrix} -10 - 10 + 15 \\ 6 - 6 + 9 \\ -12 - 12 + 18 \end{bmatrix} \neq 0$$

Hence, the given system of equations is inconsistent.

Solution of Simultaneous Linear Equations Ex 8.1 Q4(vi)

The above system can be written as

$$\begin{bmatrix} 1 & 1 & -2 \\ 1 & -2 & 1 \\ -2 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 5 \\ -2 \\ 4 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 1(-3) - 1(3) - 2(-3) = -3 - 3 + 6 = 0$$

So, A is singular. Now the system can be inconsistent, if $(adj A) \times B \neq 0$

adj
$$A$$
) = $\begin{bmatrix} -3 & -3 & -3 \\ -3 & -3 & -3 \end{bmatrix}$ = $\begin{bmatrix} -3 & -3 & -3 \\ -3 & -3 & -3 \end{bmatrix}$

$$\begin{bmatrix} -3 & -3 & -3 \end{bmatrix} \begin{bmatrix} -3 & -3 & -3 \end{bmatrix}$$

$$(adj A) \times (B) = \begin{bmatrix} -3 & -3 & -3 \\ -3 & -3 & -3 \end{bmatrix} \begin{bmatrix} 5 \\ -2 \\ 4 \end{bmatrix} = \begin{bmatrix} -15+6-12 \\ -15+6-12 \end{bmatrix}$$

$$= \begin{bmatrix} -21 \\ -21 \\ -21 \end{bmatrix}$$

$$\neq 0$$

Hence, the given system is inconsistent.

Solution of Simultaneous Linear Equations Ex 8.1 O5

$$A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & 4 \\ 0 & 1 & 2 \end{bmatrix} \text{ and } B = \begin{bmatrix} 2 & 2 & -4 \\ -4 & 2 & -4 \\ 2 & -1 & 5 \end{bmatrix}$$

$$A \times B = \begin{bmatrix} 2+4+0 & 2-2+0 & -4+4+0 \\ 4-12+8 & 4+6-4 & -8-12+20 \\ 0-4+4 & 0+2-2 & 0-4+10 \end{bmatrix}$$

$$AB = \begin{bmatrix} 6 & 0 & 0 \\ 0 & 6 & 0 \\ 0 & 0 & 6 \end{bmatrix}$$

AB = 6I, where I is a 3×3 unit matrix

or
$$A^{-1} = \frac{1}{6}B$$
 [By def. of inverse]

$$= \frac{1}{6} \begin{bmatrix} 2 & 2 & -4 \\ -4 & 2 & -4 \\ 2 & -1 & 5 \end{bmatrix}$$

$$\begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & 4 \\ 0 & 1 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ 17 \\ 7 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 1 & 2 \end{bmatrix} \begin{bmatrix} z \end{bmatrix} \begin{bmatrix} 7 \\ 0 & A \end{bmatrix}$$
 or
$$A = B$$
 or
$$X = A^{-1}B$$

or

$$= \frac{1}{6} \begin{bmatrix} 2 & 2 & -4 \\ -4 & 2 & -4 \\ 2 & -1 & 5 \end{bmatrix} \begin{bmatrix} 3 \\ 17 \\ 7 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{6} \begin{bmatrix} 6 + 34 - 28 \\ -12 + 34 - 28 \\ 6 - 17 + 35 \end{bmatrix} = \frac{1}{6} \begin{bmatrix} 12 \\ -6 \\ 24 \end{bmatrix} = \begin{bmatrix} 2 \\ -1 \\ 4 \end{bmatrix}$$

Hence,
$$x = 2, y = -1, z = 4$$

Solution of Simultaneous Linear Equations Ex 8.1 Q6

$$A = \begin{bmatrix} 2 & -3 & 5 \\ 3 & 2 & -4 \\ 1 & 1 & -2 \end{bmatrix}$$

$$|A| = 2(0) + 3(-2) + 5(1) = -1 \neq 0$$

Also,
$$C_{11} = 0$$
 $C_{21} = -1$ $C_{31} = 2$ $C_{12} = 2$ $C_{22} = -9$ $C_{32} = 23$ $C_{13} = 1$ $C_{23} = -5$ $C_{33} = 13$

$$(adj A) = \begin{bmatrix} 0 & 2 & 1 \\ -1 & -9 & -5 \\ 2 & 23 & 13 \end{bmatrix}^T = \begin{bmatrix} 0 & -1 & 2 \\ 2 & -9 & 23 \\ 1 & -5 & 13 \end{bmatrix}$$

$$A^{-1} = \frac{1}{|A|} (adj A) = \frac{1}{-1} \begin{bmatrix} 0 & -1 & 2 \\ 2 & -9 & 23 \\ 1 & -5 & 13 \end{bmatrix} = \begin{bmatrix} 0 & 1 & -2 \\ -2 & 9 & -23 \\ -1 & 5 & -13 \end{bmatrix}$$
given system of equations can be written as
$$\begin{bmatrix} 2 & -3 & 5 \\ 3 & 2 & -4 \\ -1 & 1 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 11 \\ -5 \\ -3 \end{bmatrix}$$

$$A X = B$$

$$X = A^{-1}B$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 & 1 & -2 \\ -2 & 9 & -23 \\ -1 & 5 & -13 \end{bmatrix} \begin{bmatrix} 11 \\ -5 \\ -3 \end{bmatrix}$$

$$\begin{bmatrix} -5 + 6 \end{bmatrix}$$

The given system of equations can be written as

$$\begin{bmatrix} 2 & -3 & 5 \\ 3 & 2 & -4 \\ -1 & 1 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 11 \\ -5 \\ -3 \end{bmatrix}$$

or
$$AX = A$$

$$X = A^{-1}B$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 & 1 & -2 \\ -2 & 9 & -23 \\ -1 & 5 & -13 \end{bmatrix} \begin{bmatrix} 11 \\ -5 \\ -3 \end{bmatrix}$$

$$\begin{bmatrix} -5+6 \\ -1 \end{bmatrix}$$

$$\begin{bmatrix} -5+6 \\ -22+45+69 \\ -11-25+39 \end{bmatrix}$$

$$\begin{bmatrix} x \\ 1 \\ -1 \end{bmatrix}$$

Hence,
$$x = 1, y = 2, z = 3$$

$$A = \begin{bmatrix} 1 & 2 & 5 \\ 1 & -1 & -1 \\ 2 & 3 & -1 \end{bmatrix}$$

$$|A| = 1(1+3) - 2(-1+2) + 5(5) = 4 - 2 + 25 = 27 \neq 0$$

$$C_{11} = 4$$
 $C_{21} = 17$ $C_{31} = 3$

$$C_{12} = -1$$
 $C_{22} = -11$ $C_{32} = 6$ $C_{13} = 5$ $C_{23} = 1$ $C_{33} = -3$

$$A^{-1} = \frac{1}{|A|} \times \text{adj } A = \frac{1}{27} \begin{bmatrix} 4 & 17 & 3 \\ -1 & -11 & 6 \\ 5 & 1 & -3 \end{bmatrix}$$
Now, the given set of equations can be represented as $x + 2y + 5z = 10$

$$x - y - z = -2$$

$$2x + 3y - z = -11$$
or
$$\begin{bmatrix} 1 & 2 & 5 \\ 1 & -1 & -1 \\ 2 & 3 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 10 \\ -2 \\ -11 \end{bmatrix}$$
or $X = A^{-1} \times B$

Now, the given set of equations can be represented a
$$x + 2y + 5z = 10$$

$$x + 2y + 5z = 10$$

 $x - y - z = -2$
 $2x + 3y - z = -11$

or
$$\begin{bmatrix} 1 & 2 & 5 \\ 1 & -1 & -1 \\ 2 & 3 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 10 \\ -2 \\ -11 \end{bmatrix}$$

or
$$X = A^{-1} \times B$$

$$= \frac{1}{27} \begin{bmatrix} 4 & 17 & 3 \\ -1 & -11 & 6 \\ 5 & 1 & -3 \end{bmatrix} \begin{bmatrix} 10 \\ -2 \\ -11 \end{bmatrix}$$

$$= \frac{1}{27} \begin{bmatrix} 40 - 34 - 33 \\ -10 + 22 - 66 \\ 50 - 2 + 33 \end{bmatrix} = \frac{1}{27} \begin{bmatrix} -27 \\ -54 \\ 81 \end{bmatrix} = \begin{bmatrix} -1 \\ -2 \\ 3 \end{bmatrix}$$

Hence,
$$x = -1, y = -2, z = 3$$

Solution of Simultaneous Linear Equations
$$A = \begin{bmatrix} 1 & -2 & 0 \\ 2 & 1 & 3 \\ 0 & -2 & 1 \end{bmatrix}$$

$$|A| = 1(7) + 2(2) = 11$$

$$C_{11} = 7$$
 $C_{21} = 2$ $C_{31} = -6$

$$C_{12} = -2$$
 $C_{22} = 1$ $C_{32} = -3$ $C_{13} = -4$ $C_{23} = 2$ $C_{33} = 5$

$$A^{-1} = \frac{1}{|A|} \operatorname{adj} A = \frac{1}{11} \begin{bmatrix} 7 & 2 & -6 \\ -2 & 1 & -3 \\ -4 & 2 & 5 \end{bmatrix}$$

Now,
$$x - 2y = 10$$

$$2x + y + 3z$$

$$-2y + z = 7$$

$$-2y + z = 7$$

or
$$\begin{bmatrix} 1 & -2 & 0 \\ 2 & 1 & 3 \\ 0 & -2 & 1 \end{bmatrix} = \begin{bmatrix} 10 \\ 8 \\ 7 \end{bmatrix}$$

or
$$X = A^{-1} \times B$$

$$A^{-1} = \frac{1}{|A|} \operatorname{adj} A = \frac{1}{11} \begin{bmatrix} 7 & 2 & -6 \\ -2 & 1 & -3 \\ -4 & 2 & 5 \end{bmatrix}$$
Now, $x - 2y = 10$

$$2x + y + 3z = 8$$

$$-2y + z = 7$$
or
$$\begin{bmatrix} 1 & -2 & 0 \\ 2 & 1 & 3 \\ 0 & -2 & 1 \end{bmatrix} = \begin{bmatrix} 10 \\ 8 \\ 7 \end{bmatrix}$$
or $X = A^{-1} \times B$

$$= \frac{1}{11} \begin{bmatrix} 7 & 2 & -6 \\ -2 & 1 & -3 \\ -4 & 2 & 5 \end{bmatrix} \begin{bmatrix} 10 \\ 8 \\ 7 \end{bmatrix}$$

$$= \frac{1}{11} \begin{bmatrix} 70 + 16 - 42 \\ -20 + 8 - 21 \\ -40 + 16 + 35 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{11} \begin{bmatrix} 44 \\ -33 \\ 11 \end{bmatrix} = \begin{bmatrix} 4 \\ -3 \\ 1 \end{bmatrix}$$

Hence, x = 4, y = -3, z = 1

$$A = \begin{bmatrix} 3 & -4 & 2 \\ 2 & 3 & 5 \\ 1 & 0 & 1 \end{bmatrix}$$

$$|A| = 3(3) + 4(-3) + 2(-3) = -9$$

$$C_{11} = 3$$
 $C_{21} = 4$ $C_{31} = -26$
 $C_{12} = 3$ $C_{22} = 1$ $C_{32} = -11$
 $C_{13} = -3$ $C_{22} = -4$ $C_{33} = 17$

$$A^{-1} = \frac{1}{|A|} \operatorname{adj} A = \frac{1}{-9} \begin{bmatrix} 3 & 4 & -26 \\ 3 & 1 & -11 \\ -3 & -4 & 17 \end{bmatrix}$$

Now,

$$3x-4y+2z=-1$$

 $2x+3y+5z=7$

$$x+z=2$$

$$\begin{bmatrix} 3 & -4 & 2 \\ & & 2 \end{bmatrix} \begin{bmatrix} -1 \\ & & 2 \end{bmatrix}$$

Or
$$\begin{bmatrix} 2 & 3 & 5 \\ 1 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 7 \\ 2 \end{bmatrix}$$

$$X = A^{-1} \times B$$

$$= \frac{1}{-9} \begin{bmatrix} 3 & 4 & -26 \\ 3 & 1 & -11 \\ -3 & -4 & 17 \end{bmatrix} \begin{bmatrix} -1 \\ 7 \\ 2 \end{bmatrix}$$
$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{-9} \begin{bmatrix} -27 \\ -18 \\ 9 \end{bmatrix}$$

Hence
$$x = 3, y = 2, z = -1$$

$$A = \begin{bmatrix} 1 & -2 & 0 \\ 2 & 1 & 3 \\ 0 & -2 & 1 \end{bmatrix} \text{ and } B = \begin{bmatrix} 7 & 2 & -6 \\ -2 & 1 & -3 \\ -4 & 2 & 5 \end{bmatrix}$$
$$A \times B = \begin{bmatrix} 11 & 0 & 0 \\ 0 & 11 & 0 \\ 0 & 0 & 11 \end{bmatrix}$$

AB = 11I, where I is a 3×3 unit matrix

$$A^{-1} = \frac{1}{11}B$$
 [By def. of inverse]
Or
$$= \frac{1}{11} \begin{bmatrix} 7 & 2 & -6 \\ -2 & 1 & -3 \\ -4 & 2 & 5 \end{bmatrix}$$

Now, the given system of equations can be written as

$$\frac{1}{11}B \qquad [Bydef. of inverse]$$

$$= \frac{1}{11}\begin{bmatrix} 7 & 2 & -6 \\ -2 & 1 & -3 \\ -4 & 2 & 5 \end{bmatrix}$$
the given system of equations can be written as
$$\begin{bmatrix} 1 & -2 & 0 \\ 2 & 1 & 3 \\ 0 & -2 & 1 \end{bmatrix}\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 10 \\ 8 \\ 7 \end{bmatrix}$$

$$AX = B$$

$$X = A^{-1}B$$

$$= \frac{1}{11}\begin{bmatrix} 7 & 2 & -6 \\ -2 & 1 & -3 \\ -4 & 2 & 5 \end{bmatrix}\begin{bmatrix} 10 \\ 8 \\ 7 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \frac{1}{11}\begin{bmatrix} 44 \\ -33 \end{bmatrix} = \begin{bmatrix} 4 \\ -3 \end{bmatrix}$$

$$X = A^{-1}B$$

Or

Or

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{11} \begin{bmatrix} 44 \\ -33 \\ 11 \end{bmatrix} = \begin{bmatrix} 4 \\ -3 \\ 1 \end{bmatrix}$$

Hence,
$$x = 4$$
, $y = -3$, $z = 1$

Let the numbers are x, y, z.

$$x + z + 5(x) = 6$$

 $5x + y + z = 6$ ---(3)

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 1 \\ 5 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ 1 \\ 6 \end{bmatrix}$$

or
$$AX = B$$

$$|A| = 1(1) - 1(-4) + 1(-9)$$

= 1 + 4 - 9 = -4 \(\neq 0

Hence, the unique solutions given by
$$x = A^{-1}B$$

$$C_{11} = 1$$
 $C_{21} = 0$ $C_{31} = -1$

$$C_{12} = 4$$
 $C_{22} = -4$ $C_{32} = 0$ $C_{13} = -9$ $C_{23} = 4$ $C_{33} = 0$

$$C_{11} = 1 \qquad C_{21} = 0 \qquad C_{31} = -1$$

$$C_{12} = 4 \qquad C_{22} = -4 \qquad C_{32} = 0$$

$$C_{13} = -9 \qquad C_{23} = 4 \qquad C_{33} = 1$$
or
$$X = A^{-1}B = \frac{1}{|A|} (adj A) \times B = \frac{1}{-4} \begin{bmatrix} 1 & 0 & -1 \\ 4 & -4 & 0 \\ -9 & 4 & 1 \end{bmatrix} \begin{bmatrix} 2 \\ 1 \\ 6 \end{bmatrix}$$

$$= \frac{-1}{4} \begin{bmatrix} 2 - 6 \\ 8 - 4 \\ -18 + 4 + 6 \end{bmatrix} = \frac{-1}{4} \begin{bmatrix} -4 \\ 4 \\ -8 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \\ 2 \end{bmatrix}$$

Hence,
$$x = 1, y = -1, z = 2$$

Let the three investments are x, y, z

$$x + y + z = 10,000$$
(1)

A1so

$$\frac{10}{100}x + \frac{12}{100}y + \frac{15}{100}z = 1310$$

$$0.1x + 0.12y + 0.15z = 1310 \qquad(2)$$

A1so

$$\frac{10}{100}x + \frac{12}{100}y = \frac{15}{100}z - 190$$

$$0.1x + 0.12y - 0.15z = -190$$
 (3)

The above system can be written as

$$\begin{bmatrix} 1 & 1 & 1 \\ 0.1 & 0.12 & 0.15 \\ 0.1 & 0.12 & -0.15 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 10000 \\ 1310 \\ -190 \end{bmatrix}$$

Or
$$AX = B$$

$$|A| = 1(-0.036) - 1(-0.03) + 1(0) = -0.006 \neq 0$$

So, the above system has a unique solution, given by

$$X = A^{-1}B$$

Let C_{ii} be the co-factor of a_{ii} in A

$$C_{11} = -0.036$$
 $C_{21} = 0.27$ $C_{31} = 0.03$ $C_{12} = 0.03$ $C_{22} = -0.25$ $C_{32} = -0.05$ $C_{13} = 0$ $C_{23} = -0.02$ $C_{33} = 0.02$

$$\begin{aligned} & \begin{bmatrix} 0.1 & 0.12 & -0.15 \end{bmatrix} \begin{bmatrix} z \end{bmatrix} \begin{bmatrix} -190 \end{bmatrix} \\ & AX = B \\ & |A| = 1(-0.036) - 1(-0.03) + 1(0) = -0.006 \neq 0 \end{aligned}$$
 the above system has a unique solution, given by $X = A^{-1}B$
$$\begin{aligned} & C_{ij} \text{ be the co-factor of } a_{ij} \text{ in } A \\ & C_{11} = -0.036 & C_{21} = 0.27 & C_{31} = 0.03 \\ & C_{12} = 0.03 & C_{22} = -0.25 & C_{32} = -0.05 \\ & C_{13} = 0 & C_{23} = -0.02 & C_{33} = 0.02 \end{aligned}$$

$$\begin{aligned} & adjA = \begin{bmatrix} -0.036 & 0.03 & 0 \\ 0.27 & -0.25 & -0.02 \\ 0.03 & -0.05 & 0.02 \end{bmatrix}^T = \begin{bmatrix} -0.036 & 0.27 & 0.03 \\ 0.03 & -0.25 & -0.05 \\ 0 & -0.02 & 0.02 \end{bmatrix}$$

Now.

$$X = A^{-1}B = \frac{1}{|A|} (AdjA) \times B$$

$$= \frac{1}{-0.006} \begin{bmatrix} -0.036 & 0.27 & 0.03 \\ 0.03 & -0.25 & -0.05 \\ 0 & -0.02 & 0.02 \end{bmatrix} \begin{bmatrix} 10000 \\ 1310 \\ -190 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{-0.006} \begin{bmatrix} -12 \\ -18 \\ -30 \end{bmatrix} = \begin{bmatrix} 2000 \\ 3000 \\ 5000 \end{bmatrix}$$

Hence, x = Rs 2000, y = Rs 3000, z = Rs 5000

$$x + y + z = 45$$

$$z = x + 8$$

$$x + z = 2y$$

$$x + z = 2y$$

$$---(3)$$

or
$$\begin{bmatrix} 1 & 1 & 1 \\ -1 & 0 & 1 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 45 \\ 8 \\ 0 \end{bmatrix}$$

$$\begin{vmatrix} A | = 1(2) - 1(-2) + 1(2) \\ = 2 + 2 + 2 = 6 \neq 0 \end{vmatrix}$$

$$C_{11} = 2$$

$$C_{12} = 2$$

$$C_{12} = 2$$

$$C_{22} = 0$$

$$C_{31} = 1$$

$$C_{12} = 2$$

$$C_{23} = +3$$

$$C_{33} = 1$$

$$X = A^{-1} \times B = \frac{1}{|A|} \begin{bmatrix} adj A \\ y \\ 0 \end{bmatrix} \times B$$

$$= \frac{1}{6} \begin{bmatrix} 2 & -3 & 1 \\ 2 & 0 & -2 \\ 2 & 3 & 1 \end{bmatrix} \begin{bmatrix} 45 \\ 8 \\ 0 \end{bmatrix}$$

$$= \frac{1}{6} \begin{bmatrix} 90 - 24 \\ 90 \\ 90 + 24 \end{bmatrix} = \frac{1}{6} \begin{bmatrix} 66 \\ 90 \\ 114 \end{bmatrix}$$

$$\begin{bmatrix} x \end{bmatrix} \begin{bmatrix} 11 \end{bmatrix}$$

Hence,
$$x = 11, y = 15, z = 19$$

The given problem can be modelled using the following system of equations

$$3x + 5y - 4z = 6000$$

$$2x - 3y + z = 5000$$

$$-x + 4y + 6z = 13000$$

Which can write as Ax = B,

Where

$$A = \begin{bmatrix} 3 & 5 & -4 \\ 2 & -3 & 1 \\ -1 & 4 & 6 \end{bmatrix}, \quad X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}, \quad B = \begin{bmatrix} 6000 \\ 5000 \\ 13000 \end{bmatrix}$$

Now

$$|A| = 3(-18 - 4) - 2(30 + 16) - 1(5 - 12)$$

= 3(-22) - 2(46) + 7

$$= -66 - 92 + 7$$

 $= -151 \neq 0$

$$\therefore$$
 A^{-1} exists.

Now
$$Ax = B \Rightarrow x = A^{-1}B$$

$$A^{-1} = \frac{adj(A)}{|A|}$$

Cofators of A are

$$C_{11} = -22$$
 $C_{21} = -3$

$$C_{12} = -7$$
 $C_{22} = -11$ $C_{22} =$

$$adj(A) = \begin{bmatrix} -22 & -46 & -7 \\ -13 & +14 & -11 \\ 5 & -17 & -19 \end{bmatrix}$$

Hence,

$$X = \frac{1}{|A|} adj (A)(B)$$

$$A^{-1} \text{ exists.}$$

$$A \times A \times B \Rightarrow X = A^{-1}B$$

$$A^{-1} = \frac{adj(A)}{|A|}$$

$$A^{-1} = -22 \qquad C_{21} = -13 \qquad C_{31} = 5$$

$$C_{12} = -46 \qquad C_{22} = 14 \qquad C_{32} = -17$$

$$C_{13} = -7 \qquad C_{23} = -11 \qquad C_{33} = -19$$

$$A^{-1} = -22 \qquad C_{21} = -13 \qquad C_{31} = 5$$

$$C_{12} = -46 \qquad C_{22} = 14 \qquad C_{32} = -17$$

$$C_{13} = -7 \qquad C_{23} = -11 \qquad C_{33} = -19$$

$$A^{-1} = -22 \qquad A_{14} \qquad A_{14} \qquad A_{15} \qquad A_$$

$$=\frac{1}{-151}\begin{bmatrix} -132000 & -23000 & -91000 \\ -78000 & +70000 & -143000 \\ -3000 & -85000 & -247000 \end{bmatrix}$$

From the given data, we get the following three equations:

$$x + y + z = 12$$

$$2x + 3y + 3z = 33$$

$$x - 2y + z = 0$$

This system of equations can be written

in the matrix form as

$$\begin{bmatrix} 1 & 1 & 1 \\ 2 & 3 & 3 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 12 \\ 33 \\ 0 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 2 & 3 & 3 \\ 1 & -2 & 1 \end{bmatrix}^{-1} \begin{bmatrix} 12 \\ 33 \\ 0 \end{bmatrix} \dots (1)$$

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 2 & 3 & 3 \\ 1 & -2 & 1 \end{bmatrix}$$

$$|A| = 1(9) - 1(-1) + 1(-7) = 3$$

$$cofA = \begin{bmatrix} 9 & 1 & -7 \\ -3 & 0 & 3 \\ 0 & -1 & 1 \end{bmatrix}$$

$$adjA = \begin{bmatrix} cofA \end{bmatrix} = \begin{bmatrix} 9 & -3 & 0 \\ 1 & 0 & -1 \\ -7 & 3 & 1 \end{bmatrix}$$

$$A^{-1} = \frac{adjA}{|A|} = \frac{1}{3} \begin{bmatrix} 9 & -3 & 0 \\ 1 & 0 & -1 \\ -7 & 3 & 1 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 9 & -3 & 0 \\ 1 & 0 & -1 \\ -7 & 3 & 1 \end{bmatrix} \begin{bmatrix} 12 \\ 33 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 9 & -3 & 0 \\ 1 & 0 & -1 \\ -7 & 3 & 1 \end{bmatrix} \begin{bmatrix} 12 \\ 33 \\ 0 \end{bmatrix}$$
$$\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 9 & -3 & 0 \\ 1 & 0 & -1 \\ -7 & 3 & 1 \end{bmatrix} \begin{bmatrix} 4 \\ 11 \\ 0 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 36 - 33 + 0 \\ 4 + 0 + 0 \\ -28 + 33 + 0 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ 4 \\ 5 \end{bmatrix}$$

An award for organising different festivals in the colony can be included by the management.

Let X, Y and Z be the cash awards for

Honesty, Regularity and Hard work respectively.

As per the data in the question, we get

$$X + Y + Z = 6000$$

$$X + 3Z = 11000$$

$$X - 2Y + 7 = 0$$

The above three simulataneous equations

can be written in the matrix form as

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 0 & 3 \\ 1 & -2 & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 6000 \\ 11000 \\ 0 \end{bmatrix}$$

can be written in the matrix form as
$$\begin{bmatrix}
1 & 1 & 1 \\
1 & 0 & 3 \\
1 & -2 & 1
\end{bmatrix}
\begin{bmatrix}
X \\
Y \\
Z
\end{bmatrix} = \begin{bmatrix}
6000 \\
11000 \\
0
\end{bmatrix}$$

$$\Rightarrow \begin{bmatrix}
X \\
Y \\
Z
\end{bmatrix} = \begin{bmatrix}
1 & 1 & 1 \\
1 & 0 & 3 \\
1 & -2 & 1
\end{bmatrix}
\begin{bmatrix}
6000 \\
11000 \\
0
\end{bmatrix}$$
...(1)
$$A = \begin{bmatrix}
1 & 1 & 1 \\
1 & 0 & 3 \\
1 & -2 & 1
\end{bmatrix}$$
...(1)

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 0 & 3 \\ 1 & -2 & 1 \end{bmatrix}$$

$$|A| = 1(6) - 1(-2) + 1(-2) = 6$$

$$cofA = \begin{bmatrix} 6 & 2 & -2 \\ -3 & 0 & 3 \\ 3 & -2 & -1 \end{bmatrix}$$

Let x, y and z be teh prize amount per person for Resourcefulness, Competence and Determination respectively.

As per the data in the question, we get

$$4x + 3y + 2z = 37000$$

$$5x + 3y + 4z = 47000$$

$$x + y + z = 12000$$

The above three simulataneous equations

can be written in matrix form as

$$\begin{bmatrix} 4 & 3 & 2 \\ 5 & 3 & 4 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 37000 \\ 47000 \\ 12000 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 4 & 3 & 2 \\ 5 & 3 & 4 \\ 1 & 1 & 1 \end{bmatrix}^{-1} \begin{bmatrix} 37000 \\ 47000 \\ 12000 \end{bmatrix} \dots (1)$$

$$A = \begin{bmatrix} 4 & 3 & 2 \\ 5 & 3 & 4 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 4(-1) - 3(1) + 2(2) = -3$$

$$cof A = \begin{bmatrix} -1 & -1 & 2 \\ -1 & 2 & -1 \\ 6 & -6 & -3 \end{bmatrix}$$

$$adjA = (cofA)^{T} = \begin{bmatrix} -1 & -1 & 6 \\ -1 & 2 & -6 \\ 2 & -1 & -3 \end{bmatrix}$$

$$\Rightarrow \begin{vmatrix} Y \\ Z \end{vmatrix} = \begin{vmatrix} 5 & 3 & 4 \\ 1 & 1 & 1 \end{vmatrix} \begin{vmatrix} 47000 \\ 12000 \end{vmatrix} \dots (1)$$

$$A = \begin{bmatrix} 4 & 3 & 2 \\ 5 & 3 & 4 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 4(-1) - 3(1) + 2(2) = -3$$

$$\cot A = \begin{bmatrix} -1 & -1 & 2 \\ -1 & 2 & -1 \\ 6 & -6 & -3 \end{bmatrix}$$

$$adjA = (\cot A)^{T} = \begin{bmatrix} -1 & -1 & 6 \\ -1 & 2 & -6 \\ 2 & -1 & -3 \end{bmatrix}$$

$$A^{-1} = \frac{adjA}{|A|} = \frac{1}{-3} \begin{bmatrix} -1 & -1 & 6 \\ -1 & 2 & -6 \\ 2 & -1 & -3 \end{bmatrix}$$
From (1)

From (1)

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \frac{1}{-3} \begin{bmatrix} -1 & -1 & 6 \\ -1 & 2 & -6 \\ 2 & -1 & -3 \end{bmatrix} \begin{bmatrix} 37000 \\ 47000 \\ 12000 \end{bmatrix}$$

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \frac{1}{-3} \begin{bmatrix} -12000 \\ -15000 \\ -9000 \end{bmatrix} = \begin{bmatrix} 4000 \\ 5000 \\ 3000 \end{bmatrix}$$

The values x, y and z describe the amount of prizes per person for resourcefulness, competence and determination.

Let x, y and z be the prize amount per person for adaptibility, carefulness and calmness respectively.

As per the given data, we get

$$2x + 4y + 3z = 29000$$

$$5x + 2y + 3z = 30500$$

$$x + y + z = 9500$$

The above three simulataneous equations can be written in the matrix form as

$$\begin{bmatrix} 2 & 4 & 3 \\ 5 & 2 & 3 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 29000 \\ 30500 \\ 9500 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 2 & 4 & 3 \end{bmatrix}^{1} \begin{bmatrix} 29000 \\ 30500 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 9500 \end{bmatrix} \dots (1)$$

$$A = \begin{bmatrix} 2 & 4 & 3 \\ 5 & 2 & 3 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 2(-1) - 4(2) + 3(3) = -1$$

$$cofA = \begin{bmatrix} -1 & -2 & 3 \\ -1 & -1 & 2 \\ 6 & 9 & -16 \end{bmatrix}$$

$$adjA = (cofA)^T = \begin{bmatrix} -1 & -1 & 6 \\ -2 & -1 & 9 \\ 3 & 2 & -16 \end{bmatrix}$$

$$\Rightarrow \begin{vmatrix} Y \\ Z \end{vmatrix} = \begin{vmatrix} 5 & 2 & 3 \\ 1 & 1 & 1 \end{vmatrix} \begin{vmatrix} 30500 \\ 9500 \end{vmatrix} \dots (1)$$

$$A = \begin{bmatrix} 2 & 4 & 3 \\ 5 & 2 & 3 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 2(-1) - 4(2) + 3(3) = -1$$

$$cofA = \begin{bmatrix} -1 & -2 & 3 \\ -1 & -1 & 2 \\ 6 & 9 & -16 \end{bmatrix}$$

$$adjA = (cofA)^T = \begin{bmatrix} -1 & -1 & 6 \\ -2 & 1 & 9 \\ 3 & 2 & -16 \end{bmatrix}$$

$$A^{-1} = \frac{adjA}{|A|} = \frac{\begin{bmatrix} -1 & -1 & 6 \\ -2 & 1 & 9 \\ 3 & 2 & -16 \end{bmatrix}}{\begin{bmatrix} -1 & 1 & 6 \\ -2 & 1 & 9 \\ 3 & 2 & -16 \end{bmatrix}} = \begin{bmatrix} 1 & 1 & -6 \\ 2 & 1 & -9 \\ -3 & -2 & 16 \end{bmatrix}$$

From (1)

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 1 & 1 & -6 \\ 2 & 1 & -9 \\ -3 & -2 & 16 \end{bmatrix} \begin{bmatrix} 29000 \\ 30500 \\ 9500 \end{bmatrix} \dots (1)$$

$$\begin{bmatrix} X \\ Y \end{bmatrix} = \begin{bmatrix} 2500 \\ 3000 \\ 2 \end{bmatrix}$$

Let x, y and z be the prize amount per student for sincerity, truthfulness and helpfulness respectively.

As per the data in the question, we get

$$3x + 2y + z = 1600$$

$$4x + y + 3z = 2300$$

$$x + y + z = 900$$

The above three simulataneous equations can be written in matrix form as

$$\begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1600 \\ 2300 \\ 900 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix}^{1} \begin{bmatrix} 1600 \\ 2300 \\ 900 \end{bmatrix} \dots (1)$$

$$A = \begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 3(-2) - 2(1) + 1(3) = -5$$

$$cofA = \begin{bmatrix} -2 & -1 & 3 \\ -1 & 2 & -1 \\ 5 & -5 & -5 \end{bmatrix}$$

$$adjA = (cofA)^{T} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}$$

$$A^{-1} = \frac{adjA}{|A|} = \frac{\begin{bmatrix} -2 & -1 & 3 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}}{-5}$$

$$A = \begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 3(-2) - 2(1) + 1(3) = -5$$

$$cof A = \begin{bmatrix} -2 & -1 & 3 \\ -1 & 2 & -1 \\ 5 & -5 & -5 \end{bmatrix}$$

$$adj A = (cof A)^T = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}$$

$$A^{-1} = \frac{adj A}{|A|} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}$$
From (1)
$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix} \begin{bmatrix} 1600 \\ 2300 \\ 900 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix} \begin{bmatrix} -320 \\ -460 \\ -180 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 200 \\ 300 \\ 400 \end{bmatrix}$$

Excellence in extra-curricular activities should be another value considered for an award.

x, y and z be prize amount per student for

Discipline, Politeness and Punctuality respectively.

As per the data in the question, we get

$$3x+2y+z=1000$$

$$4x+y+3z=1500$$

$$x+y+z=600$$

The above three simulataneous equations

can be written in matrix form as

$$\begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1000 \\ 1500 \\ 600 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix}^{1} \begin{bmatrix} 1000 \\ 1500 \\ 600 \end{bmatrix} \dots (1)$$

$$A = \begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 3(-2) - 2(1) + 1(3) = -5$$

$$cofA = \begin{bmatrix} -2 & -1 & 3 \\ -1 & 2 & -1 \\ 5 & -5 & -5 \end{bmatrix}$$

$$adjA = (cofA)^{T} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}$$

$$A = \begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 3(-2) - 2(1) + 1(3) = -5$$

$$cofA = \begin{bmatrix} -2 & -1 & 3 \\ -1 & 2 & -1 \\ 5 & -5 & -5 \end{bmatrix}$$

$$adjA = (cofA)^{T} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}$$

$$A^{-1} = \frac{adjA}{|A|} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}$$
From (1)

From (1)

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix} \begin{bmatrix} 1000 \\ 1500 \\ 600 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix} \begin{bmatrix} -200 \\ -300 \\ -120 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 100 \\ 200 \\ 300 \end{bmatrix}$$

x, y and z be prize amount per student for

Tolerance, Kindness and Leadership respectively.

As per the data in the question, we get

$$3x+2y+z=2200$$

$$4x+y+3z=3100$$

$$x+y+z=1200$$

The above three simulataneous equations

can be written in matrix form as

$$\begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2200 \\ 3100 \\ 1200 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix}^{1} \begin{bmatrix} 2200 \\ 3100 \\ 1200 \end{bmatrix} \dots (1)$$

$$A = \begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 3(-2) - 2(1) + 1(3) = -5$$

$$cof A = \begin{bmatrix} -2 & -1 & 3 \\ -1 & 2 & -1 \\ 5 & -5 & -5 \end{bmatrix}$$

$$adjA = (cofA)^{T} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}$$

$$A = \begin{bmatrix} 3 & 2 & 1 \\ 4 & 1 & 3 \\ 1 & 1 & 1 \end{bmatrix}$$

$$|A| = 3(-2) - 2(1) + 1(3) = -5$$

$$cof A = \begin{bmatrix} -2 & -1 & 3 \\ -1 & 2 & -1 \\ 5 & -5 & -5 \end{bmatrix}$$

$$adj A = (cof A)^{T} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}$$

$$A^{-1} = \frac{adj A}{|A|} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix}$$
From (1)

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix} \begin{bmatrix} 2200 \\ 3100 \\ 1200 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} -2 & -1 & 5 \\ -1 & 2 & -5 \\ 3 & -1 & -5 \end{bmatrix} \begin{bmatrix} -440 \\ -620 \\ -240 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 300 \\ 400 \\ 500 \end{bmatrix}$$

Let the amount deposited be x, y and z respectively.

As per the data in the question, we get

$$x + y + z = 7000$$

$$5\%x + 8\%y + 8.5\%z = 550$$

$$\Rightarrow 5x + 8y + 8.5z = 55000$$

$$x - y = 0$$

The above equations can be written in matrix form as

$$\begin{bmatrix} 1 & 1 & 1 \\ 5 & 8 & 8.5 \\ 1 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 7000 \\ 55000 \\ 0 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 5 & 8 & 8.5 \\ 1 & -1 & 0 \end{bmatrix}^{-1} \begin{bmatrix} 7000 \\ 55000 \\ 0 \end{bmatrix} \dots (1)$$

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 5 & 8 & 8.5 \\ 1 & -1 & 0 \end{bmatrix}$$

$$|A| = 1(8.5) - 1(-8.5) + 1(-13) = 4$$

$$cofA = \begin{bmatrix} 8.5 & 8.5 & -13 \\ -1 & -1 & 2 \\ 0.5 & -3.5 & 3 \end{bmatrix}$$

$$|A| = 1(8.5) - 1(-8.5) + 1(-13) = 4$$

$$cofA = \begin{bmatrix} 8.5 & 8.5 & -13 \\ -1 & -1 & 2 \\ 0.5 & -3.5 & 3 \end{bmatrix}$$

$$adjA = (cofA)^{T} = \begin{bmatrix} 8.5 & 8.5 & -13 \\ -1 & -1 & 2 \\ 0.5 & -3.5 & 3 \end{bmatrix}$$

$$adjA = (cofA)^{T} = \begin{bmatrix} 8.5 & 8.5 & -13 \\ -1 & -1 & 2 \\ 0.5 & -3.5 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 8.5 & -1 & 0.5 \\ 8.5 & -1 & -3.5 \\ -13 & 2 & 3 \end{bmatrix}$$

$$adjA = (cofA)^{T} = \begin{bmatrix} 8.5 & 8.5 & -13 \\ -1 & -1 & 2 \\ 0.5 & -3.5 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 8.5 & -1 & 0.5 \\ 8.5 & -1 & -3.5 \\ -13 & 2 & 3 \end{bmatrix}$$

$$A^{-1} = \frac{adjA}{|A|} = \frac{1}{4} \begin{bmatrix} 8.5 & -1 & 0.5 \\ 8.5 & -1 & -3.5 \\ -13 & 2 & 3 \end{bmatrix}$$

From (1)

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{4} \begin{bmatrix} 8.5 & -1 & 0.5 \\ 8.5 & -1 & -3.5 \\ -13 & 2 & 3 \end{bmatrix} \begin{bmatrix} 7000 \\ 55000 \\ 0 \end{bmatrix}$$

$$=\frac{1}{4} \begin{bmatrix} 4500 \\ 4500 \\ 19000 \end{bmatrix} = \begin{bmatrix} 1125 \\ 1125 \\ 4750 \end{bmatrix}$$

Hence, the amounts deposited in the three accounts are 1125, 1125 and 4750 respectively.