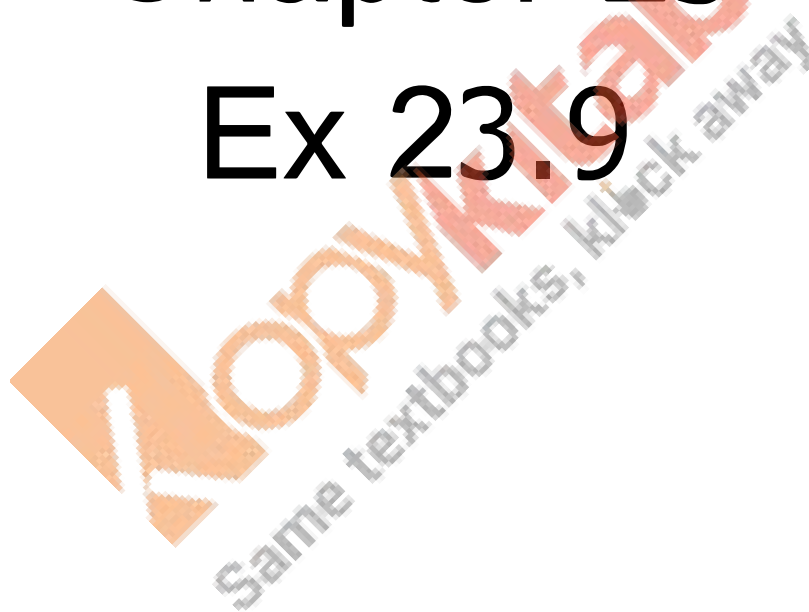


RD Sharma
Solutions
Class 11 Maths
Chapter 23
Ex 23.9



Straight lines Ex 23.9 Q1

(i) Slope intercept form ($y = mx + c$)

$$\sqrt{3}x + y + 2 = 0$$

$$\Rightarrow y = -\sqrt{3}x - 2$$

$$\Rightarrow m = -\sqrt{3}, c = -2$$

$$y\text{-intercept} = -2, \text{ slope} = -\sqrt{3}$$

(ii) Intercept form ($\frac{x}{a} + \frac{y}{b} = 1$)

$$\sqrt{3}x + y + 2 = 0$$

$$\Rightarrow \sqrt{3}x + y = -2$$

$$\Rightarrow \frac{\sqrt{3}x}{-2} + \frac{y}{-2} = 1$$

$$\Rightarrow \frac{x}{-\frac{2}{\sqrt{3}}} + \frac{y}{-2} = 1$$

$$\Rightarrow x \text{ intercept} = -\frac{2}{\sqrt{3}}, y \text{ intercept} = -2$$

(iii) Normal form ($x \cos \alpha + y \sin \alpha = p$)

$$\sqrt{3}x + y + 2 = 0$$

$$\Rightarrow -\sqrt{3}x - y = 2$$

$$\Rightarrow \left(\frac{-\sqrt{3}}{2}\right)x + \left(\frac{-1}{2}\right)y = 1$$

$$\Rightarrow \cos \alpha = \frac{-\sqrt{3}}{2} = \cos 210^\circ \text{ and } \sin \alpha = \frac{-1}{2} = \sin 210^\circ$$

$$\Rightarrow p = 1, \alpha = 210^\circ$$

Straight lines Ex 23.9 Q2(i)

$$x + \sqrt{3}y - 4 = 0$$

Divide the equation by 2, we get

$$\frac{1}{2}x + \frac{\sqrt{3}}{2}y = 2$$

$$x \cos 60 + y \sin 60 = 2$$

So, $p=2$ and $\omega=60$

Straight lines Ex 23.9 Q2(ii)

$$x + y + \sqrt{2} = 0$$

$$x + y = -\sqrt{2}$$

Dividing each term by $\sqrt{(1)^2 + (1)^2} = \sqrt{2}$

$$\frac{x}{\sqrt{2}} + \frac{y}{\sqrt{2}} = -1$$

$$\frac{-x}{\sqrt{2}} - \frac{y}{\sqrt{2}} = 1$$

Comparing with $x \cos \alpha + y \sin \alpha = p$

$$\cos \alpha = \frac{-1}{\sqrt{2}}, \quad \sin \alpha = \frac{-1}{\sqrt{2}}, \quad p = 1$$

Both are negative

α is in III quadrant

$$\Rightarrow \alpha = \pi \frac{\pi}{4} = \frac{5\pi}{4} = 225^\circ$$

Straight lines Ex 23.9 Q2(iii)

$$x - y + 2\sqrt{2} = 0$$

$$-x + y = 2\sqrt{2}$$

Dividing each term by $\sqrt{(1)^2 + (1)^2} = \sqrt{2}$

$$\frac{-x}{\sqrt{2}} + \frac{y}{\sqrt{2}} = 2$$

Comparing with $x \cos \alpha + y \sin \alpha = p$

$$\cos \alpha = \frac{-1}{\sqrt{2}}, \quad \sin \alpha = \frac{1}{\sqrt{2}}, \quad p = 2$$

α is in II quadrant

$$\Rightarrow \alpha = \frac{\pi}{4} + \frac{\pi}{2} = \frac{3\pi}{4} = 135^\circ, \quad p = 2$$

Straight lines Ex 23.9 Q2(iv)

$$x - 3 = 0$$

$$x = 3$$

Comparing with $x \cos \alpha + y \sin \alpha = p$

$$\cos \alpha = 1$$

$$= \cos 0$$

$$\Rightarrow \alpha = 0$$

$$p = 3$$

Straight lines Ex 23.9 Q2(v)

$$y - 2 = 0$$

$$y = 2$$

Comparing with $x \cos \alpha + y \sin \alpha = p$

$$\sin \alpha = 1$$

$$\alpha = \frac{\pi}{2}, \quad p = 2$$

Straight lines Ex 23.9 Q3

$$\frac{x}{a} + \frac{y}{b} = 1$$

The slope intercept form is

$$y = mx + c$$

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$bx + ay = ab$$

$$ay = -bx + ab$$

$$y = \frac{-bx}{a} + b$$

Thus y -intercept is b .

$$\text{Slope} = \frac{-b}{a}$$

Kopykitab
Same textbooks, click away

Straight lines Ex 23.9 Q4

The normal form is obtained by dividing each term of the equation by $\sqrt{a^2 + b^2}$,

a = coefficient of x

b = coefficient of y

$$3x - 4y + 4 = 0 \quad \text{--- (1)}$$

$$3x - 4y = -4$$

$$-3x + 4y = 4$$

Dividing each term by $\sqrt{(-3)^2 + (4)^2} = \sqrt{9 + 16} = \sqrt{25} = 5$

$$\frac{-3}{5}x + \frac{4}{5}y = \frac{4}{5}$$

$$\Rightarrow p = \frac{4}{5} \quad \text{for equation (1)}$$

Also

$$2x + 4y - 5 = 0 \quad \text{--- (2)}$$

$$2x + 4y = 5$$

Dividing each term by $\sqrt{(2)^2 + (4)^2} = \sqrt{4 + 16} = \sqrt{20}$

$$\frac{2x}{\sqrt{20}} + \frac{4y}{\sqrt{20}} = \frac{5}{\sqrt{20}}$$

$$p = \frac{5}{\sqrt{20}} = \frac{5}{4.4} \quad \text{for equation (2)}$$

Comparing p of (1) and (2)

We conclude that $3x - 4y + 4 = 0$ is nearest to origin

Straight lines Ex 23.9 Q5

Reduce $4x + 3y + 10 = 0$ to perpendicular form

$$4x + 3y = -10$$

$$-4x - 3y = 10$$

Dividing each term by $\sqrt{(-4)^2 + (-3)^2} = \sqrt{16 + 9} = \sqrt{25} = 5$

$$\frac{-4}{5}x - \frac{3}{5}y = \frac{10}{5} = 2$$

$$\Rightarrow p_1 = 2 \quad \text{--- (1)}$$

$$5x - 12y + 26 = 0$$

$$5x - 12y = -26$$

Dividing each term by $\sqrt{(-5)^2 + (-12)^2} = \sqrt{25 + 144} = \sqrt{169} = 13$

$$\frac{-5}{13}x + \frac{12}{13}y = \frac{-26}{13} = -2$$

$$\Rightarrow p_2 = 2 \quad \text{--- (2)}$$

$$7x + 24y = 50$$

Dividing each term by $\sqrt{(7)^2 + (24)^2} = \sqrt{49 + 576} = \sqrt{625} = 25$

$$\frac{7}{25}x + \frac{24}{25}y = \frac{50}{25} = 2$$

$$\Rightarrow p_3 = 2 \quad \text{--- (3)}$$

Hence, origin is equidistant from all three lines.

Straight lines Ex 23.9 Q6

$$\sqrt{3}x + y + 2 = 0$$

$$\sqrt{3}x + y = 2$$

$$-\sqrt{3}x - y = 2 \text{ --- (1)}$$

So,

$$\cos \theta = -\sqrt{3}, \sin \theta = -1$$

$$\tan \theta = \frac{1}{\sqrt{3}}$$

$$\theta = \left(\pi + \frac{\pi}{6} \right)$$

$$= 180^\circ + 30^\circ$$

$$\theta = 210^\circ$$

$$p = 2 \quad \left[\text{From equation (1)} \right]$$

Straight lines Ex 23.9 Q7

The intercept form of equation is

$$\frac{x}{a} + \frac{y}{b} = 1$$

$$3x - 2y + 6 = 0$$

$$3x - 2y = -6$$

$$\frac{-3x}{-6} - \frac{2y}{-6} = 1$$

$$\frac{x}{-6} + \frac{y}{-3} = 1$$

$$\frac{x}{-2} + \frac{y}{3} = 1$$

$$\Rightarrow x\text{-intercept} = a = -2$$

$$y\text{-intercept} = b = 3$$

Straight lines Ex 23.9 Q8

Perpendicular distance from the origin to the line is 5, so

$$x \cos \alpha + y \sin \alpha = 5$$

$$y \sin \alpha = -x \cos \alpha + 5$$

$$y = -\frac{\cos \alpha}{\sin \alpha} x + 5$$

$$y = -\cot \alpha x + 5$$

Comparing with $y = mx + c$

$$m = -\cot \alpha$$

$$-1 = -\cot \alpha$$

$$\cot \alpha = 1$$

$$\alpha = \frac{\pi}{4}$$

So, equation of line is

$$x \cos \frac{\pi}{4} + y \sin \frac{\pi}{4} = 5$$

$$\frac{x}{\sqrt{2}} + \frac{y}{\sqrt{2}} = 5$$

$$x + y = 5\sqrt{2}$$

Kopykitab
Same textbooks, click away