

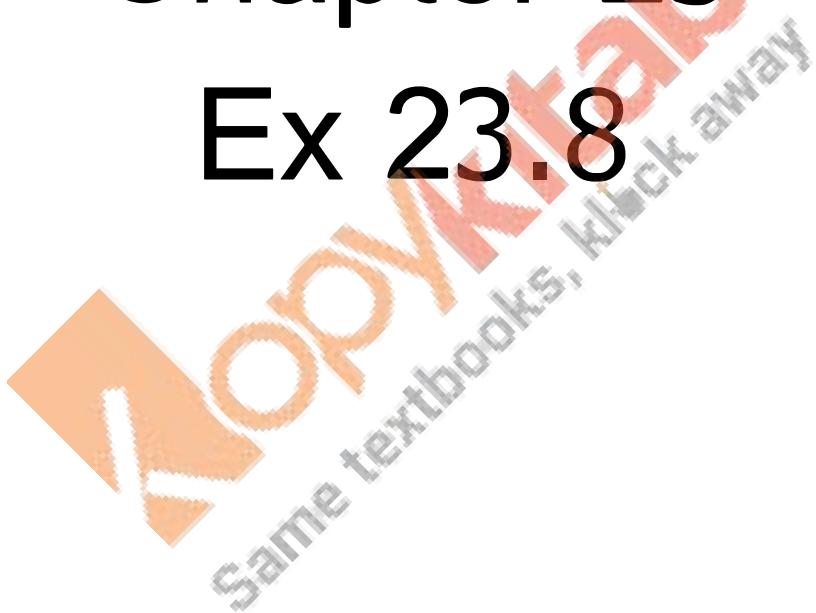
# RD Sharma

## Solutions

### Class 11 Maths

#### Chapter 23

##### Ex 23.8



### Straight lines Ex 23.8 Q1

The equation of line through  $(1, 2)$  and making an angle of  $60^\circ$  with the x-axis is

$$\frac{x-1}{\cos 60^\circ} = \frac{y-2}{\sin 60^\circ} = r$$

$$\frac{x-1}{\frac{1}{2}} = \frac{y-2}{\frac{\sqrt{3}}{2}} = r$$

Where  $r$  is the distance of any point on the line from  $A(1, 2)$ .

The coordinates of  $P$  on the line are

$$\left(1 + \frac{1}{2}r, 2 + \frac{\sqrt{3}}{2}r\right)$$

and

$P$  lies on  $x + y = 6$

$$\therefore 1 + \frac{r}{2} + 2 + \frac{\sqrt{3}r}{2} = 6$$

$$\text{or } r = \frac{6}{1 + \sqrt{3}} = 3(\sqrt{3} - 1)$$

$$\text{Hence length } AP = 3(\sqrt{3} - 1)$$

### Straight lines Ex 23.8 Q2

The equation of line is

$$\frac{x-3}{\cos \frac{\pi}{6}} = \frac{y-4}{\sin \frac{\pi}{6}} = \pm r$$

$$\text{or } x = \pm \frac{\sqrt{3}}{2}r + 3 \text{ and } y = \pm \frac{1}{2}r + 4$$



$$Q\left(\pm \frac{\sqrt{3}r}{2} + 3, \pm \frac{r}{2} + 4\right) \text{ lie in } 12x + 5y + 10 = 0$$

$$\therefore 12\left(\pm \frac{\sqrt{3}r}{2} + 3\right) + 5\left(\pm \frac{r}{2} + 4\right) + 10 = 0$$

$$\pm \frac{12\sqrt{3}r}{2} + 36 \pm \frac{5r}{2} + 20 + 10 = 0$$

$$r = \frac{\pm 132}{5 + 12\sqrt{3}}$$

Hence, length  $PQ$  is  $\frac{132}{12\sqrt{3} + 5}$

### Straight lines Ex 23.8 Q3

The equation of line is

$$\frac{x - 2}{\cos \alpha} = \frac{y - 1}{\sin \alpha} = r$$

$$\Rightarrow \frac{x - 2}{\frac{1}{\sqrt{2}}} = \frac{y - 1}{\frac{1}{\sqrt{2}}} = r$$

$$\text{or } x = \frac{1}{\sqrt{2}}r + 2, y = \frac{1}{\sqrt{2}}r + 1$$

$$B\left(\frac{r}{\sqrt{2}} + 2, \frac{r}{\sqrt{2}} + 1\right) \text{ lie on } x + 2y + 1 = 0$$

$$\therefore \frac{r}{\sqrt{2}} + 2 + \frac{2r}{\sqrt{2}} + 2 + 1 = 0$$

$$\frac{3r}{\sqrt{2}} = \pm 5$$

$$r = \frac{5\sqrt{2}}{3}$$

The length  $AB$  is  $\frac{5\sqrt{2}}{3}$  units

### Straight lines Ex 23.8 Q4

The required line is parallel to  $3x - 4y + 1 = 0$

$$\therefore \text{Slope of the line} = \text{slope of } 3x - 4y + 1 = \frac{-3}{-4}$$

$$\tan \alpha = \frac{3}{4}$$

$$\Rightarrow \sin \alpha = \frac{3}{5} \text{ and } \cos \alpha = \frac{4}{5}$$

The equation of line is

$$\frac{x+4}{\cos \alpha} + \frac{y+1}{\sin \alpha} = r$$

$$\Rightarrow \frac{x-4}{\frac{4}{5}} + \frac{y+1}{\frac{3}{5}} = \pm 5$$

$$\Rightarrow x = 8 \text{ and } y = 2$$

or

$$x = 0 \text{ and } y = -4$$

$\therefore (8, 2)$  and  $(0, -4)$  are coordinates of two points on the line which are at a distance of 5 units from  $(4, 1)$

### Straight lines Ex 23.8 Q5

The equation of line is

$$\frac{x-x_1}{\cos\theta} = \frac{y-y_1}{\sin\theta} = \pm r$$

or

$$x = x_1 \pm r \cos\theta \text{ and } y = y_1 \pm r \sin\theta$$

Q  $(x_1 \pm r \cos\theta, y_1 \pm r \sin\theta)$  lie in  $ax + by + c = 0$

$$\Rightarrow a(x_1 + r \cos\theta) + b(y_1 + r \sin\theta) + c = 0$$

$$\Rightarrow \pm r(a \cos\theta + b \sin\theta) = -c - ax_1 - by_1$$

$$\Rightarrow -r = \left| \frac{ax_1 + by_1 + c}{a \cos\theta + b \sin\theta} \right|$$

### Straight lines Ex 23.8 Q6

Equation of line is

$$\frac{x-2}{\cos 45^\circ} = \frac{y-3}{\sin 45^\circ} = r$$

$$x = \frac{r}{\sqrt{2}} + 2 \quad \text{and} \quad y = \frac{r}{\sqrt{2}} + 3$$

$P\left(\frac{r}{\sqrt{2}} + 2, \frac{r}{\sqrt{2}} + 3\right)$  lie on  $2x - 3y + 9 = 0$

$$\therefore 2\left(\frac{r+2\sqrt{2}}{\sqrt{2}}\right) - 3\left(\frac{r+3\sqrt{2}}{\sqrt{2}}\right) + 9 = 0$$

$$\Rightarrow 2r + 4\sqrt{2} - 3r - 9\sqrt{2} + 9\sqrt{2} = 0$$

$$\Rightarrow r = 4\sqrt{2}$$

$\therefore$  The point  $(2, 3)$  is at a distance of  $4\sqrt{2}$  from  $2x - 3y + 9 = 0$

### Straight lines Ex 23.8 Q7

Equation of the required line is

$$\frac{x-3}{\cos \alpha} = \frac{y-5}{\sin \alpha} = r \quad \dots \dots (1)$$

$$\tan \alpha = \frac{1}{2} \Rightarrow \cos \alpha = \frac{2}{\sqrt{5}} \quad \text{and} \quad \sin \alpha = \frac{1}{\sqrt{5}}$$

$\therefore$  equation is

$$\frac{x-3}{\frac{2}{\sqrt{5}}} = \frac{y-5}{\frac{1}{\sqrt{5}}} = r$$

$$\text{or } x = \frac{2}{\sqrt{5}}r + 3, y = \frac{1}{\sqrt{5}}r + 5$$

$P\left(\frac{2r}{\sqrt{5}} + 3, \frac{r}{\sqrt{5}} + 5\right)$  lie on  $2x + 3y = 14$

$$\therefore \frac{4r}{\sqrt{5}} + 6 + \frac{3r}{\sqrt{5}} + 15 = 14$$

$$\frac{7r}{\sqrt{5}} = \pm 17$$

$$r = \pm\sqrt{5}$$

$$r = \sqrt{5} \quad (r \neq -\sqrt{5})$$

$\therefore$  Distance of  $(3, 5)$  from  $2x + 3y = 14$  is  $\sqrt{5}$  units

### Straight lines Ex 23.8 Q8

$$\text{Slope of the line} = \tan \alpha = \frac{3}{4}$$

$$\therefore \sin \alpha = \frac{3}{5} \quad \text{and} \quad \cos \alpha = \frac{4}{5}$$

$\therefore$  Equation of line is

$$\frac{x-2}{\cos \alpha} = \frac{y-5}{\sin \alpha} = r$$

$$\Rightarrow \frac{x-2}{\frac{4}{5}} = \frac{y-5}{\frac{3}{5}} = r$$

$$\text{or } x = \frac{4r}{5} + 2 \text{ and } y = \frac{3r}{5} + 5$$

then  $P\left(\frac{4r}{5} + 2, \frac{3r}{5} + 5\right)$  lie on  $3x + y + 4 = 0$

$$\therefore 3\left(\frac{4r}{5} + 2\right) + \left(\frac{3r}{5} + 5\right) + 4 = 0$$

$$\frac{15}{5}r = \pm 15$$

$$r = \pm \frac{15 \times 5}{15}$$
$$= 5 \text{ units}$$