RD SHARMA
Solutions
Class 10 Maths
Chapter 1
Ex 1.4

Q.1: Find the LCM and HCF of the following pairs of integers and verify that LCM x HCF = product of the integers:

- (i) 26 and 91
- (ii) 510 and 92
- (iii) 336 and 54

Sol:

TO FIND: LCM and HCF of following pairs of integers

TO VERIFY: L.C.M x H.C.F = product of the numbers

(i) 26 and 91

Let us first find the factors of 26 and 91

 $26 = 2 \times 13$

 $91 = 7 \times 13$

L.C.M of 26, and $91 = 2 \times 7 \times 13$

L.C.M of 26, and 91 = 182

H.C.F of 26, and 91 = 182

We know that, L.C.M x H.C.F = First number x Second number

 $182 \times 13 = 26 \times 91 = 2366 = 2366$

Hence verified

(ii) 510 and 92

Let us first find the factors of 510 and 92

 $510 = 2 \times 3 \times 5 \times 17$

 $92 = 2 \times 2 \times 23$

L.C.M of 510 and $92 = 2 \times 2 \times 3 \times 5 \times 23 \times 17$

L.C.M of 510 and 92 = 23460

H.C.F of 510 and 92 = 2

We know that, L.C.M x H.C.F = First Number x Second Number

 $23460 \times 2 = 510 \times 92$

46920 = 46920

Hence verified.

(iii) 336 and 54

Let us first find the factors of 336 and 54

 $336 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 7$

 $54 = 2 \times 3 \times 3 \times 3$

L.C.M of 336 and $54 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 7$

L.C.M of 336 and 54 = 3024

H.C.F of 336 and 54 = 6

We know that, L.C.M x H.C.F = First Number x Second Number

 $3024 \times 6 = 336 \times 54$

18144 = 18144

Hence verified

Q.2: Find the LCM and HCF of the following integers by applying the prime factorization method:

- (i) 12, 15 and 21
- (ii) 17, 23 and 29
- (iii) 8, 9 and 25
- (iv) 40, 36 and 126
- (v) 84, 90 and 120
- (vi) 24, 15 and 36

Sol:

TO FIND: LCM and HCF of following pairs of integers

(i) 15, 12 and 21

Let us first find the factors of 15, 12 and 21

 $12 = 2 \times 2 \times 3$

$$15 = 3 \times 5$$

$$21 = 3 \times 7$$

L.C.M of 12, 15 and
$$21 = 2 \times 2 \times 3 \times 5 \times 7$$

L.C.M of 12, 15 and
$$21 = 420$$

H.C.F of 12, 15 and
$$21 = 3$$

(ii) 17, 23 and 29

Let us first find the factors of 17, 23 and 29

$$17 = 1 \times 17$$

$$23 = 1 \times 23$$

$$29 = 1 \times 29$$

L.C.M of 17, 23 and
$$29 = 1 \times 17 \times 23 \times 29$$

H.C.F of 17, 23 and
$$29 = 1$$

(iii) 8, 9 and 25

Let us first find the factors of 8, 9 and 25

$$8 = 2 \times 2 \times 2$$

$$9 = 3 \times 3$$

$$25 = 5 \times 5$$

L.C.M of 8, 9 and 25 =
$$2^3 \times 3^2 \times 5^2$$

(iv) 40, 36 and 126

Let us first find the factors of 40, 36 and 126

$$40 = 2^3 \times 5$$

$$36 = 2^3 \times 3^2$$

$$126 = 2 \times 3 \times 3 \times 7$$

L.C.M of 40, 36 and $126 = 2^3 \times 3^2 \times 5 \times 7$

L.C.M of 40, 36 and 126 = 2520

H.C.F of 40, 36 and 126 = 2

(v) 84, 90 and 120

Let us first find the factors of 84, 90 and 120

$$84 = 2 \times 2 \times 3 \times 7$$

$$90 = 2 \times 3 \times 3 \times 5$$

$$120 = 2 \times 2 \times 2 \times 3 \times 5$$

L.C.M of 84, 90 and $120 = 2^3 \times 3^2 \times 5 \times 7$

L.C.M of 84, 90 and 120 = 2520

H.C.F of 84, 90 and 120 = 6

(vi) 24, 15 and 36

Let us first find the factors of 24, 15 and 36

$$24 = 2^3 \times 3$$

$$15 = 3 \times 5$$

$$36 = 2 \times 2 \times 3 \times 3$$

LCM of 24, 15 and 36 = $2 \times 2 \times 2 \times 3 \times 3 \times 5$

LCM of 24, 15 and 36 = 360

HCF of 24, 15 and 36 = 3

Q.3: Given that HCF (306, 657) = 9, find LCM (306, 657)

Sol:

Given:

HCF of two numbers 306 and 657 is 9

To find: LCM of number
We know that,

LCM x HCF = first number x second number

 $LCM \times 9 = 306 \times 657$

LCM=306x6579=22338LCM = $\frac{306x657}{9}$ = 22338

Q.4: Can two numbers have 16 as their HCF and 380 as their as their LCM? Give reason.

Sol:

To find: can two numbers have 16 as their HCF and 380 as their LCM

On dividing 380 by 16 we get 23 as the quotient and 12 as the remainder

Since LCM is not exactly divisible by the HCF, two number cannot have 16 as their HCF and 380 as their LCM

Q.5: The HCF of two numbers is 145 and their LCM is 2175. If one number is 725, find the other.

Sol:

Given:

LCM and HCF of two numbers 145 and 2175 respectively.

If one number is 725

To find: other number

We know that,

LCM x HCF = first number x second number

 $2175 \times 145 = 725 \times \text{second number}$

LCM=2175x145725=435LCM = $\frac{2175x145}{725}$ = 435

Q.6: The HCF of two numbers is 16 and their LCM is 3072. Find the LCM.

Sol:

Given: HCF of two numbers is 16. If the product of the numbers is 3072

To find: LCM of number

We know that,

LCM x HCF = first number x second number

 $LCM \times 16 = 3072$

$$LCM = 307216 = 192LCM = \frac{3072}{16} = 192$$

Q.7: The LCM and HCF of two numbers are 180 and 6 respectively. If one of the numbers is 30, find the other number.

Sol:

Given:

LCM and HCF of two numbers 180 and 6 respectively.

If one number is 30

To find: other number

We know that,

LCM x HCF = first number x second number

 $180 \times 6 = 30 \times \text{second number}$

secondnumber= $180 \times 630 = 36$ secondnumber = $\frac{180 \times 6}{30} = 36$

Q.8: Find the smallest number which when increased by 17 is exactly divisible by both 520 and 468.

Sol:

TO FIND: Smallest number which when increased by 17 is exactly divisible by both 520 and 468. L.C.M OF 520 and 468

 $520 = 23 \times 5 \times 13$

 $468 = 2 \times 2 \times 3 \times 3 \times 13$

LCM of 520 and $468 = 23 \times 32 \times 5 \times 13 = 4680$

Hence 4680 is the least number which exactly divides 520 and 468 i.e. we will get a remainder of 0 in this case. But we need the Smallest number which when increased by 17 is exactly divided by 520 and 468.

Therefore = 4680 - 17 = 46631

Hence 4663 is Smallest number which when increased by 17 is exactly divisible by both 520 and 468.

Q.9: Find the smallest number which leaves remainders 8 and 12 when divided by 28 and 32 respectively.

Sol:

TO FIND: The smallest number which leaves remainders 8 and 12 when divided by 28 and 32 respectively.

L.C.M of 28 and 32.

 $28 = 2 \times 2 \times 7$

 $32 = 2^5$

L.C.M of 28. and $32 = 2^5 \times 7 = 224$

Hence 224 is the least number which exactly divides 28 and 32 i.e. we will get a remainder of 0 in this case. But we need the smallest number which leaves remainders 8 and 12 when divided by 28 and 32 respectively.

Therefore = 224 - 8 - 12 = 204

Hence 2041 is the smallest number which leaves remainders 8 and 12 when divided by 28 and 32 respectively

Q.10: What is the smallest number that, when divided by 35, 56 and 91 leaves remainders of 7 in each case?

Sol:

TO FIND: Smallest number that. When divided by 35, 56 and 91 leaves remainder of 7 in each case L.C.M OF 35, 56 and 91

 $35 = 5 \times 7$

 $56 = 2^3 \times 7$

 $91 = 13 \times 7$

L.C.M of 35, 56 and $91 = 2^3 \times 7 \times 5 \times 13 = 3640$

Hence 84 is the least number which exactly divides 28, 42 and 84 i.e. we will get a remainder of 0 in this case. But we need the smallest number that, when divided by 35, 56 and 91 leaves remainder of 7 in each case.

Therefore = 3640 + 7 = 3647

Hence 36471 is smallest number that, when divided by 35, 56 and 91 leaves remainder of 7 in each case.

Q.11: A rectangular courtyard is 18m 72cm long and 13m 20 cm broad. It is to be paved with square tiles of the same size. Find the least possible number of such tiles.

Sol:

GIVEN: A rectangular yard is 18 m 72 cm long and 13 m 20 cm broad .It is to be paved with square tiles of the same size.

TO FIND: Least possible number of such tiles.

Length of the yard = 18 m 72 cm = 1800 cm + 72 cm = 1872 cm (therefore, 1 m = 100 cm)

Breadth of the yard = 13 in 20 cm = 1300 cm + 20 cm = 1320 cm

The size of the square tile of same size needed to the pave the rectangular yard is equals the HCF of the length and breadth of the rectangular yard.

Prime factorization of $1872 = 24 \times 32 \times 13$

Prime factorization of $1320 = 23 \times 3 \times 5 \times 11$

HCF of 1872 and $1320 = 23 \times 3 = 24$

Therefore, Length of side of the square tile = 24 cm

Number of tiles required = Area of the courtyard, Area of each tile = Length x Breadth

 $Side^2 = 1872 \text{ cm x } 1320 \text{ cm } 24 \text{ cm} = 4290.$

Thus, the least possible number of tiles required is 4290.

Q.12: Find the greatest number of 6 digits exactly divisible by 24, 15 and 36.

Sol:

TO FIND: Greatest number of 6 digits exactly divisible by 24, 15 and 36

The greatest 6 digit number be 999999 24, 15 and 36

 $24 = 2 \times 2 \times 2 \times 3$

$$15 = 3 \times 5$$

$$36 = 2 \times 2 \times 3 \times 3$$

L.C.M of 24, 15 and 36 = 360

Since, 999999360 = 2777x360 + 279Since, $\frac{999999}{360} = 2777x360 + 279$

Therefore, the remainder is 279. Hence the desired number is = 999999 – 279 = 9997201

Hence 9997201 is the greatest number of 6 digits exactly divisible by 24, 15 and 36.

Q.13: Determine the number nearest to 110000 but greater 100000 which is exactly divisible by each of 8, 15 and 21.

Sol:

TO FIND: The number nearest to 110000 but greater than 100000 which is exactly divisible by each of 8, 15 and 21.

L.C.M of 8, 15 and 21.

$$8 = 2 \times 2 \times 2$$

$$15 = 3 \times 5$$

$$21 = 3 \times 7$$

L.C.M of 8, 15 and 21 = $2^3 \times 3 \times 5 \times 71 = 840$

When 110000 is divided by 840, the remainder is obtained as 800.

Now, 110000 - 800 = 109200 is divisible by each of 8, 15 and 21.

Also, 110000 + 40 = 110040 is divisible by each of 8, 15 and 21.

109200 and 110040 are greater than 100000.

Hence, 110040 is the number nearest to 110000 but greater than 100000 which is exactly divisible by each of 8, 15 and 21.

Q.14: Find the least number that is divisible by all the numbers between 1 and 10 (both inclusive)

Sol:

| TO FIND: Least number that is divisible by all the numbers between 1 and 10 (both inclusive) Let us first find the L.C.M of all the numbers between 1 and 10 (both inclusive) |
|--|
| 1 = 1 |
| 2 = 2 |
| 3 = 3 |
| 4 = 2 x 2 |
| 5 = 5 |
| 6 = 2 x 3 |
| 7 = 7 |
| 8 = 2 x 2 x 2 |
| $9 = 3 \times 3$ |
| 10 = 2 x 5 |
| L.C.M 2520 |
| Hence 2520 is the least number that is divisible by all the numbers between 1 and 10 (both inclusive) |
| Q.15: A circular field has a circumference of 360km. three cyclists start together and can cycle 48, 60 and 72 km a day, round the field. When will they meet again? |
| Sol: |
| GIVEN: A circular field has a circumference of 360 km. Three cyclists start together and can cycle 48, |
| 60, and 72 km a day, round the field. |
| |
| 60, and 72 km a day, round the field. |
| 60, and 72 km a day, round the field. TO FIND: When they meet again. In order to calculate the time when they meet, we first find out the time taken by each cyclist in |
| 60, and 72 km a day, round the field. TO FIND: When they meet again. In order to calculate the time when they meet, we first find out the time taken by each cyclist in covering the distance. Number of days 1 st cyclist took to cover 360 km = Total distance covered in 1 day = 36048 = 7.5 = |
| 60, and 72 km a day, round the field. TO FIND: When they meet again. In order to calculate the time when they meet, we first find out the time taken by each cyclist in covering the distance. Number of days 1 st cyclist took to cover 360 km = Total distance covered in 1 day = 36048 = 7.5 = 7510 = 152 days |
| 60, and 72 km a day, round the field. TO FIND: When they meet again. In order to calculate the time when they meet, we first find out the time taken by each cyclist in covering the distance. Number of days 1 st cyclist took to cover 360 km = Total distance covered in 1 day = 36048 = 7.5 = 7510 = 152 days Similarly, number of days taken by 2 nd cyclist to cover same distance = 36060 = 6 days |
| 60, and 72 km a day, round the field. TO FIND: When they meet again. In order to calculate the time when they meet, we first find out the time taken by each cyclist in covering the distance. Number of days 1 st cyclist took to cover 360 km = Total distance covered in 1 day = 36048 = 7.5 = 7510 = 152 days Similarly, number of days taken by 2 nd cyclist to cover same distance = 36060 = 6 days Also, number of days taken by 3rd cyclist to cover this distance = 36072 = 5 days |

Q.16: In a morning walk three persons step off together, their steps measure 80cm, 85 cm and 90 cm respectively. What is the minimum distance each should walk so that he can cover the distance in complete steps?

Sol:

GIVEN: In a morning walk, three persons step off together. Their steps measure 80 cm, 85 cm and 90 cm.

TO FIND: minimum distance each should walk so that all can cover the same distance in complete steps.

The distance covered by each of them is required to be same as well as minimum. The required distance each should walk would be the L.C.M of the measures of their steps i.e. 80 cm, 85 cm, and 90 cm,

So we have to find the L.C.M of 80 cm, 85 cm, and 90 cm.

$$80 = 2^4 \times 5$$

$$85 = 17 \times 5$$

$$90 = 2 \times 3 \times 3 \times 5$$

L.C.M of 80, 85 and $90 = 2^4 \times 3 \times 3 \times 5 \times 17 = 12240 \text{ cm}$

Hence minimum 12240 cm distance each should walk so that all can cove the same distance in complete steps.