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# CAT

# Mathematics

Abhijit Guha



# CAT

# MATHEMATICS

(QUANTITATIVE ABILITY AND DATA INTERPRETATION  
FOR COMMON ADMISSION TEST)

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Delhi-110092

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**CAT MATHEMATICS**

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AMAR SONAMAA



*To*  
the loving memory of **My Mother**  
—Loving son



# Contents

Preface xvii

Acknowledgements xix

## A. LEVEL BOOST-UP SECTION

### 0. Vedic Mathematics

0-1-0-12

- 0.1 Introduction 1
- 0.2 Subtraction from Base 1
- 0.3 Multiplication Near a Base 2
  - 0.3.1 Number Just below the Base 2
  - 0.3.2 Numbers Just above the Base 3
  - 0.3.3 Number above and Number below the Base 3
- 0.4 Simple Multiplication 4
  - 0.4.1 Two 2-Digit Numbers 5
  - 0.4.2 Two 3-Digit Numbers 5
  - 0.4.3 Multiplication of Numbers with Different Bases 6
- 0.5 Multiplication by Repeating Numbers with Zeroes in between 6
- 0.6 Multiplication by Numbers with Zeroes in between 7
- 0.7 Squaring of Two Digit Number 0-7
  - 0.7.1 Express 26 0-8
  - 0.7.2 Beyond 75 0-8
- 0.8 Magic Squaring of 2-Digit Number 0-8
- 0.9 Magic Squaring of 3-Digit Number 0-9
- 0.10 Square Roots of Perfect Squares 0-10
- 0.11 Solution of Equations 0-10
- 0.12 Quadratic Equations 0-11

### RAPID CONCEPT (EXPRESSIONS, EQUATIONS AND INEQUATIONS)

1-1-1-3

### 1. Expressions, Equations and Inequations

1-4-1-55

- 1.1 Evaluating an Algebraic Expression 1-4
  - 1.1.1 Formula Method 1-4
  - 1.1.2 Assumption Method 1-6



1.2	Linear Equation	1-7	
1.2.1	Linear Equation in One Variable	1-7	
1.2.2	Word Problems on Linear Equation in One Variable; How to Solve	1-8	
1.2.3	Single Linear Equation in Two Variables	1-10	
1.2.4	Special Cases in Linear Equations	1-12	
1.3	Simultaneous Equations	1-12	
1.3.1	Solutions of Simultaneous Equations	1-13	
1.3.2	Number of Solutions of the Simultaneous Equations	1-14	
1.3.3	Word Problems	1-16	
1.4	Theory of Equations	1-16	
1.4.1	General Equation of the $n$ th Degree	1-16	
1.4.2	Properties of Equations and Their Roots	1-16	
1.4.3	Descartes Rule of Signs	1-17	
1.5	Quadratic Expression	1-19	
1.5.1	Graph of a Quadratic Expression	1-19	
1.6	Quadratic Equation	1-19	
1.6.1	Roots of the Quadratic Equation	1-20	
1.6.2	Nature of the Roots and Number of Solutions	1-20	
1.6.3	Sum and Product of the Roots	1-24	
1.6.4	Different Conditions of Roots	1-24	
1.6.5	Formation of Quadratic Equation	1-27	
1.6.6	Common Root(s)	1-28	
1.6.7	Sign of the Quadratic Expression $ax^2 + bx + c$	1-29	
1.6.8	Greatest and Least values of $ax^2 + bx + c$	1-31	
1.7	Modulus	1-32	
1.7.1	Basic Concept of Modulus	1-32	
1.7.2	Rule of Modulus Operation	1-32	
1.7.3	Alternative Solution of Modulus Equation by Origin Method	1-34	
1.7.4	Minimum Value of Modulus Expression	1-36	
1.8	Inequalities	1-37	
1.8.1	Introduction	1-37	
1.8.2	Theorem on Inequalities	1-37	
1.8.3	Comparison of Two Inequalities	1-38	
1.8.4	Important Inequality Theorem	1-39	
1.8.5	Solving the Inequalities	1-40	
1.9	Number of Integral Solutions	1-50	
	<i>Check Your Progress</i>	1-53	

**RAPID CONCEPT (FUNCTIONS)****2-1-2-2****2. Functions****2-3-2-33**

2.1	Definition	2-3	
2.2	Domain and Range	2-4	
2.2.1	Finding Domain and Range	2-4	
2.2.2	Restricted Domain and Range	2-5	
2.3	Composite Functions	2-6	
2.3.1	Domain and Range of a Composite Function	2-7	
2.3.2	Evaluation of Composite Functions	2-8	

2.4	Inverse Function	2-9
2.4.1	Finding Inverse of a Given Function	2-10
2.4.2	Graphing Inverse Functions	2-12
2.4.3	Inverse of Composite Functions	2-12
2.5	Odd and Even Function	2-13
2.5.1	Properties of Odd and Even Functions	2-15
2.6	Greatest Integer Function	2-16
2.7	Arithmetic Combinations of Functions	2-17
2.8	Equality of Function	2-17
2.8.1	For Single Function	2-17
2.8.2	For Composite Function	2-18
2.9	Minimum and Maximum Values of Function	2-19
2.10	Evaluation of Function	2-23
2.10.1	Direct Evaluation	2-23
2.10.2	Evaluation by Deduction	2-25
2.10.3	Evaluation of Composition of Log Function	2-28
2.10.4	Evaluation of Function of Two Variables	2-29
2.11	Important Deductions on Functions	2-30
2.12	Functional Equation of a Function	2-30
	<i>Check Your Progress</i>	2-31

**RAPID CONCEPT (PERMUTATION AND COMBINATION)**

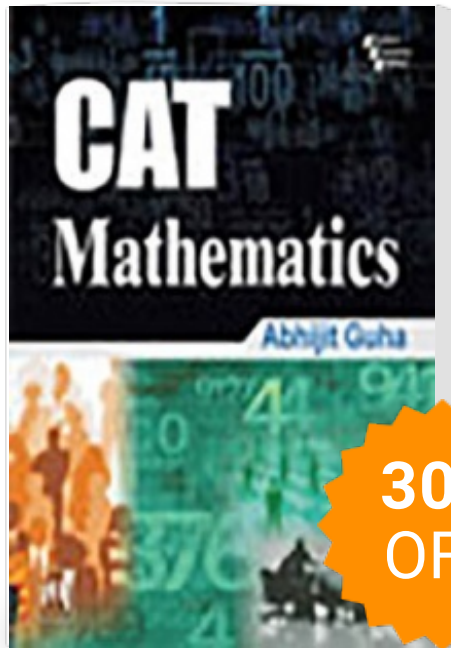
**3-1-3-2**

**3. Permutation and Combination**

**3-3-3-33**

3.1	Introduction	3-3
3.2	Fundamental Counting Principle	3-3
3.3	Permutation	3-5
3.3.1	Use of Number of Choices Available	3-6
3.4	Factorial Function	3-6
3.4.1	Use of $!$ in Permutation	3-7
3.5	Restricted Use of ${}^n P_r$	3-7
3.5.1	When Order does Not Matter	3-8
3.6	Arrangement with Repetition of Objects	3-8
3.6.1	Direct Use of $K^n$	3-9
3.7	Concept of Step Arrangement	3-11
3.8	Permutation of Things When Some of Them are Identical	3-11
3.9	Combination	3-14
3.9.1	Meaning of ${}^n C_r$	3-14
3.10	Concept of $2^n$ (Rule of Maximum Possible Selection)	3-19
3.10.1	Concept of Never Together	3-22
3.11	Division of Things into Groups	3-22
3.12	Distribution of Things	3-24
3.12.1	Distribution of $n$ Identical Things into $r$ Different Box	3-24
3.12.2	Distribution of $n$ Different Things in $r$ Identical Boxes	3-25
3.12.3	Distribution of $n$ Identical Things in $r$ Identical Boxes	3-26
3.13	Arrangement in a Circle	3-27
	<i>Check Your Progress</i>	3-29

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