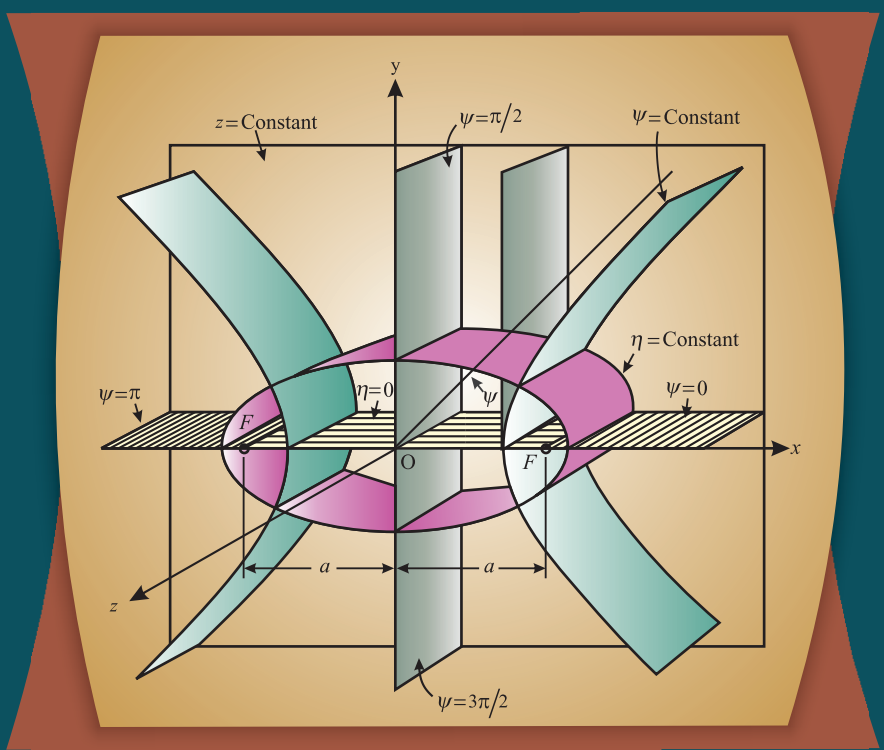
Eastern Economy Edition

# ELECTROMAGNETISM

## Volume 1

## (Theory)




Ashutosh Pramanik

# ELECTROMAGNETISM

## Volume 1
## Theory

**ASHUTOSH PRAMANIK**
Professor Emeritus, College of Engineering, Pune
Formerly of Corporate Research and Development Division, BHEL
(Senior Dy. General Manager)
*and*
The Universities of Birmingham and Leeds
(Research Engineer and Lecturer)
*and*
D.J. Gandhi Distinguished Visiting Professor, IIT Bombay

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**ELECTROMAGNETISM VOLUME 1 (THEORY)**
Ashutosh Pramanik

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To the revered memory of my parents
**Tarapada Pramanik** and **Renubala Pramanik**
whose encouragement and support for my professional career
made this book possible
*and*
to all my family members
My wife **Lalita Pramanik**
my daughter **Mrinmayee** and son-in-law **Sreekant Advant**
and (last but not the least) my grandson
**Om Advant**
for their love and concern for the book

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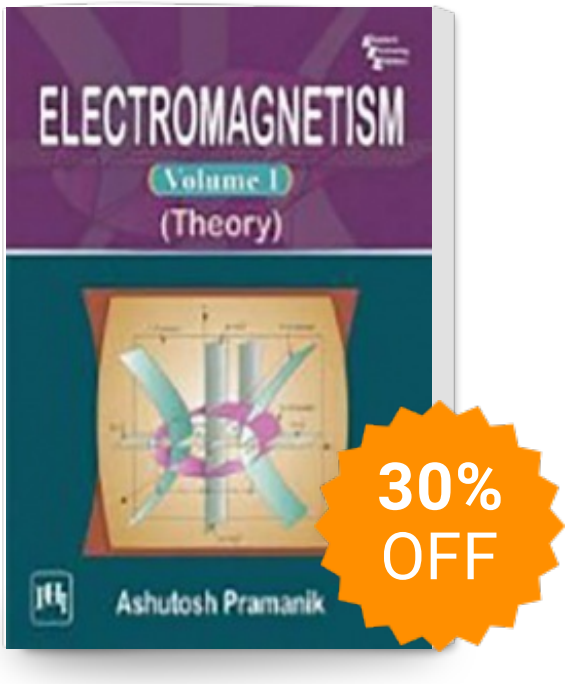
# Electromagnetism: Volume 1: Theory

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